



# Chapter 11

## Data Link Control

# 11-1 FRAMING

*The data link layer needs to pack bits into **frames**, so that each frame is distinguishable from another. Our postal system practices a type of framing. The simple act of inserting a letter into an envelope separates one piece of information from another; the envelope serves as the delimiter.*

*Topics discussed in this section:*

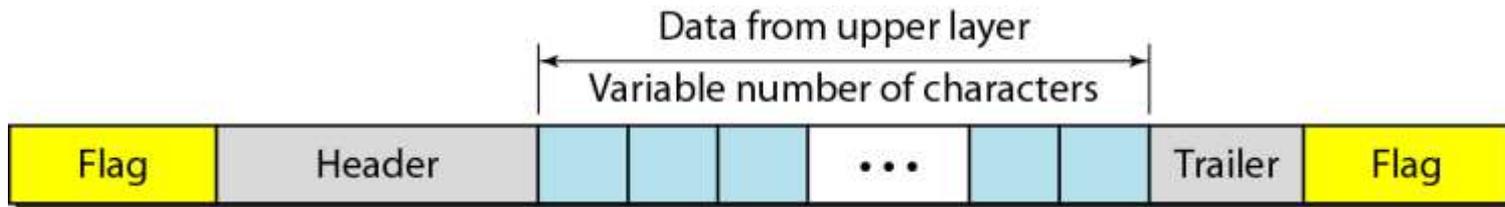
**Fixed-Size Framing**

**Variable-Size Framing**

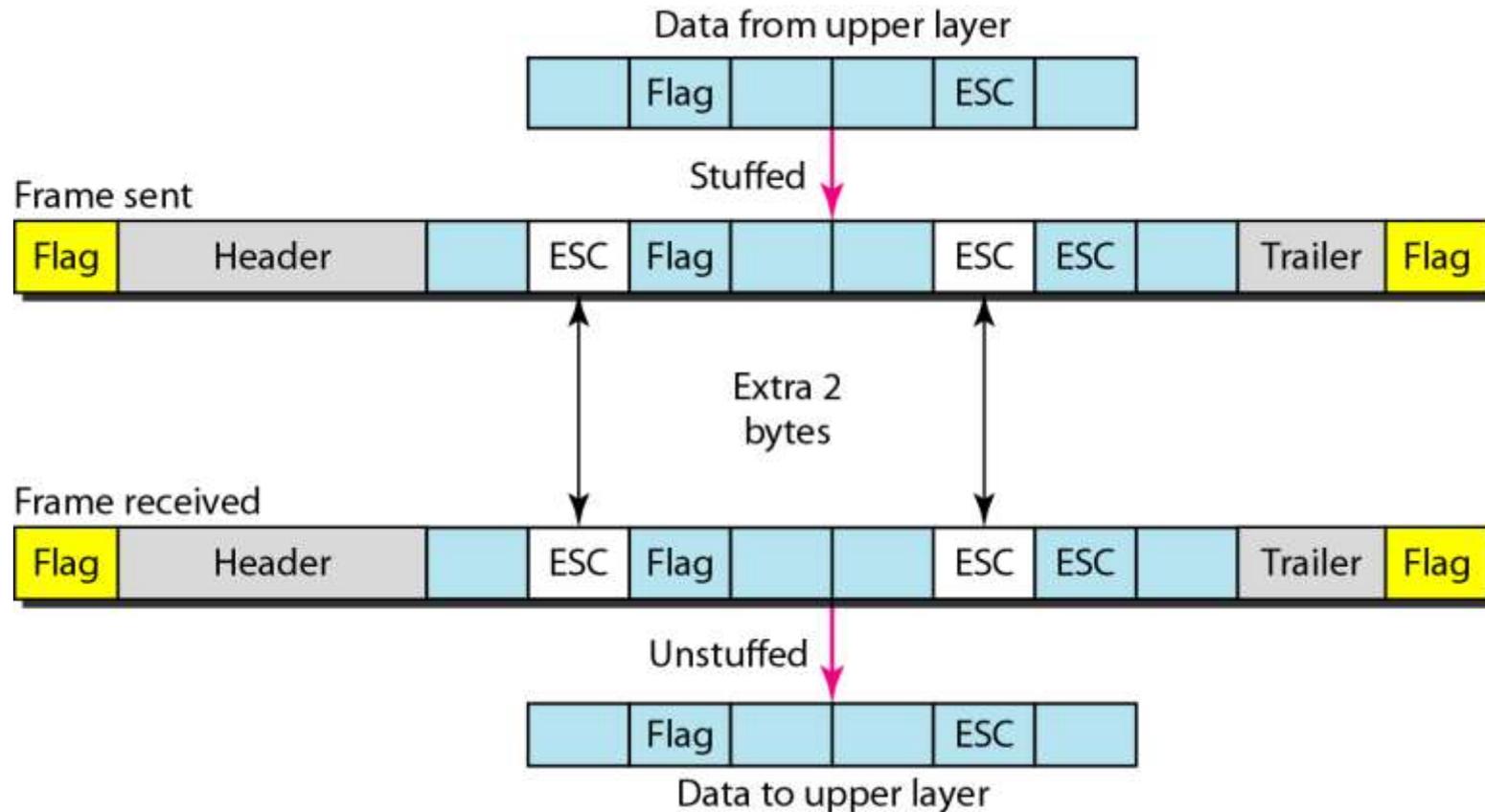
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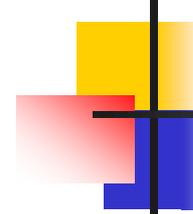
**Figure 11.1** *A frame in a character-oriented protocol*

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**Figure 11.2** *Byte stuffing and unstuffing*

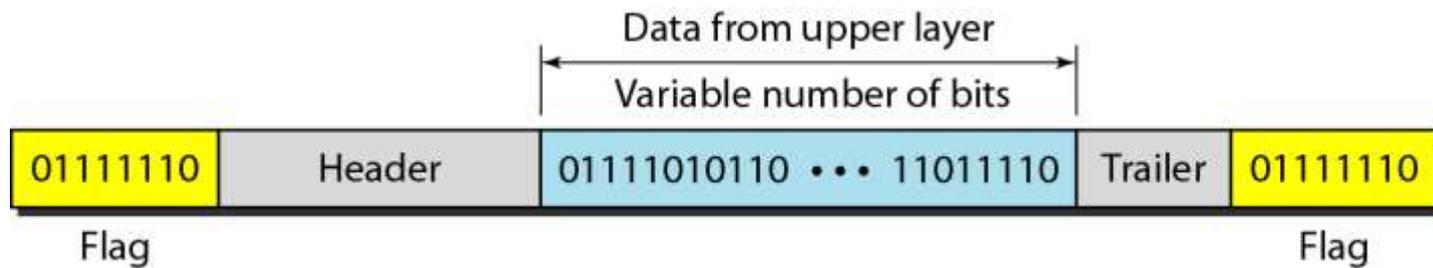


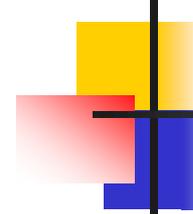


*Note*

**Byte stuffing is the process of adding 1 extra byte whenever there is a flag or escape character in the text.**

**Figure 11.3** *A frame in a bit-oriented protocol*

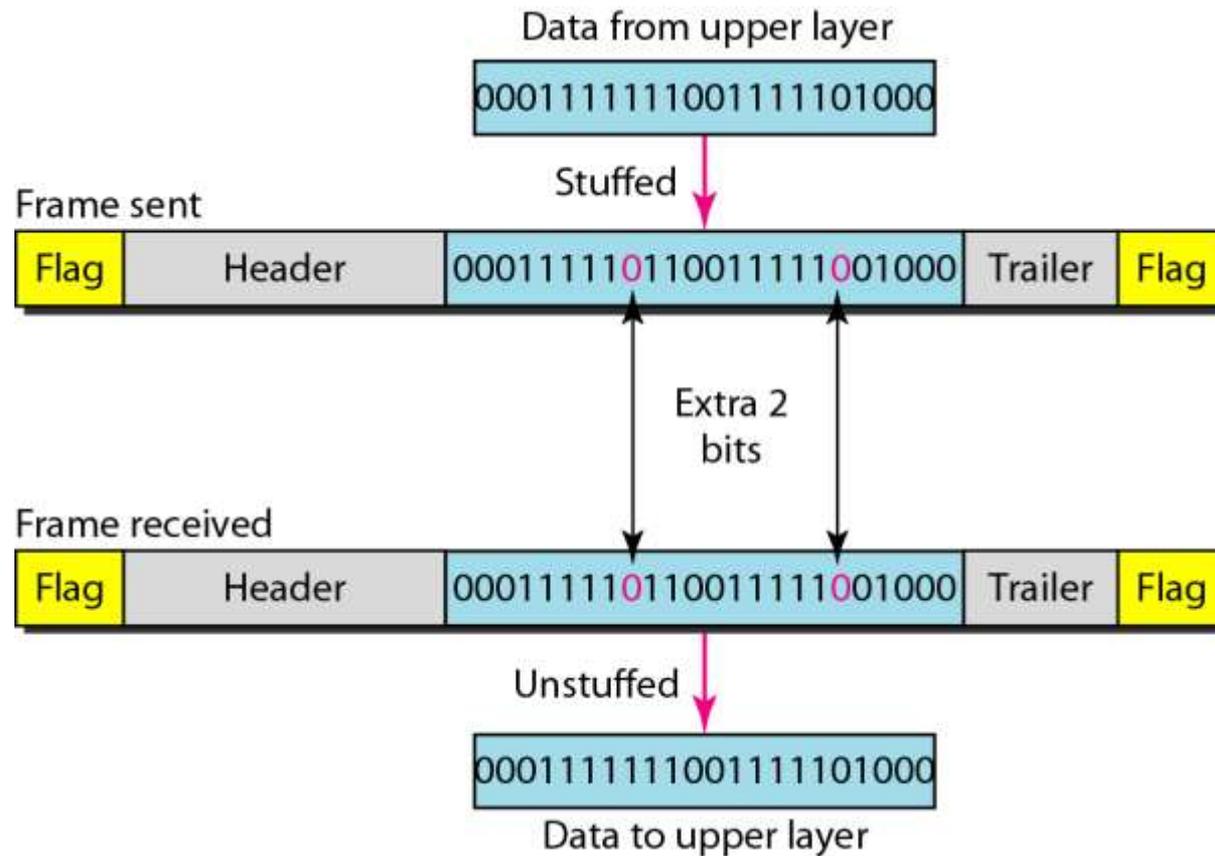




*Note*

**Bit stuffing is the process of adding one extra 0 whenever five consecutive 1s follow a 0 in the data, so that the receiver does not mistake the pattern 011110 for a flag.**

**Figure 11.4** *Bit stuffing and unstuffing*



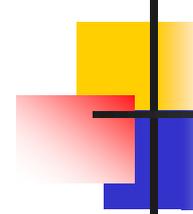
## 11-2 FLOW AND ERROR CONTROL

*The most important responsibilities of the data link layer are **flow control** and **error control**. Collectively, these functions are known as **data link control**.*

*Topics discussed in this section:*

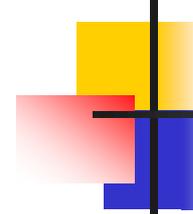
**Flow Control**

**Error Control**



*Note*

**Flow control refers to a set of procedures used to restrict the amount of data that the sender can send before waiting for acknowledgment.**



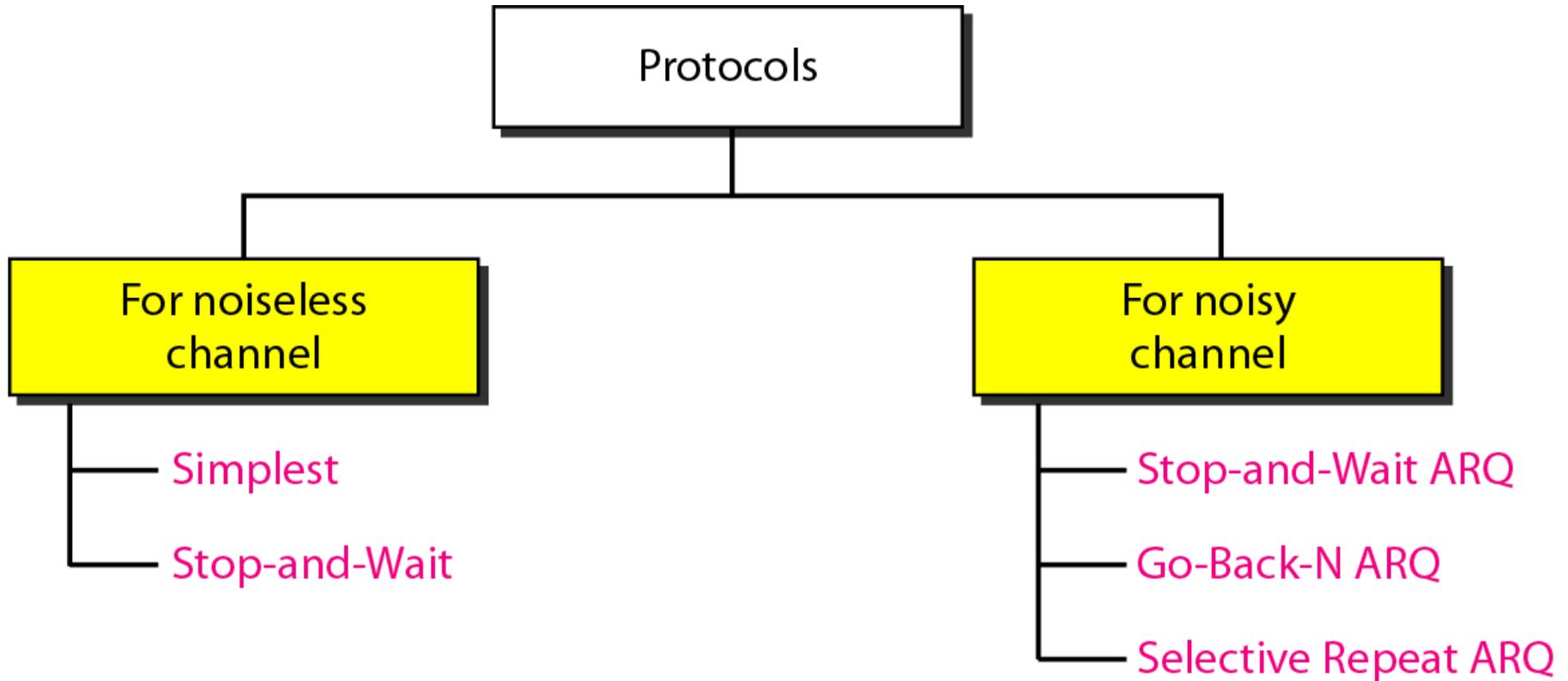
*Note*

**Error control in the data link layer is based on automatic repeat request, which is the retransmission of data.**

## 11-3 PROTOCOLS

*Now let us see how the data link layer can combine framing, flow control, and error control to achieve the delivery of data from one node to another. The protocols are normally implemented in software by using one of the common programming languages. To make our discussions language-free, we have written in pseudocode a version of each protocol that concentrates mostly on the procedure instead of delving into the details of language rules.*

**Figure 11.5** *Taxonomy of protocols discussed in this chapter*



## 11-4 NOISELESS CHANNELS

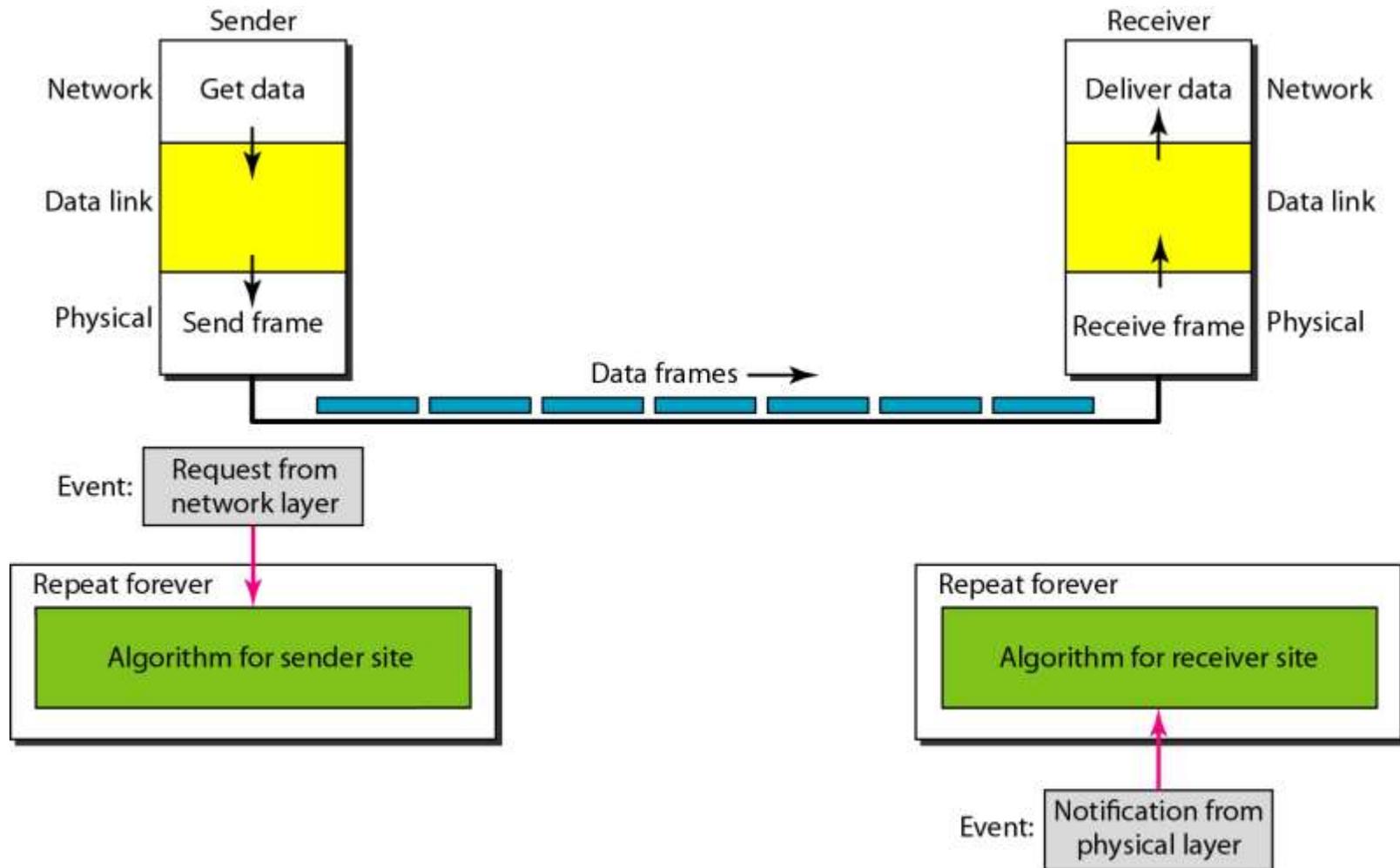
*Let us first assume we have an ideal channel in which no frames are lost, duplicated, or corrupted. We introduce two protocols for this type of channel.*

*Topics discussed in this section:*

**Simplest Protocol**

**Stop-and-Wait Protocol**

**Figure 11.6** *The design of the simplest protocol with no flow or error control*

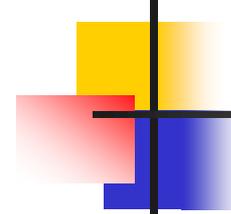


## Algorithm 11.1 *Sender-site algorithm for the simplest protocol*

```
1 while(true) // Repeat forever
2 {
3   WaitForEvent(); // Sleep until an event occurs
4   if(Event(RequestToSend)) //There is a packet to send
5   {
6     GetData();
7     MakeFrame();
8     SendFrame(); //Send the frame
9   }
10 }
```

## Algorithm 11.2 Receiver-site algorithm for the simplest protocol

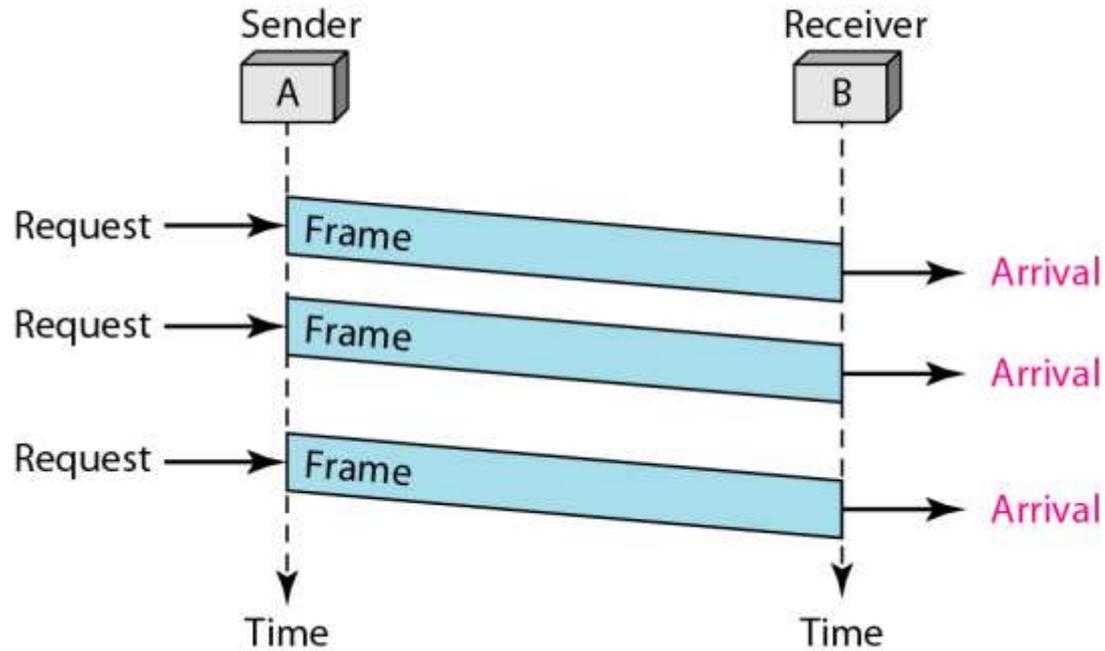
```
1 while(true) // Repeat forever
2 {
3   WaitForEvent(); // Sleep until an event occurs
4   if(Event(ArrivalNotification)) //Data frame arrived
5   {
6     ReceiveFrame();
7     ExtractData();
8     DeliverData(); //Deliver data to network layer
9   }
10 }
```



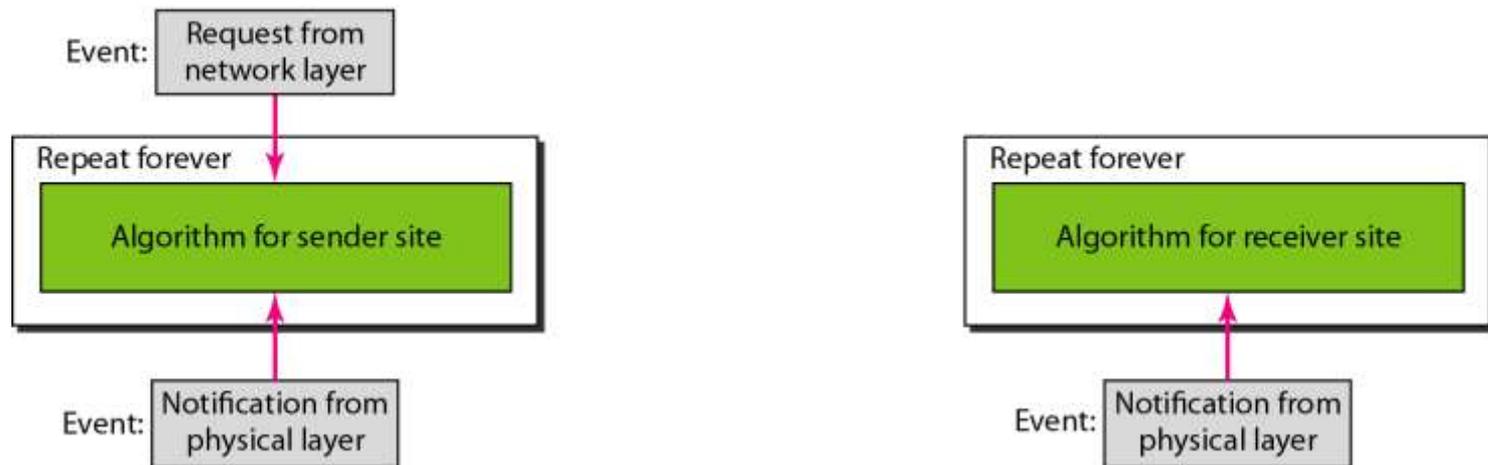
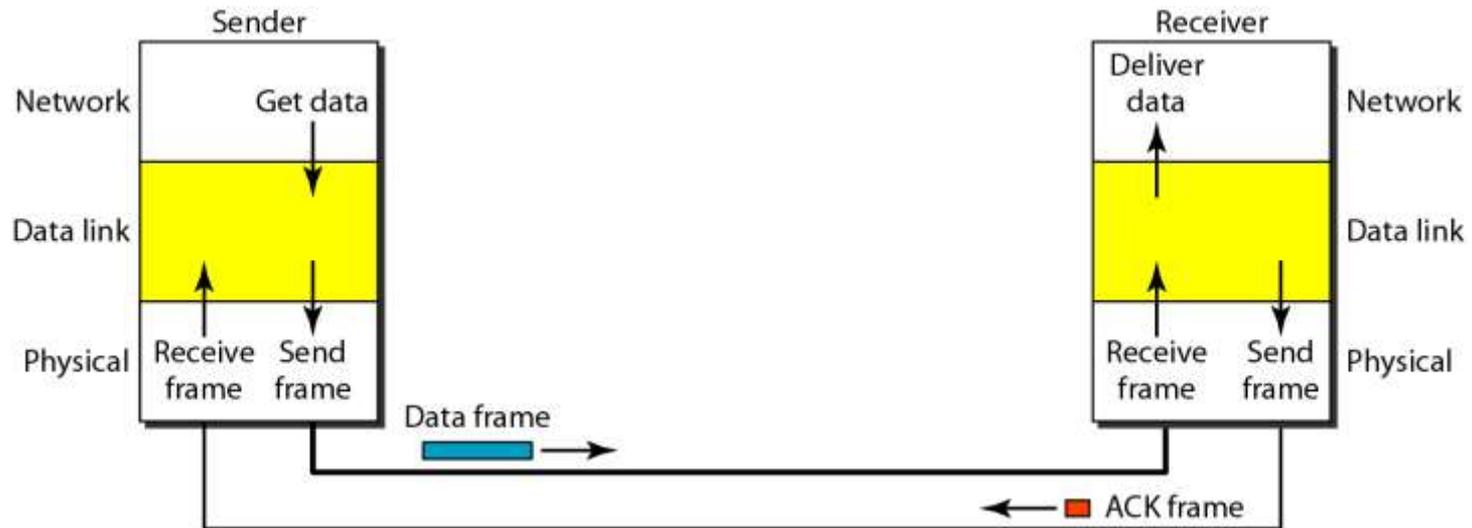
## *Example 11.1*

*Figure 11.7 shows an example of communication using this protocol. It is very simple. The sender sends a sequence of frames without even thinking about the receiver. To send three frames, three events occur at the sender site and three events at the receiver site. Note that the data frames are shown by tilted boxes; the height of the box defines the transmission time difference between the first bit and the last bit in the frame.*

**Figure 11.7** *Flow diagram for Example 11.1*



**Figure 11.8** *Design of Stop-and-Wait Protocol*

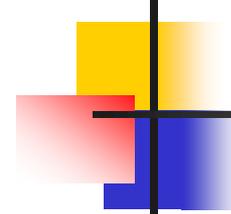


### Algorithm 11.3 *Sender-site algorithm for Stop-and-Wait Protocol*

```
1 while(true) //Repeat forever
2 canSend = true //Allow the first frame to go
3 {
4   WaitForEvent(); // Sleep until an event occurs
5   if(Event(RequestToSend) AND canSend)
6   {
7     GetData();
8     MakeFrame();
9     SendFrame(); //Send the data frame
10    canSend = false; //Cannot send until ACK arrives
11  }
12  WaitForEvent(); // Sleep until an event occurs
13  if(Event(ArrivalNotification) // An ACK has arrived
14  {
15    ReceiveFrame(); //Receive the ACK frame
16    canSend = true;
17  }
18 }
```

## Algorithm 11.4 Receiver-site algorithm for Stop-and-Wait Protocol

```
1 while(true) //Repeat forever
2 {
3   WaitForEvent(); // Sleep until an event occurs
4   if(Event(ArrivalNotification)) //Data frame arrives
5   {
6     ReceiveFrame();
7     ExtractData();
8     Deliver(data); //Deliver data to network layer
9     SendFrame(); //Send an ACK frame
10  }
11 }
```

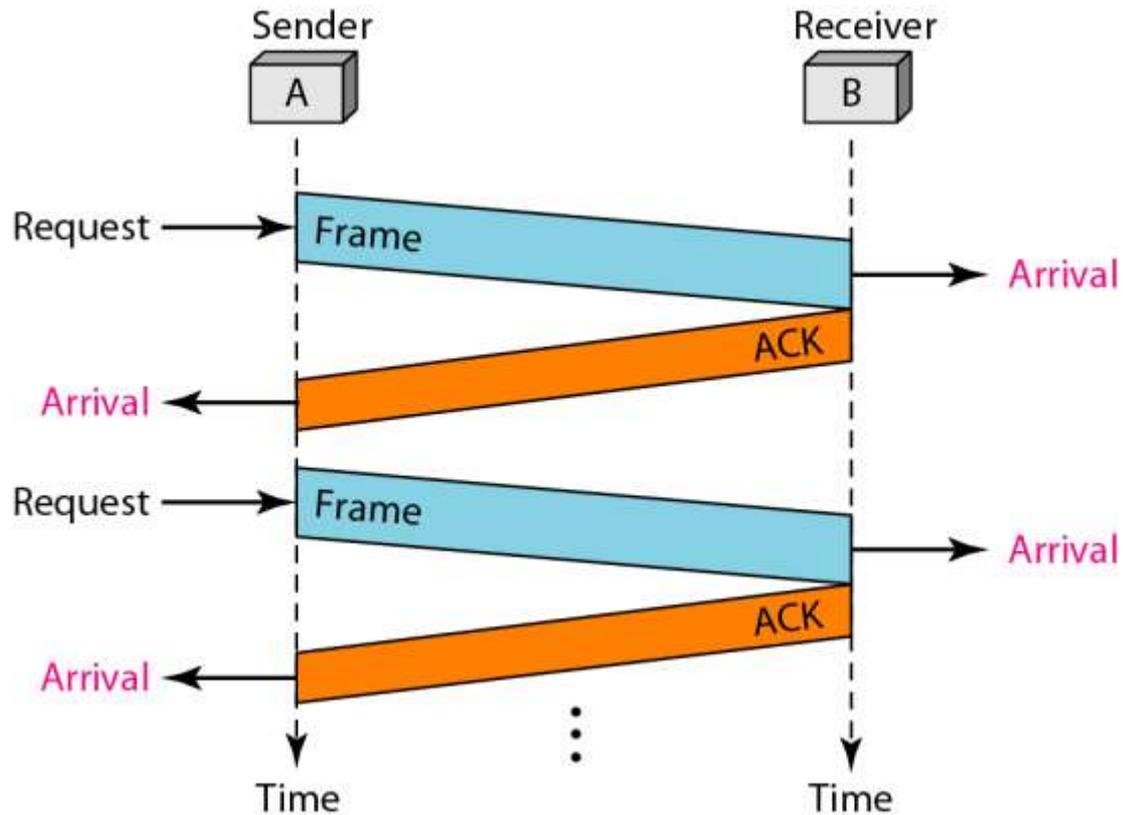


## *Example 11.2*

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*Figure 11.9 shows an example of communication using this protocol. It is still very simple. The sender sends one frame and waits for feedback from the receiver. When the ACK arrives, the sender sends the next frame. Note that sending two frames in the protocol involves the sender in four events and the receiver in two events.*

**Figure 11.9** *Flow diagram for Example 11.2*



## 11-5 NOISY CHANNELS

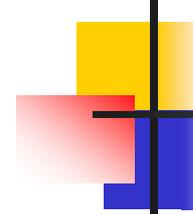
*Although the Stop-and-Wait Protocol gives us an idea of how to add flow control to its predecessor, noiseless channels are nonexistent. We discuss three protocols in this section that use error control.*

**Topics discussed in this section:**

**Stop-and-Wait Automatic Repeat Request**

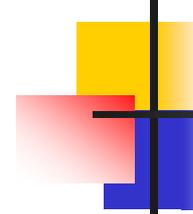
**Go-Back-N Automatic Repeat Request**

**Selective Repeat Automatic Repeat Request**



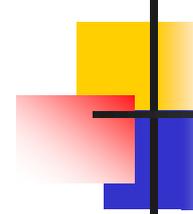
*Note*

**Error correction in Stop-and-Wait ARQ is done by keeping a copy of the sent frame and retransmitting of the frame when the timer expires.**



*Note*

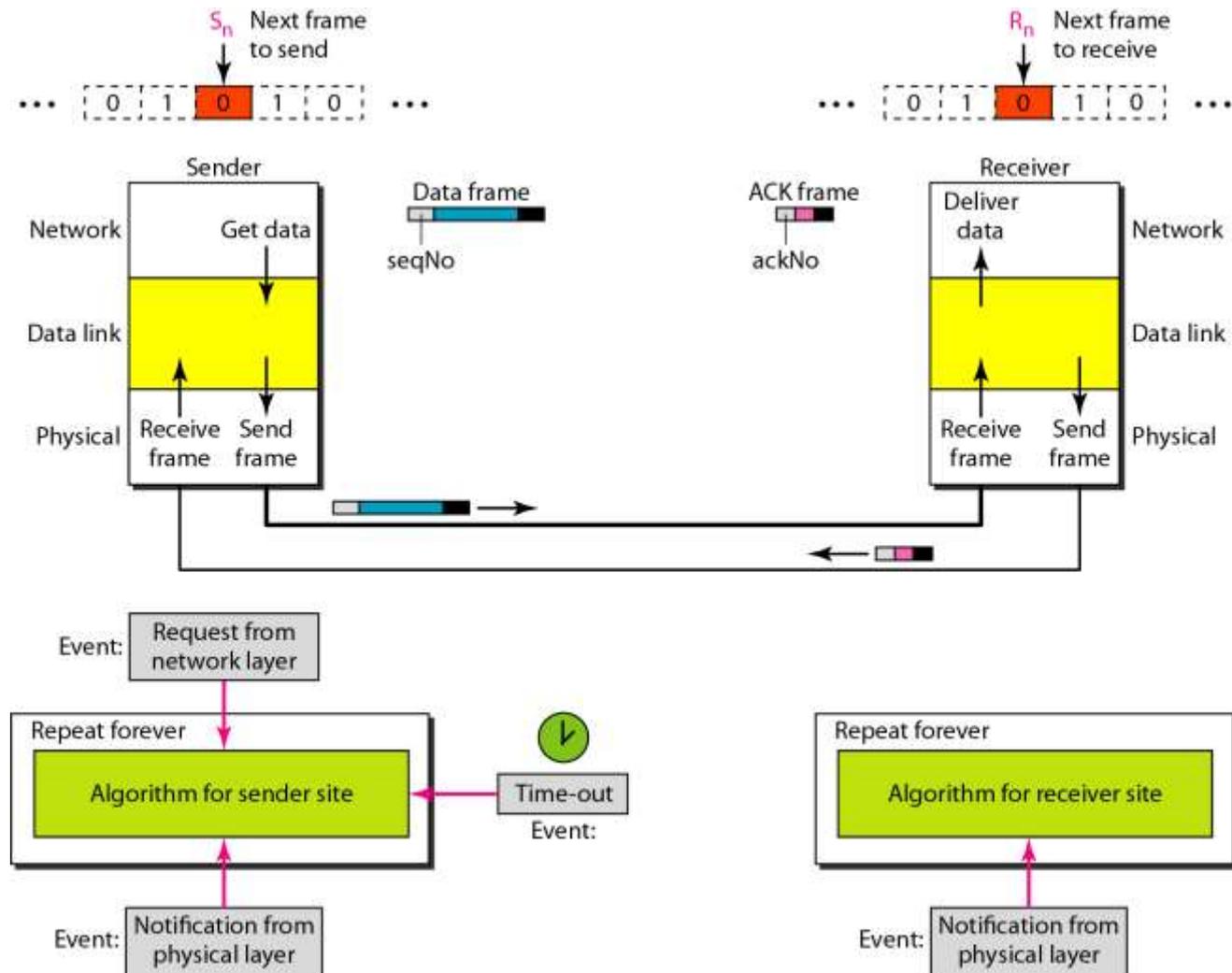
**In Stop-and-Wait ARQ, we use sequence numbers to number the frames.  
The sequence numbers are based on modulo-2 arithmetic.**



*Note*

**In Stop-and-Wait ARQ, the acknowledgment number always announces in modulo-2 arithmetic the sequence number of the next frame expected.**

**Figure 11.10** *Design of the Stop-and-Wait ARQ Protocol*



## Algorithm 11.5 *Sender-site algorithm for Stop-and-Wait ARQ*

```
1  Sn = 0;           // Frame 0 should be sent first
2  canSend = true;    // Allow the first request to go
3  while(true)       // Repeat forever
4  {
5      WaitForEvent(); // Sleep until an event occurs
6      if(Event(RequestToSend) AND canSend)
7      {
8          GetData();
9          MakeFrame(Sn); //The seqNo is Sn
10         StoreFrame(Sn); //Keep copy
11         SendFrame(Sn);
12         StartTimer();
13         Sn = Sn + 1;
14         canSend = false;
15     }
16     WaitForEvent(); // Sleep
```

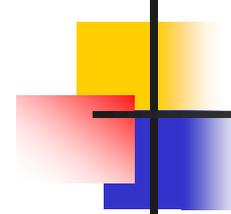
*(continued)*

## Algorithm 11.5 *Sender-site algorithm for Stop-and-Wait ARQ* (continued)

```
17   if(Event(ArrivalNotification)           // An ACK has arrived
18   {
19       ReceiveFrame(ackNo);                 //Receive the ACK frame
20       if(not corrupted AND ackNo == Sn) //Valid ACK
21       {
22           Stoptimer();
23           PurgeFrame(Sn-1);               //Copy is not needed
24           canSend = true;
25       }
26   }
27
28   if(Event(TimeOut)                       // The timer expired
29   {
30       StartTimer();
31       ResendFrame(Sn-1);                 //Resend a copy check
32   }
33 }
```

## Algorithm 11.6 Receiver-site algorithm for Stop-and-Wait ARQ Protocol

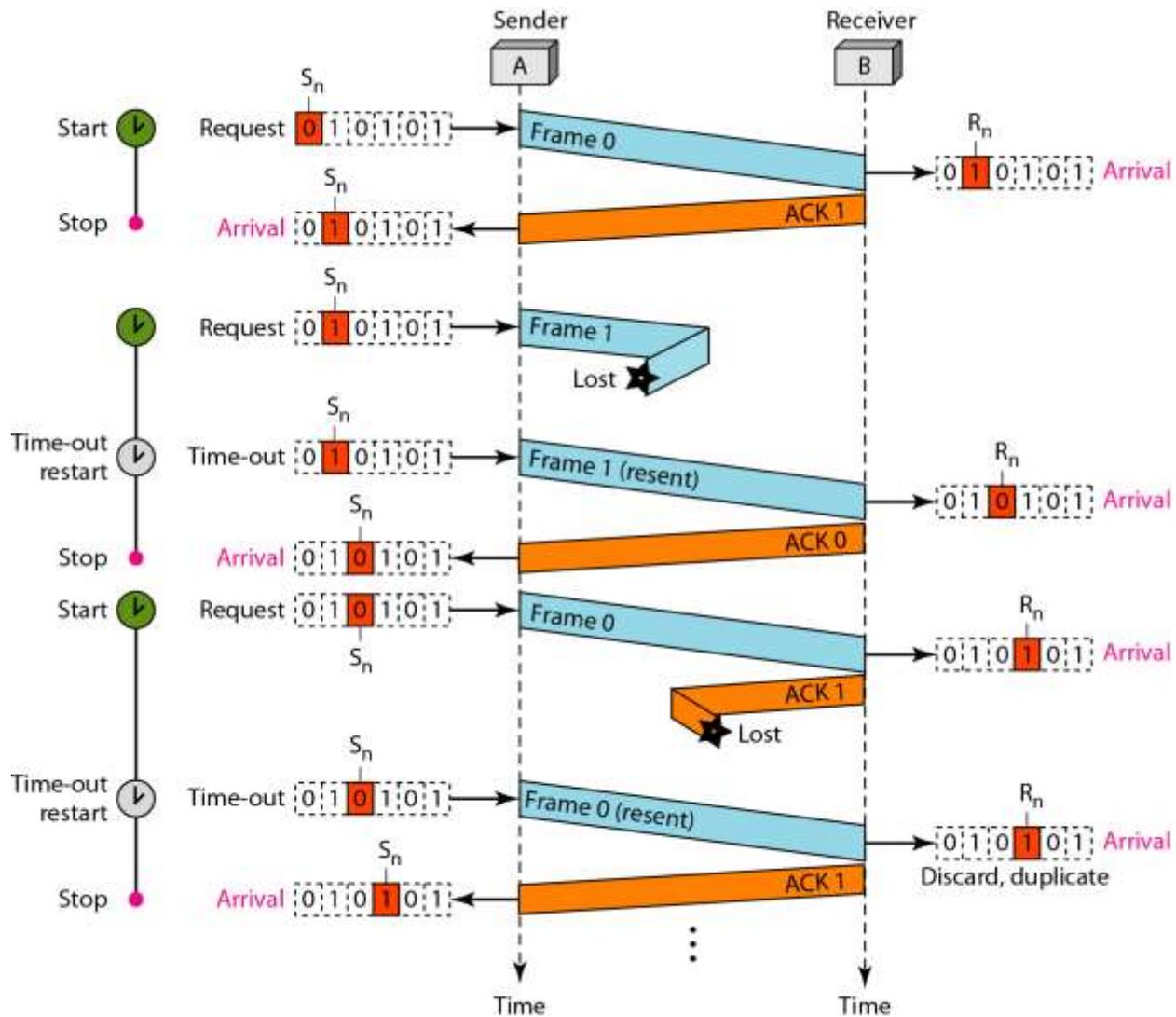
```
1  Rn = 0; // Frame 0 expected to arrive first
2  while(true)
3  {
4      WaitForEvent(); // Sleep until an event occurs
5      if(Event(ArrivalNotification)) //Data frame arrives
6      {
7          ReceiveFrame();
8          if(corrupted(frame));
9              sleep();
10         if(seqNo == Rn) //Valid data frame
11         {
12             ExtractData();
13             DeliverData(); //Deliver data
14             Rn = Rn + 1;
15         }
16         SendFrame(Rn); //Send an ACK
17     }
18 }
```



## Example 11.3

*Figure 11.11 shows an example of **Stop-and-Wait ARQ**. Frame 0 is sent and acknowledged. Frame 1 is lost and resent after the time-out. The resent frame 1 is acknowledged and the timer stops. Frame 0 is sent and acknowledged, but the acknowledgment is lost. The sender has no idea if the frame or the acknowledgment is lost, so after the time-out, it resends frame 0, which is acknowledged.*

**Figure 11.11** *Flow diagram for Example 11.3*



## *Example 11.4*

*Assume that, in a Stop-and-Wait ARQ system, the bandwidth of the line is 1 Mbps, and 1 bit takes 20 ms to make a round trip. What is the bandwidth-delay product? If the system data frames are 1000 bits in length, what is the utilization percentage of the link?*

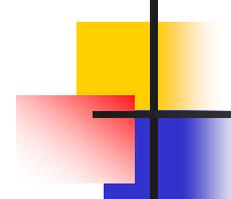
### **Solution**

**The bandwidth-delay product is**

$$(1 \times 10^6) \times (20 \times 10^{-3}) = 20,000 \text{ bits}$$

## *Example 11.4 (continued)*

*The system can send 20,000 bits during the time it takes for the data to go from the sender to the receiver and then back again. However, the system sends only 1000 bits. We can say that the link utilization is only  $1000/20,000$ , or 5 percent. For this reason, for a link with a high bandwidth or long delay, the use of Stop-and-Wait ARQ wastes the capacity of the link.*

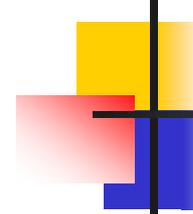


## *Example 11.5*

*What is the utilization percentage of the link in Example 11.4 if we have a protocol that can send up to 15 frames before stopping and worrying about the acknowledgments?*

### *Solution*

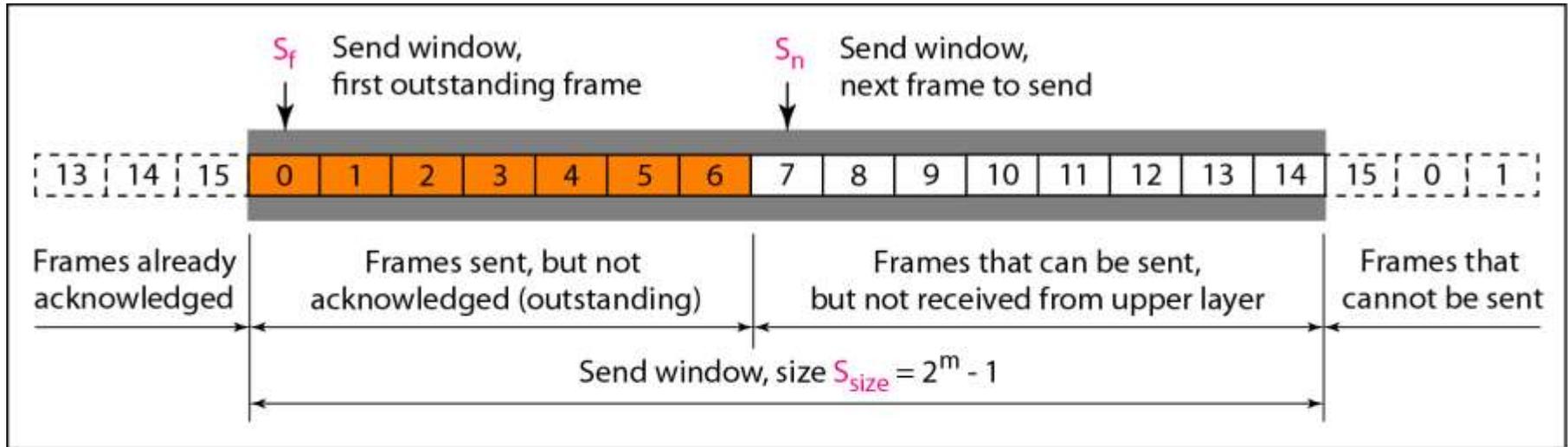
*The bandwidth-delay product is still 20,000 bits. The system can send up to 15 frames or 15,000 bits during a round trip. This means the utilization is  $15,000/20,000$ , or **75** percent. Of course, if there are damaged frames, the utilization percentage is much less because frames have to be resent.*



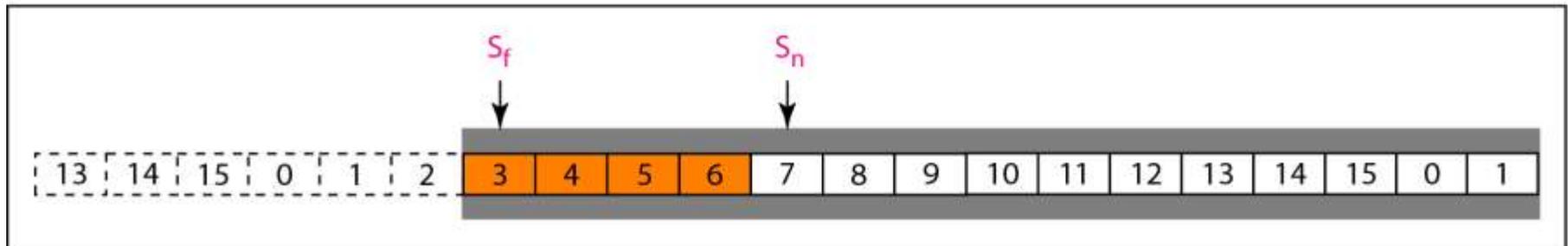
*Note*

**In the Go-Back-N Protocol, the sequence numbers are modulo  $2^m$ , where  $m$  is the size of the sequence number field in bits.**

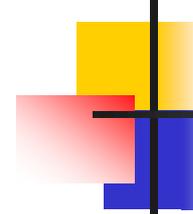
**Figure 11.12** *Send window for Go-Back-N ARQ*



a. Send window before sliding

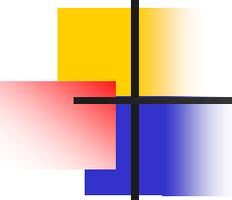


b. Send window after sliding



*Note*

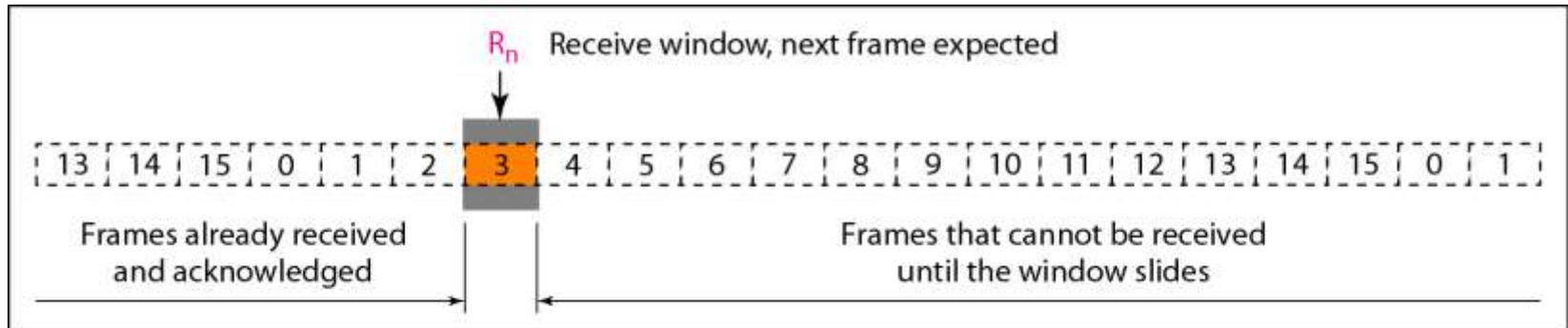
**The send window is an abstract concept defining an imaginary box of size  $2^m - 1$  with three variables:  $S_f$ ,  $S_n$ , and  $S_{size}$ .**



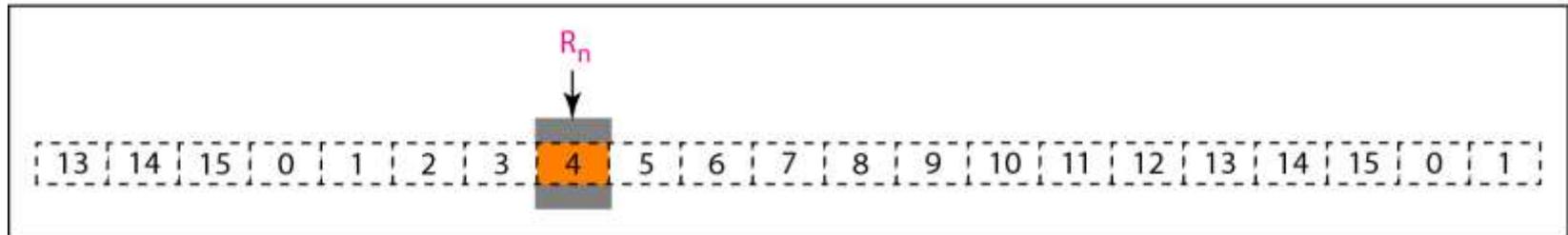
*Note*

**The send window can slide one or more slots when a valid acknowledgment arrives.**

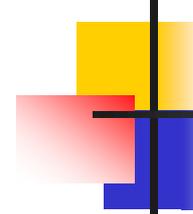
**Figure 11.13** *Receive window for Go-Back-N ARQ*



a. Receive window



b. Window after sliding

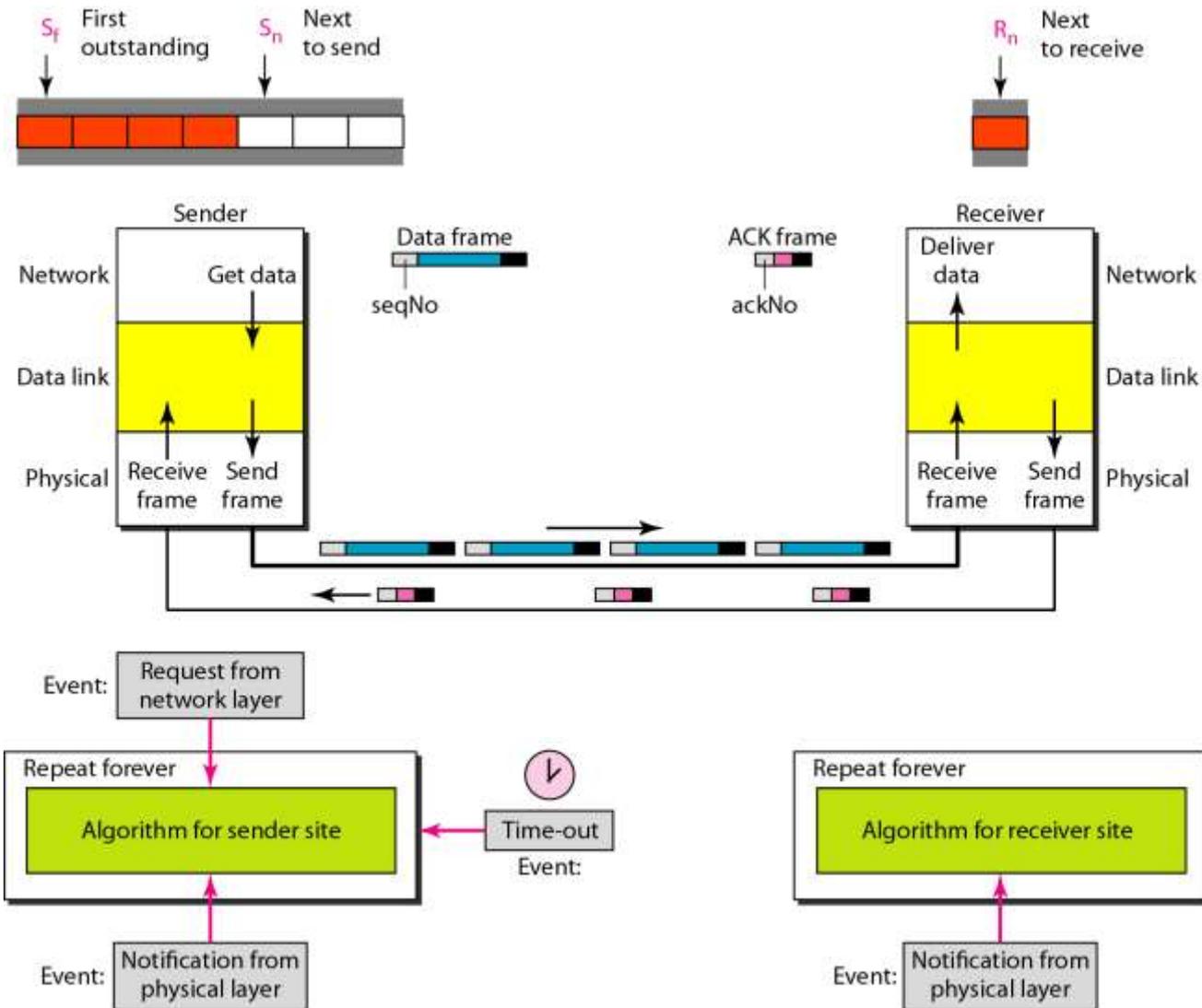


*Note*

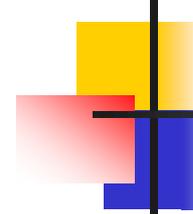
**The receive window is an abstract concept defining an imaginary box of size 1 with one single variable  $R_n$ .**

**The window slides when a correct frame has arrived; sliding occurs one slot at a time.**

**Figure 11.14** *Design of Go-Back-N ARQ*







*Note*

**In Go-Back-N ARQ, the size of the send window must be less than  $2^m$ ; the size of the receiver window is always 1.**

## Algorithm 11.7 *Go-Back-N sender algorithm*

```
1   $S_w = 2^m - 1;$ 
2   $S_f = 0;$ 
3   $S_n = 0;$ 
4
5  while (true)                                //Repeat forever
6  {
7    WaitForEvent();
8    if(Event(RequestToSend))                  //A packet to send
9    {
10     if( $S_n - S_f \geq S_w$ )                    //If window is full
11         Sleep();
12     GetData();
13     MakeFrame( $S_n$ );
14     StoreFrame( $S_n$ );
15     SendFrame( $S_n$ );
16      $S_n = S_n + 1;$ 
17     if(timer not running)
18         StartTimer();
19 }
20
```

**(continued)**

```
21  if(Event(ArrivalNotification))  //ACK arrives
22  {
23      Receive(ACK);
24      if(corrupted(ACK))
25          Sleep();
26      if((ackNo>Sf)&&(ackNo<=Sn))  //If a valid ACK
27      While(Sf <= ackNo)
28          {
29              PurgeFrame(Sf);
30              Sf = Sf + 1;
31          }
32      StopTimer();
33  }
34
35  if(Event(TimeOut))  //The timer expires
36  {
37      StartTimer();
38      Temp = Sf;
39      while(Temp < Sn);
40      {
41          SendFrame(Sf);
42          Sf = Sf + 1;
43      }
44  }
45 }
```

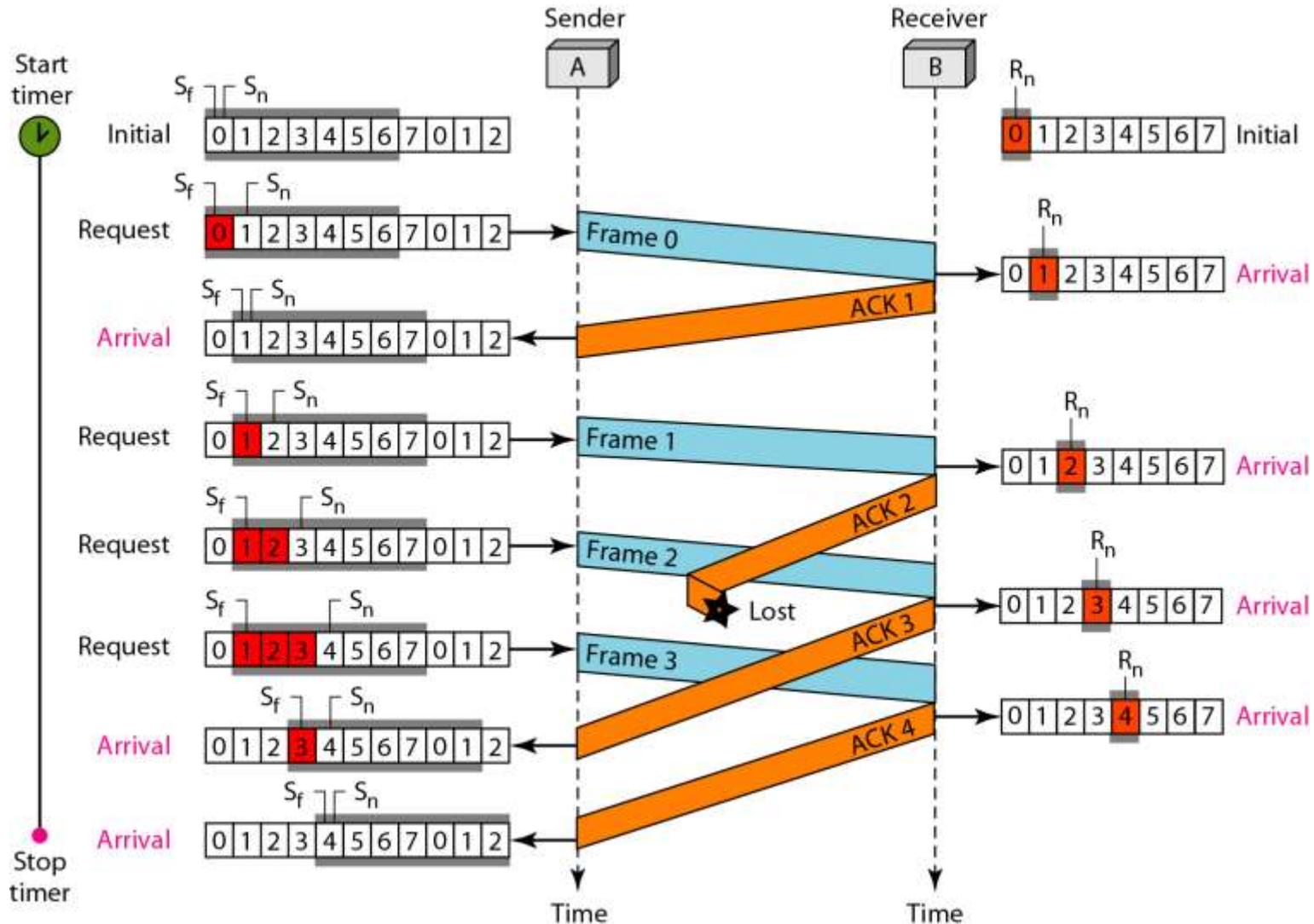
## Algorithm 11.8 *Go-Back-N receiver algorithm*

```
1  Rn = 0;
2
3  while (true)                //Repeat forever
4  {
5      WaitForEvent();
6
7      if(Event(ArrivalNotification)) //Data frame arrives
8      {
9          Receive(Frame);
10         if(corrupted(Frame))
11             Sleep();
12         if(seqNo == Rn)        //If expected frame
13         {
14             DeliverData();      //Deliver data
15             Rn = Rn + 1;        //Slide window
16             SendACK(Rn);
17         }
18     }
19 }
```

## *Example 11.6*

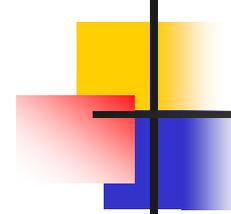
*Figure 11.16 shows an example of Go-Back-N. This is an example of a case where the forward channel is reliable, but the reverse is not. No data frames are lost, but some ACKs are delayed and one is lost. The example also shows how cumulative acknowledgments can help if acknowledgments are delayed or lost. After initialization, there are seven sender events. Request events are triggered by data from the network layer; arrival events are triggered by acknowledgments from the physical layer. There is no time-out event here because all outstanding frames are acknowledged before the timer expires. Note that although ACK 2 is lost, ACK 3 serves as both ACK 2 and ACK 3.*

**Figure 11.16** *Flow diagram for Example 11.6*



## *Example 11.7*

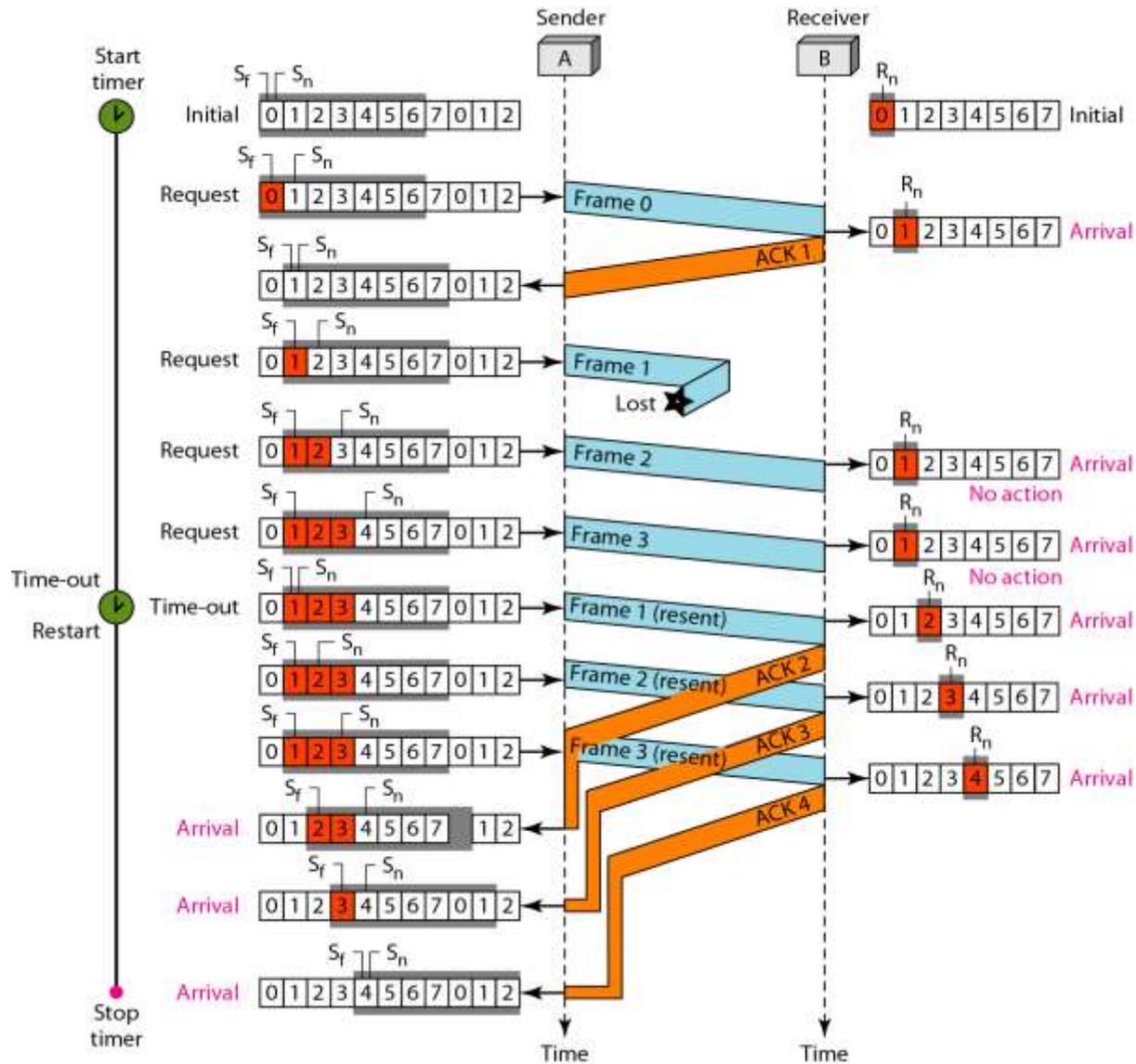
*Figure 11.17 shows what happens when a frame is lost. Frames 0, 1, 2, and 3 are sent. However, frame 1 is lost. The receiver receives frames 2 and 3, but they are discarded because they are received out of order. The sender receives no acknowledgment about frames 1, 2, or 3. Its timer finally expires. The sender sends all outstanding frames (1, 2, and 3) because it does not know what is wrong. Note that the resending of frames 1, 2, and 3 is the response to one single event. When the sender is responding to this event, it cannot accept the triggering of other events. This means that when ACK 2 arrives, the sender is still busy with sending frame 3.*

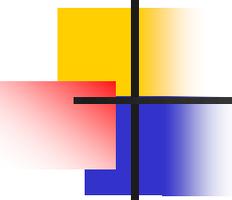


## *Example 11.7 (continued)*

*The physical layer must wait until this event is completed and the data link layer goes back to its sleeping state. We have shown a vertical line to indicate the delay. It is the same story with ACK 3; but when ACK 3 arrives, the sender is busy responding to ACK 2. It happens again when ACK 4 arrives. Note that before the second timer expires, all outstanding frames have been sent and the timer is stopped.*

**Figure 11.17** *Flow diagram for Example 11.7*



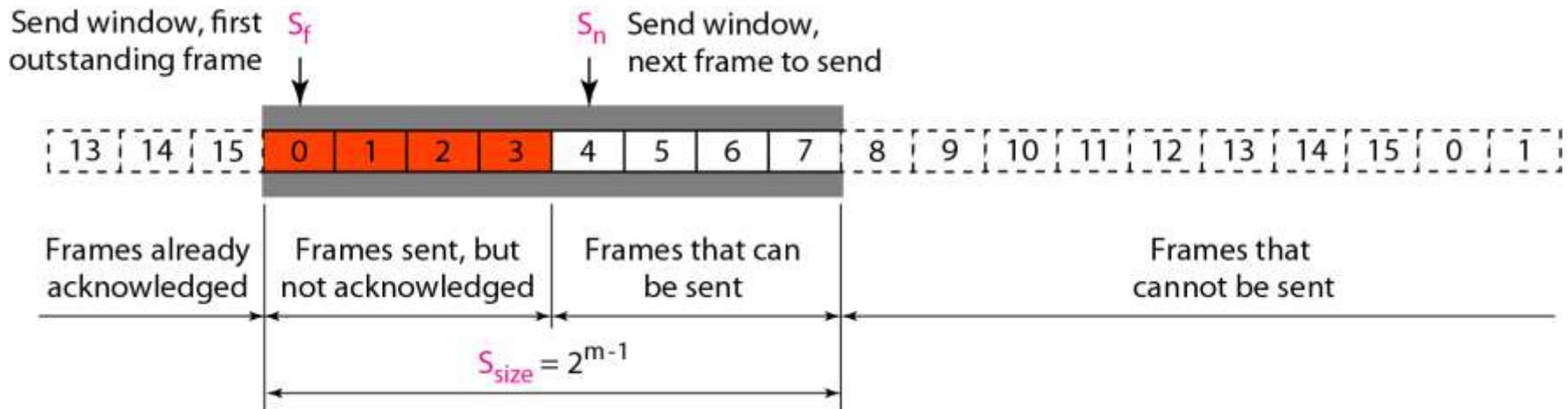


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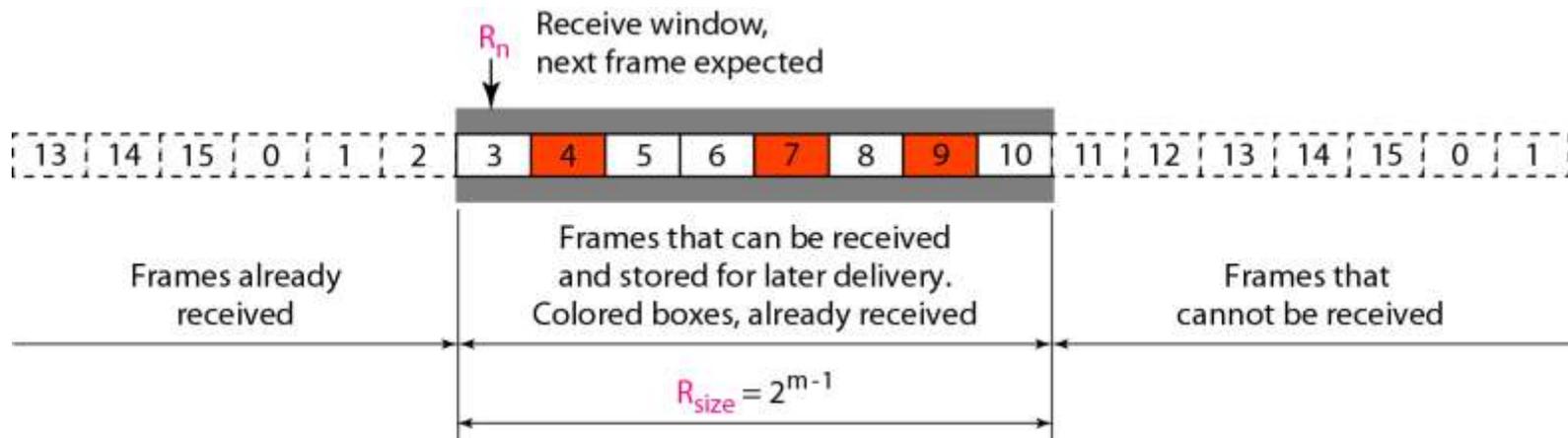
*Note*

**Stop-and-Wait ARQ is a special case of Go-Back-N ARQ in which the size of the send window is 1.**

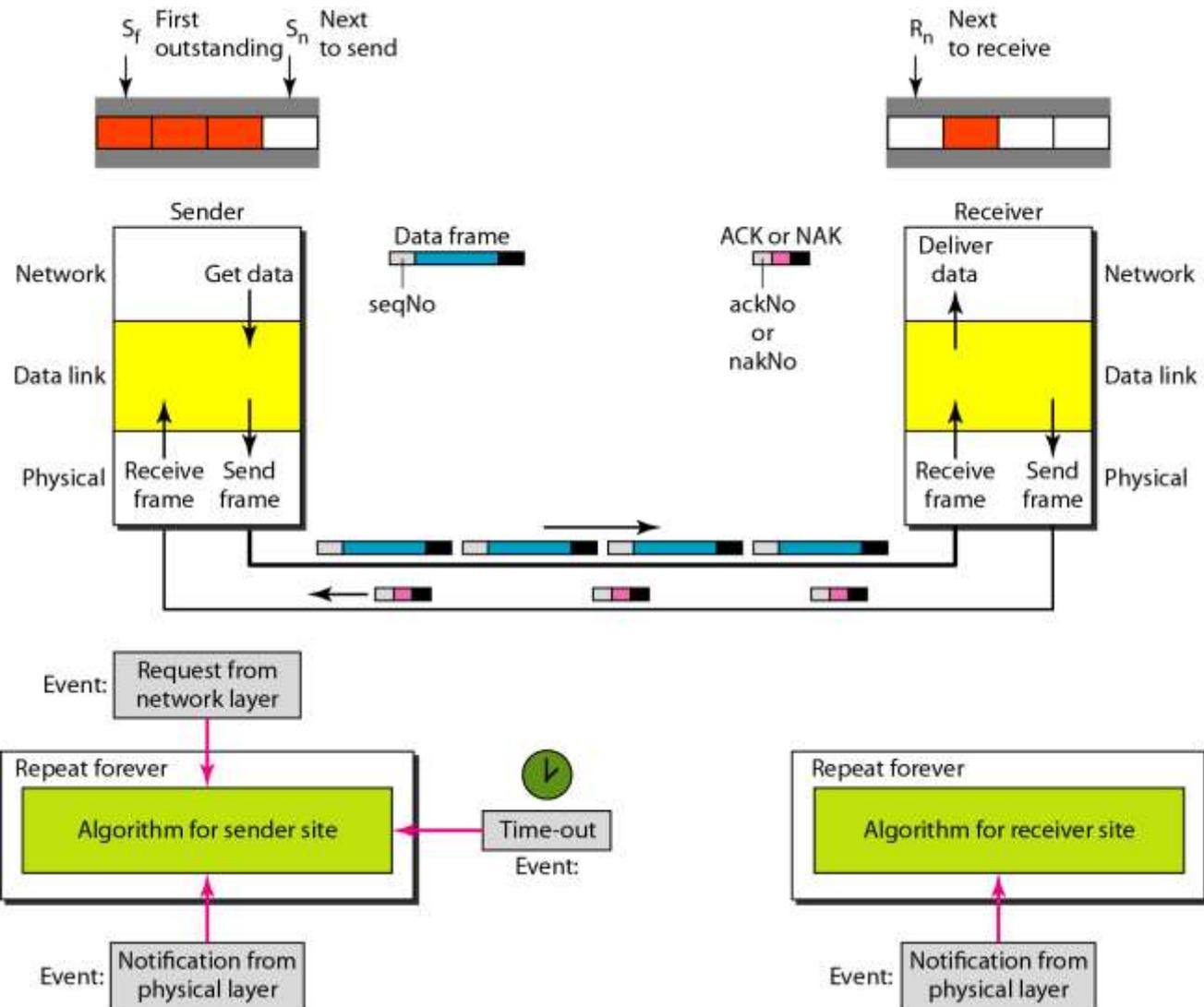
**Figure 11.18** *Send window for Selective Repeat ARQ*



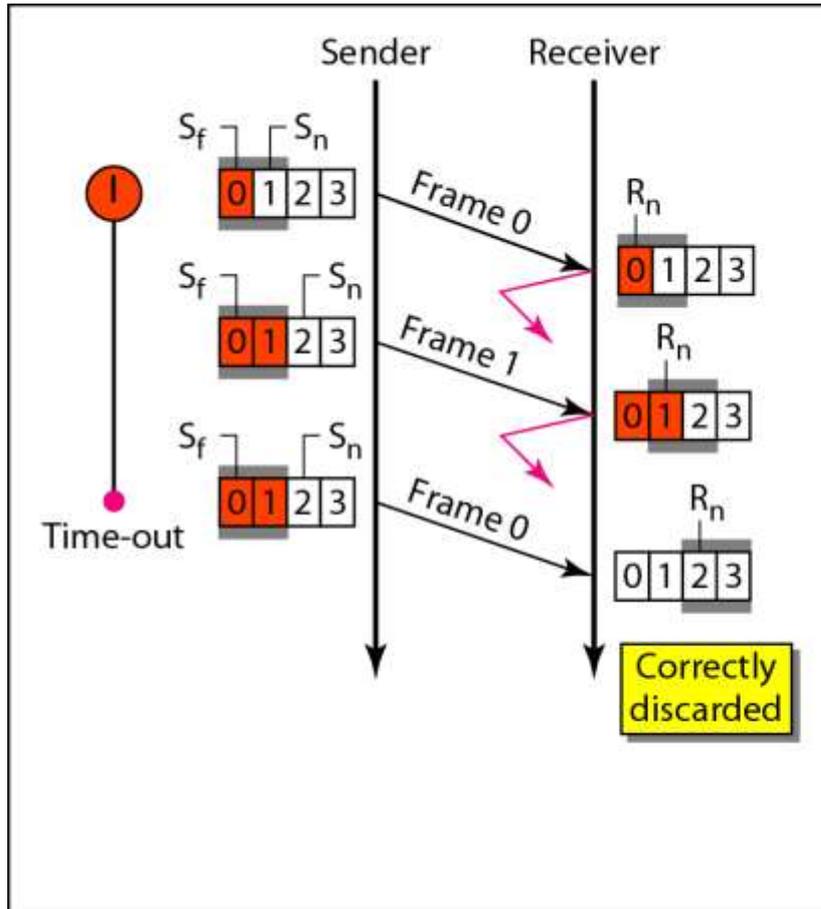
**Figure 11.19** *Receive window for Selective Repeat ARQ*



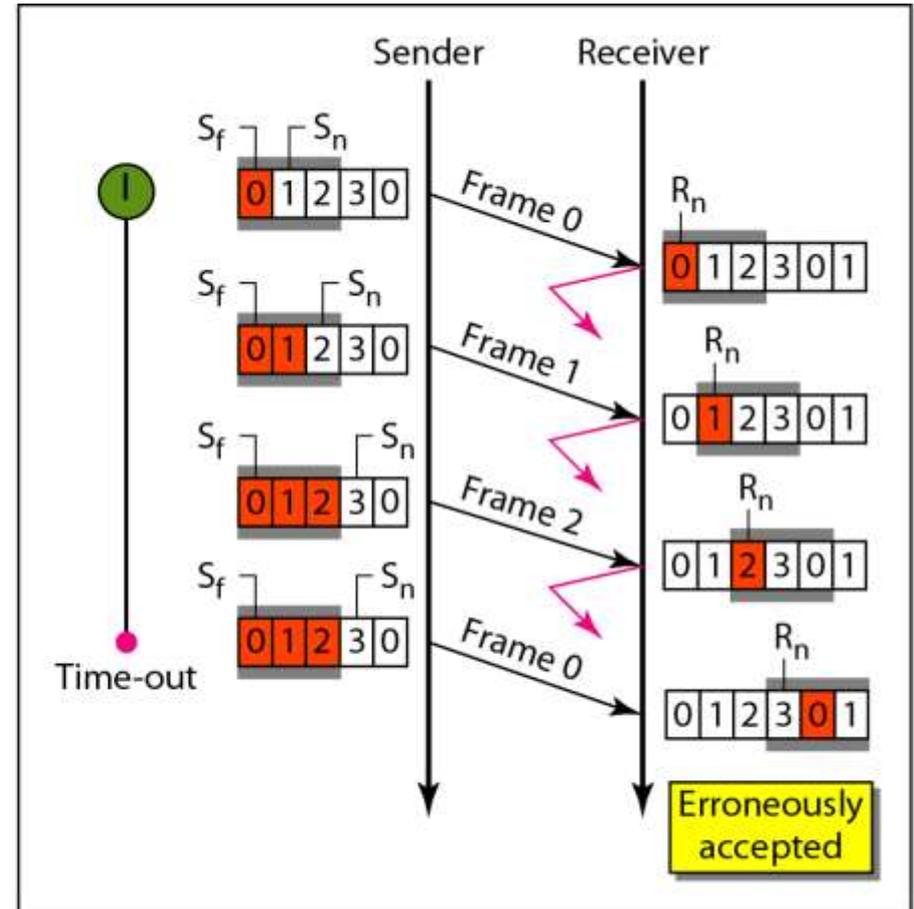
**Figure 11.20** *Design of Selective Repeat ARQ*



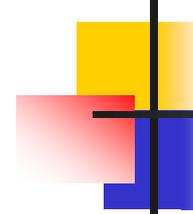
**Figure 11.21** *Selective Repeat ARQ, window size*



a. Window size =  $2^m - 1$



b. Window size  $> 2^m - 1$



*Note*

**In Selective Repeat ARQ, the size of the sender and receiver window must be at most one-half of  $2^m$ .**

## Algorithm 11.9 *Sender-site Selective Repeat algorithm*

```
1  Sw = 2m-1 ;
2  Sf = 0;
3  Sn = 0;
4
5  while (true)                                //Repeat forever
6  {
7      WaitForEvent();
8      if(Event(RequestToSend))                //There is a packet to send
9      {
10         if(Sn-Sf >= Sw)                    //If window is full
11             Sleep();
12         GetData();
13         MakeFrame(Sn);
14         StoreFrame(Sn);
15         SendFrame(Sn);
16         Sn = Sn + 1;
17         StartTimer(Sn);
18     }
19
```

***(continued)***

## Algorithm 11.9 *Sender-site Selective Repeat algorithm*

*(continued)*

```
20  if(Event(ArrivalNotification)) //ACK arrives
21  {
22      Receive(frame);           //Receive ACK or NAK
23      if(corrupted(frame))
24          Sleep();
25      if (FrameType == NAK)
26          if (nakNo between  $S_f$  and  $S_n$ )
27          {
28              resend(nakNo);
29              StartTimer(nakNo);
30          }
31      if (FrameType == ACK)
32          if (ackNo between  $S_f$  and  $S_n$ )
33          {
34              while( $s_f < \text{ackNo}$ )
35              {
36                  Purge( $s_f$ );
37                  StopTimer( $s_f$ );
38                   $S_f = S_f + 1$ ;
39              }
40          }
41  }
```

*(continued)*

## Algorithm 11.9 *Sender-site Selective Repeat algorithm*

*(continued)*

```
42
43  if(Event(Timeout(t)))           //The timer expires
44  {
45    StartTimer(t);
46    SendFrame(t);
47  }
48 }
```

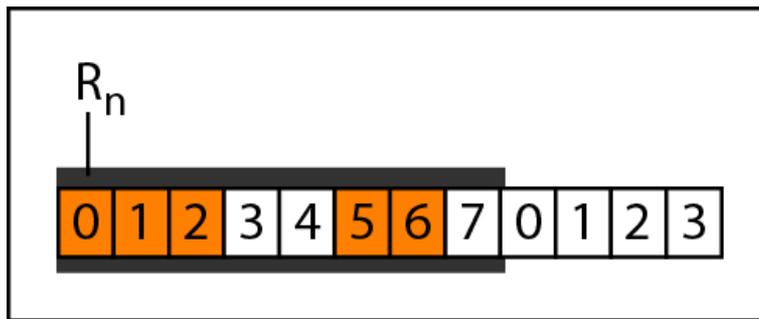
## Algorithm 11.10 Receiver-site Selective Repeat algorithm

```
1  Rn = 0;
2  NakSent = false;
3  AckNeeded = false;
4  Repeat(for all slots)
5      Marked(slot) = false;
6
7  while (true)                                //Repeat forever
8  {
9      WaitForEvent();
10
11     if(Event(ArrivalNotification))           //Data frame arrives
12     {
13         Receive(Frame);
14         if(corrupted(Frame)&& (NOT NakSent))
15         {
16             SendNAK(Rn);
17             NakSent = true;
18             Sleep();
19         }
20         if(seqNo <> Rn)&& (NOT NakSent)
21         {
22             SendNAK(Rn);
```

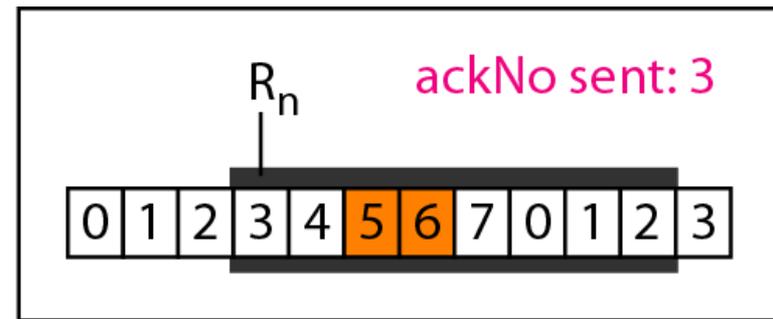
## Algorithm 11.10 Receiver-site Selective Repeat algorithm

```
23     NakSent = true;
24     if ((seqNo in window)&&(!Marked(seqNo)))
25     {
26         StoreFrame(seqNo)
27         Marked(seqNo)= true;
28         while(Marked(Rn))
29         {
30             DeliverData(Rn);
31             Purge(Rn);
32             Rn = Rn + 1;
33             AckNeeded = true;
34         }
35         if(AckNeeded);
36         {
37             SendAck(Rn);
38             AckNeeded = false;
39             NakSent = false;
40         }
41     }
42 }
43 }
44 }
```

## Figure 11.22 *Delivery of data in Selective Repeat ARQ*



a. Before delivery



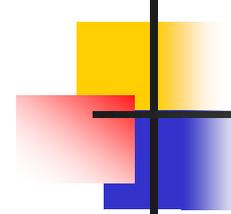
b. After delivery

## Example 11.8

*This example is similar to Example 11.3 in which frame 1 is lost. We show how Selective Repeat behaves in this case. Figure 11.23 shows the situation. One main difference is the number of timers. Here, each frame sent or resent needs a timer, which means that the timers need to be numbered (0, 1, 2, and 3). The timer for frame 0 starts at the first request, but stops when the ACK for this frame arrives. The timer for frame 1 starts at the second request, restarts when a NAK arrives, and finally stops when the last ACK arrives. The other two timers start when the corresponding frames are sent and stop at the last arrival event.*

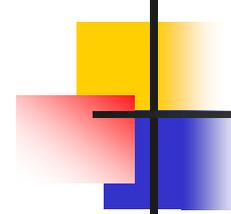
## *Example 11.8 (continued)*

*At the receiver site we need to distinguish between the acceptance of a frame and its delivery to the network layer. At the second arrival, frame 2 arrives and is stored and marked, but it cannot be delivered because frame 1 is missing. At the next arrival, frame 3 arrives and is marked and stored, but still none of the frames can be delivered. Only at the last arrival, when finally a copy of frame 1 arrives, can frames 1, 2, and 3 be delivered to the network layer. There are two conditions for the delivery of frames to the network layer: First, a set of consecutive frames must have arrived. Second, the set starts from the beginning of the window.*



## *Example 11.8 (continued)*

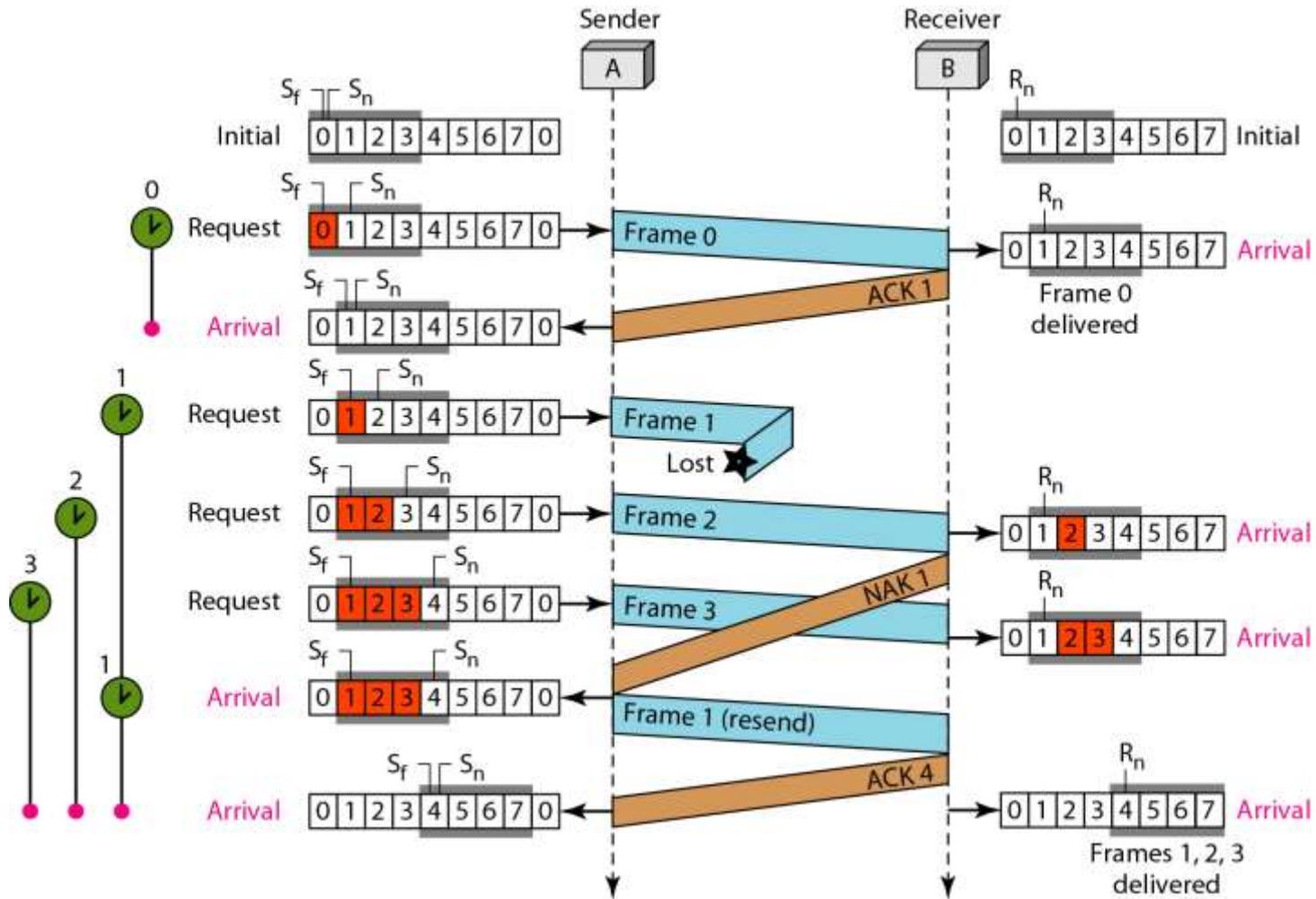
*Another important point is that a NAK is sent after the second arrival, but not after the third, although both situations look the same. The reason is that the protocol does not want to crowd the network with unnecessary NAKs and unnecessary resent frames. The second NAK would still be NAK1 to inform the sender to resend frame 1 again; this has already been done. The first NAK sent is remembered (using the nakSent variable) and is not sent again until the frame slides. A NAK is sent once for each window position and defines the first slot in the window.*



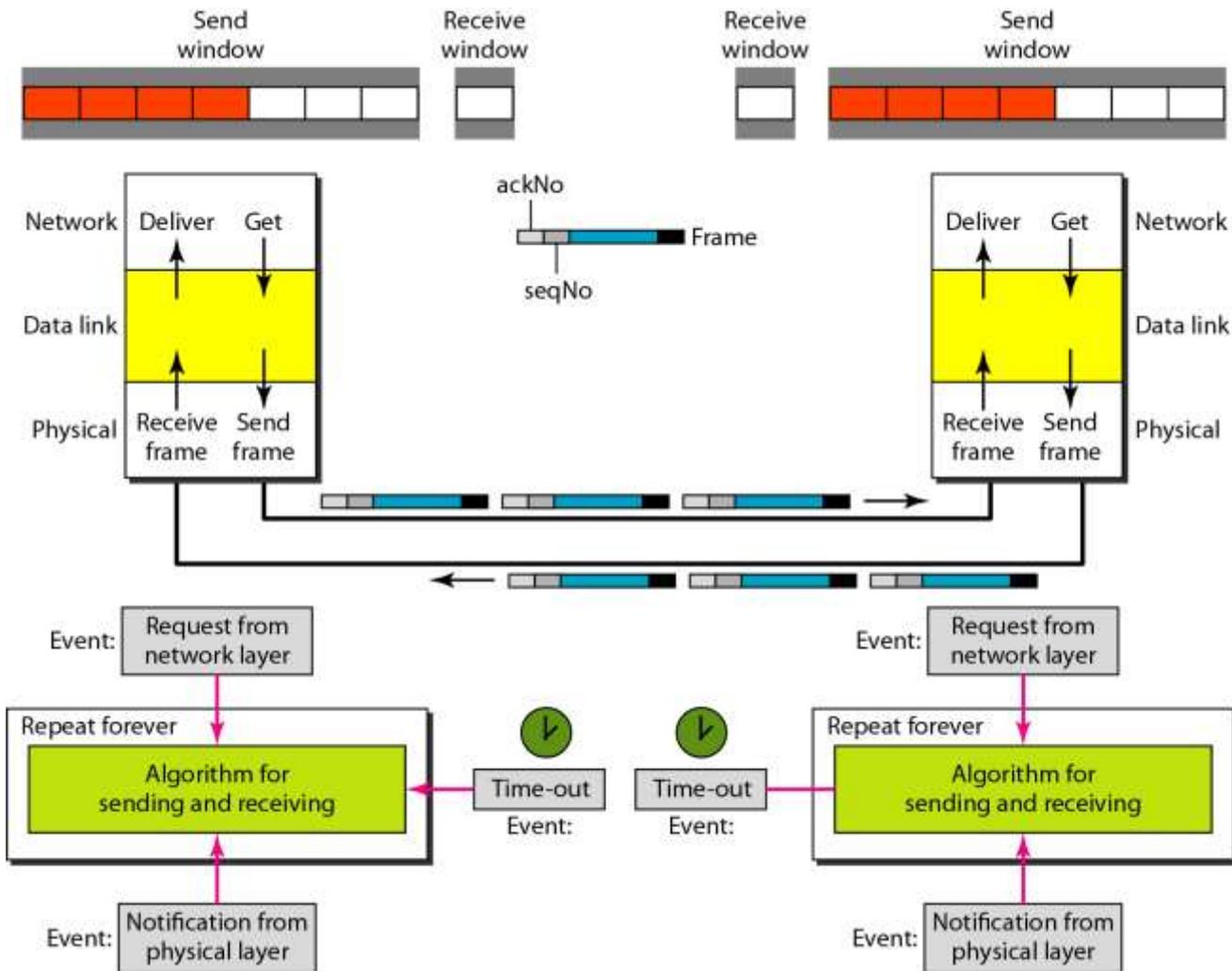
## *Example 11.8 (continued)*

*The next point is about the ACKs. Notice that only two ACKs are sent here. The first one acknowledges only the first frame; the second one acknowledges three frames. In Selective Repeat, ACKs are sent when data are delivered to the network layer. If the data belonging to  $n$  frames are delivered in one shot, only one ACK is sent for all of them.*

**Figure 11.23** *Flow diagram for Example 11.8*



**Figure 11.24** *Design of piggybacking in Go-Back-N ARQ*



## 11-6 HDLC

*High-level Data Link Control (HDLC) is a bit-oriented protocol for communication over point-to-point and multipoint links. It implements the ARQ mechanisms we discussed in this chapter.*

*Topics discussed in this section:*

**Configurations and Transfer Modes**

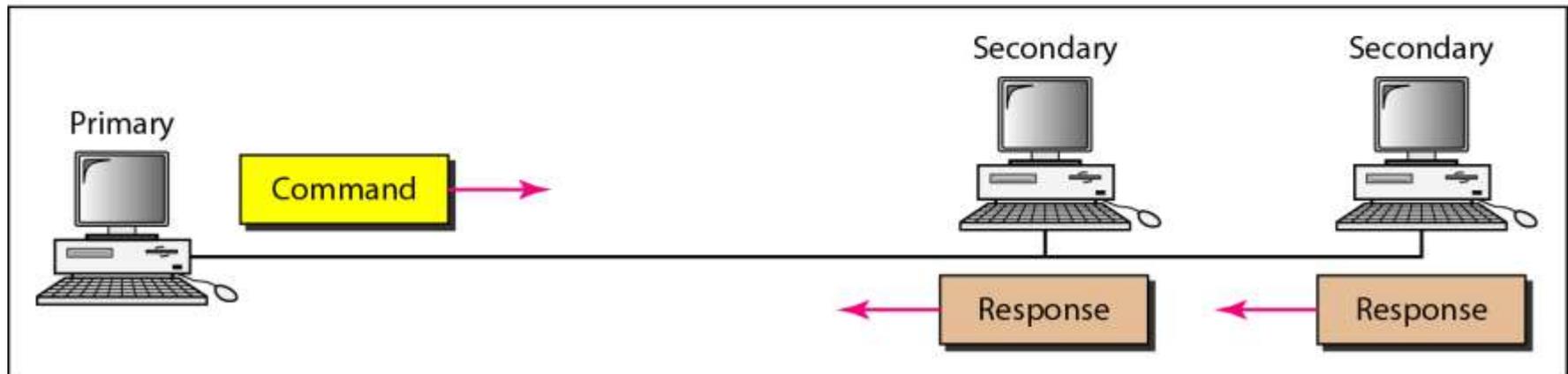
**Frames**

**Control Field**

**Figure 11.25** *Normal response mode*



a. Point-to-point

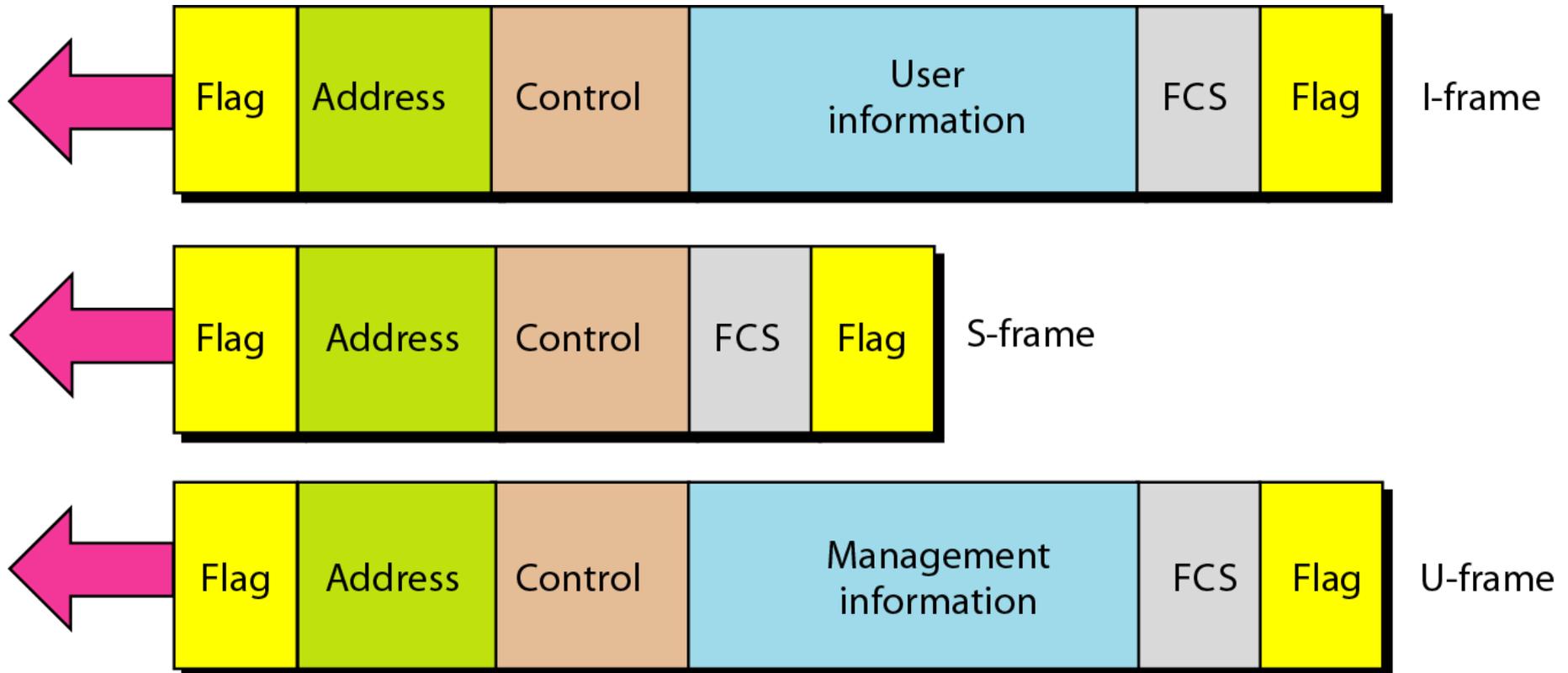


b. Multipoint

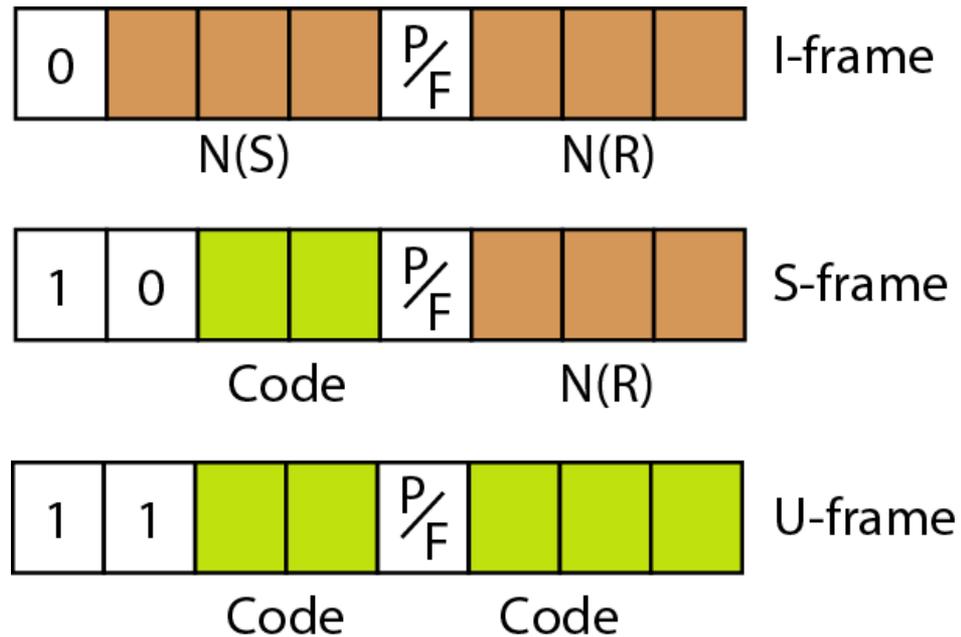
**Figure 11.26** *Asynchronous balanced mode*



**Figure 11.27** *HDLC frames*

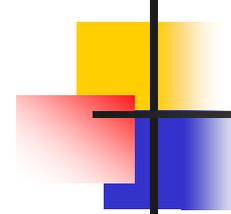


**Figure 11.28** *Control field format for the different frame types*



**Table 11.1** *U-frame control command and response*

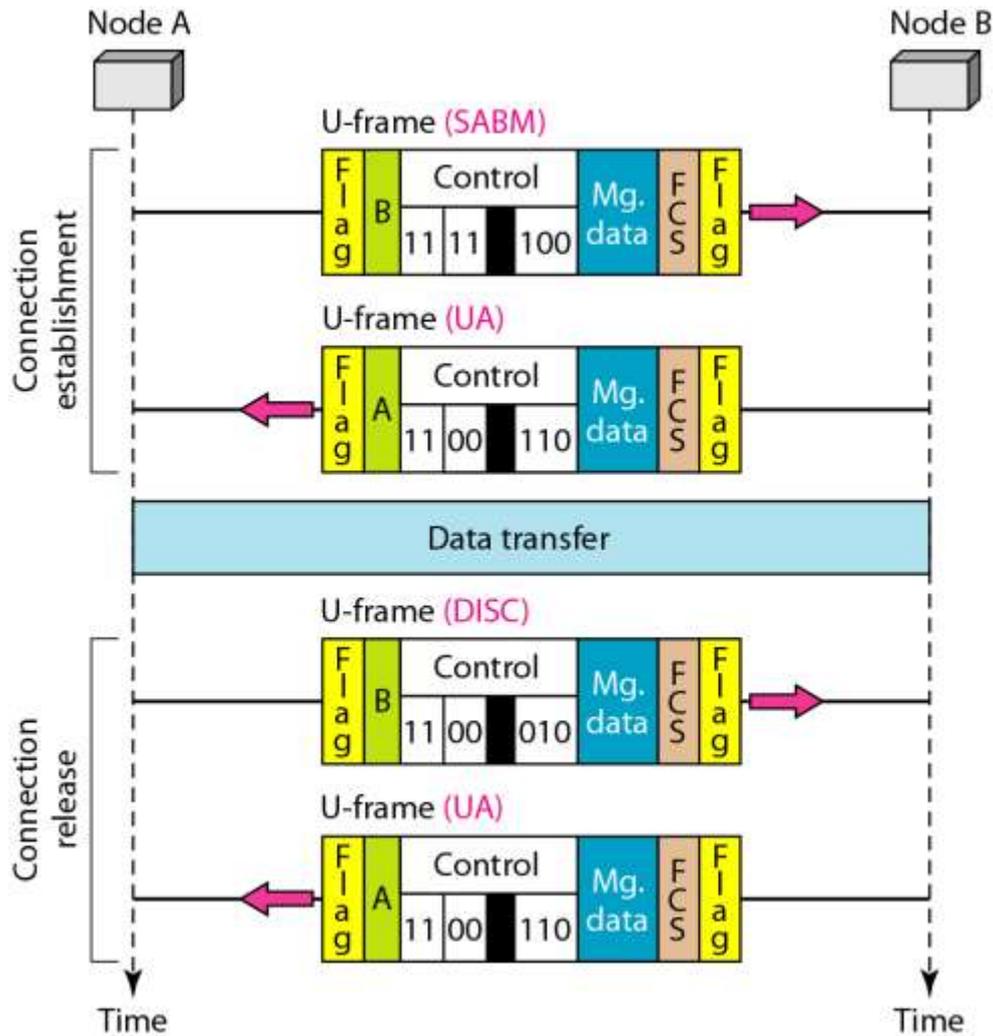
<i>Code</i>	<i>Command</i>	<i>Response</i>	<i>Meaning</i>
<b>00 001</b>	SNRM		Set normal response mode
<b>11 011</b>	SNRME		Set normal response mode, extended
<b>11 100</b>	SABM	<b>DM</b>	Set asynchronous balanced mode or <b>disconnect mode</b>
<b>11 110</b>	SABME		Set asynchronous balanced mode, extended
<b>00 000</b>	UI	<b>UI</b>	Unnumbered information
<b>00 110</b>		<b>UA</b>	<b>Unnumbered acknowledgment</b>
<b>00 010</b>	DISC	<b>RD</b>	Disconnect or <b>request disconnect</b>
<b>10 000</b>	SIM	<b>RIM</b>	Set initialization mode or <b>request information mode</b>
<b>00 100</b>	UP		Unnumbered poll
<b>11 001</b>	RSET		Reset
<b>11 101</b>	XID	<b>XID</b>	Exchange ID
<b>10 001</b>	FRMR	<b>FRMR</b>	Frame reject



## *Example 11.9*

*Figure 11.29 shows how **U-frames** can be used for connection establishment and connection release. Node A asks for a connection with a set asynchronous balanced mode (SABM) frame; node B gives a positive response with an unnumbered acknowledgment (UA) frame. After these two exchanges, data can be transferred between the two nodes (not shown in the figure). After data transfer, node A sends a DISC (disconnect) frame to release the connection; it is confirmed by node B responding with a UA (unnumbered acknowledgment).*

**Figure 11.29** *Example of connection and disconnection*



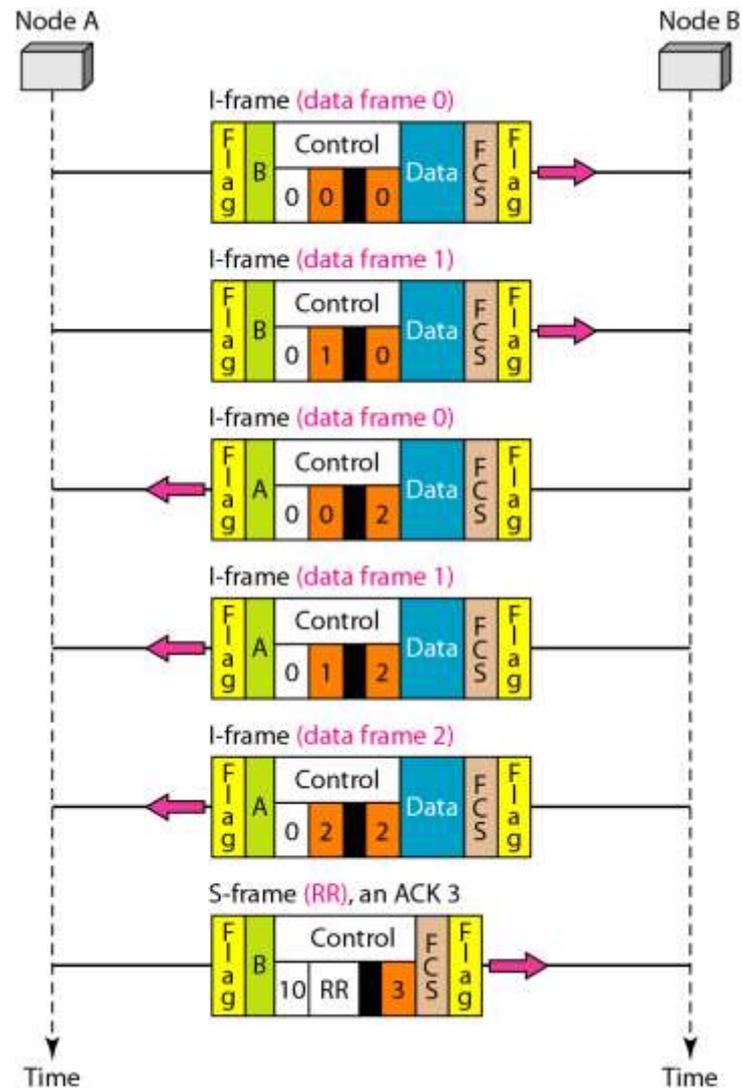
## *Example 11.10*

*Figure 11.30 shows an exchange using piggybacking. Node A begins the exchange of information with an I-frame numbered 0 followed by another I-frame numbered 1. Node B piggybacks its acknowledgment of both frames onto an I-frame of its own. Node B's first I-frame is also numbered 0 [N(S) field] and contains a 2 in its N(R) field, acknowledging the receipt of A's frames 1 and 0 and indicating that it expects frame 2 to arrive next. Node B transmits its second and third I-frames (numbered 1 and 2) before accepting further frames from node A.*

## *Example 11.10 (continued)*

*Its  $N(R)$  information, therefore, has not changed:  $B$  frames 1 and 2 indicate that node  $B$  is still expecting  $A$ 's frame 2 to arrive next. Node  $A$  has sent all its data. Therefore, it cannot piggyback an acknowledgment onto an  $I$ -frame and sends an  $S$ -frame instead. The  $RR$  code indicates that  $A$  is still ready to receive. The number 3 in the  $N(R)$  field tells  $B$  that frames 0, 1, and 2 have all been accepted and that  $A$  is now expecting frame number 3.*

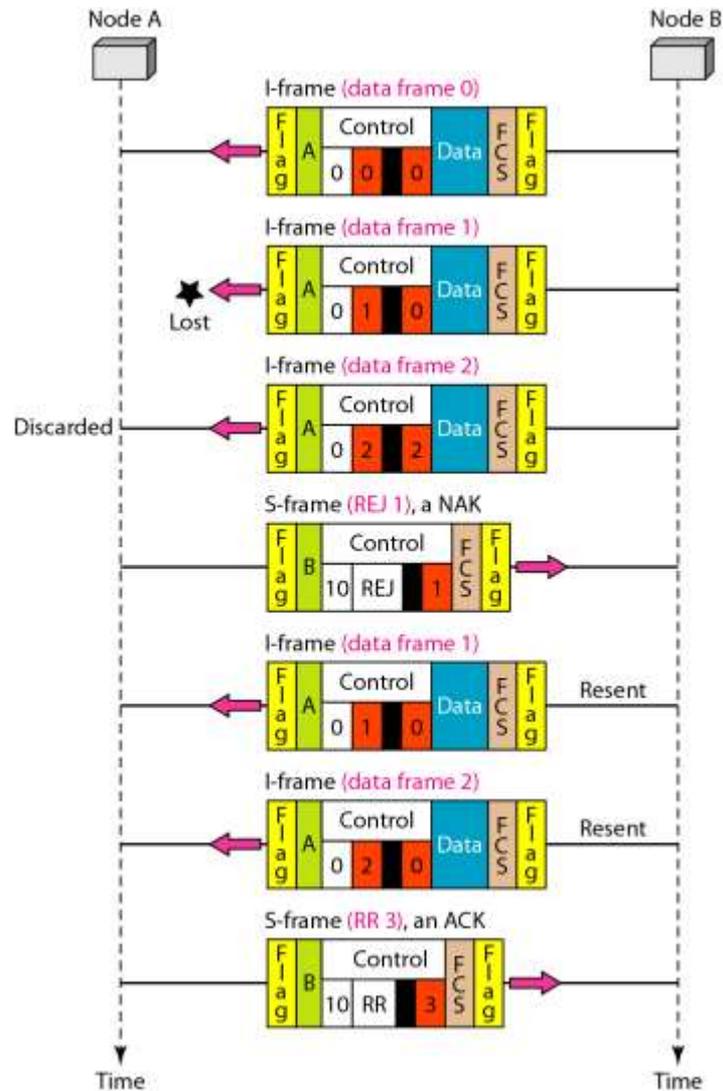
**Figure 11.30** *Example of piggybacking without error*



## *Example 11.11*

*Figure 11.31 shows an exchange in which a frame is lost. Node B sends three data frames (0, 1, and 2), but frame 1 is lost. When node A receives frame 2, it discards it and sends a REJ frame for frame 1. Note that the protocol being used is Go-Back-N with the special use of an REJ frame as a NAK frame. The NAK frame does two things here: It confirms the receipt of frame 0 and declares that frame 1 and any following frames must be resent. Node B, after receiving the REJ frame, resends frames 1 and 2. Node A acknowledges the receipt by sending an RR frame (ACK) with acknowledgment number 3.*

**Figure 11.31** *Example of piggybacking with error*



## 11-7 POINT-TO-POINT PROTOCOL

*Although HDLC is a general protocol that can be used for both point-to-point and multipoint configurations, one of the most common protocols for point-to-point access is the **Point-to-Point Protocol (PPP)**. PPP is a **byte-oriented** protocol.*

### *Topics discussed in this section:*

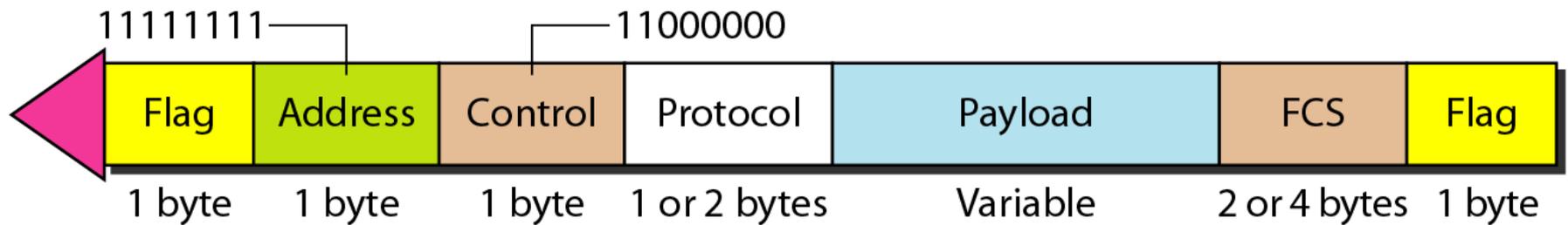
**Framing**

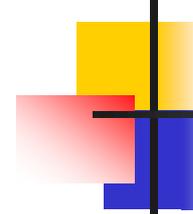
**Transition Phases**

**Multiplexing**

**Multilink PPP**

**Figure 11.32** *PPP frame format*

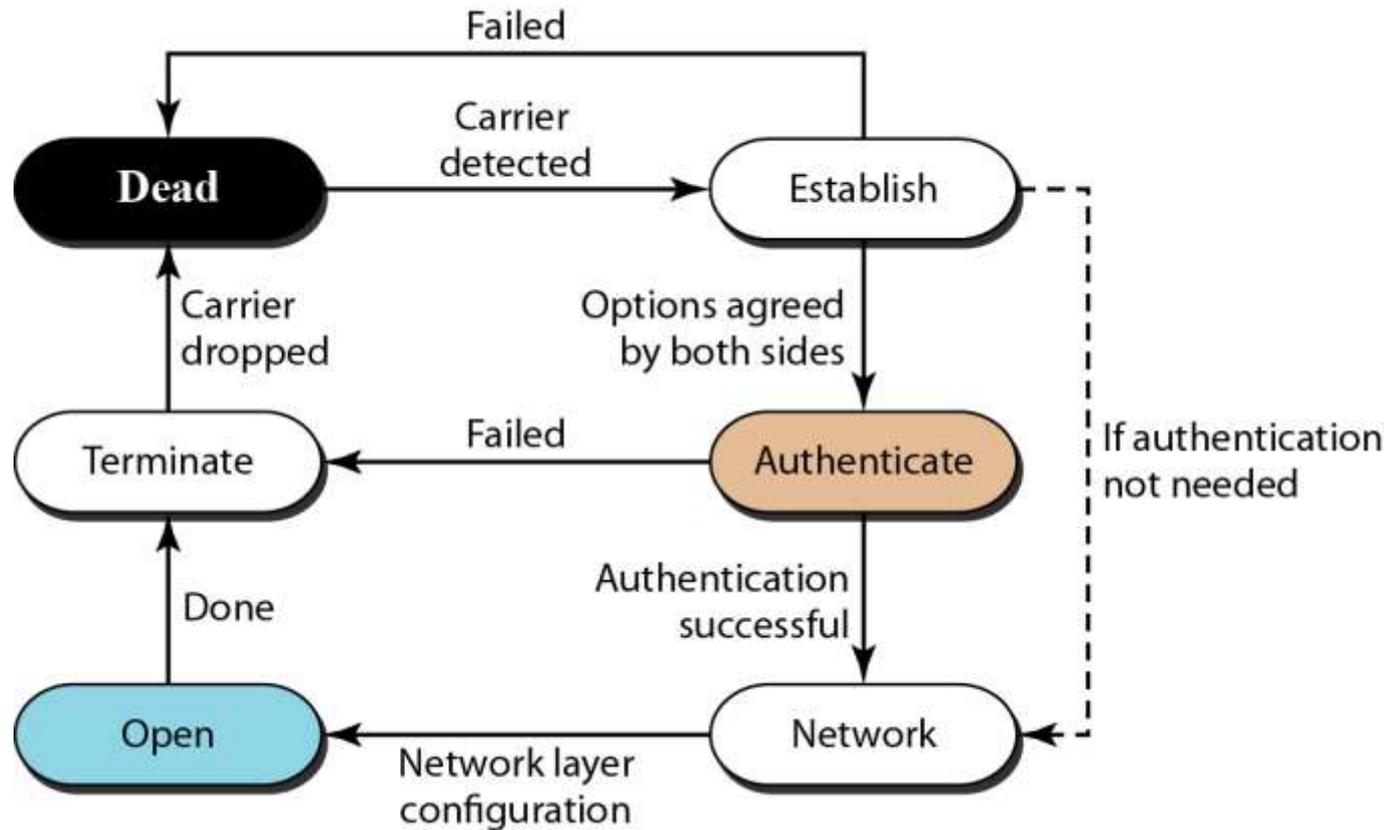




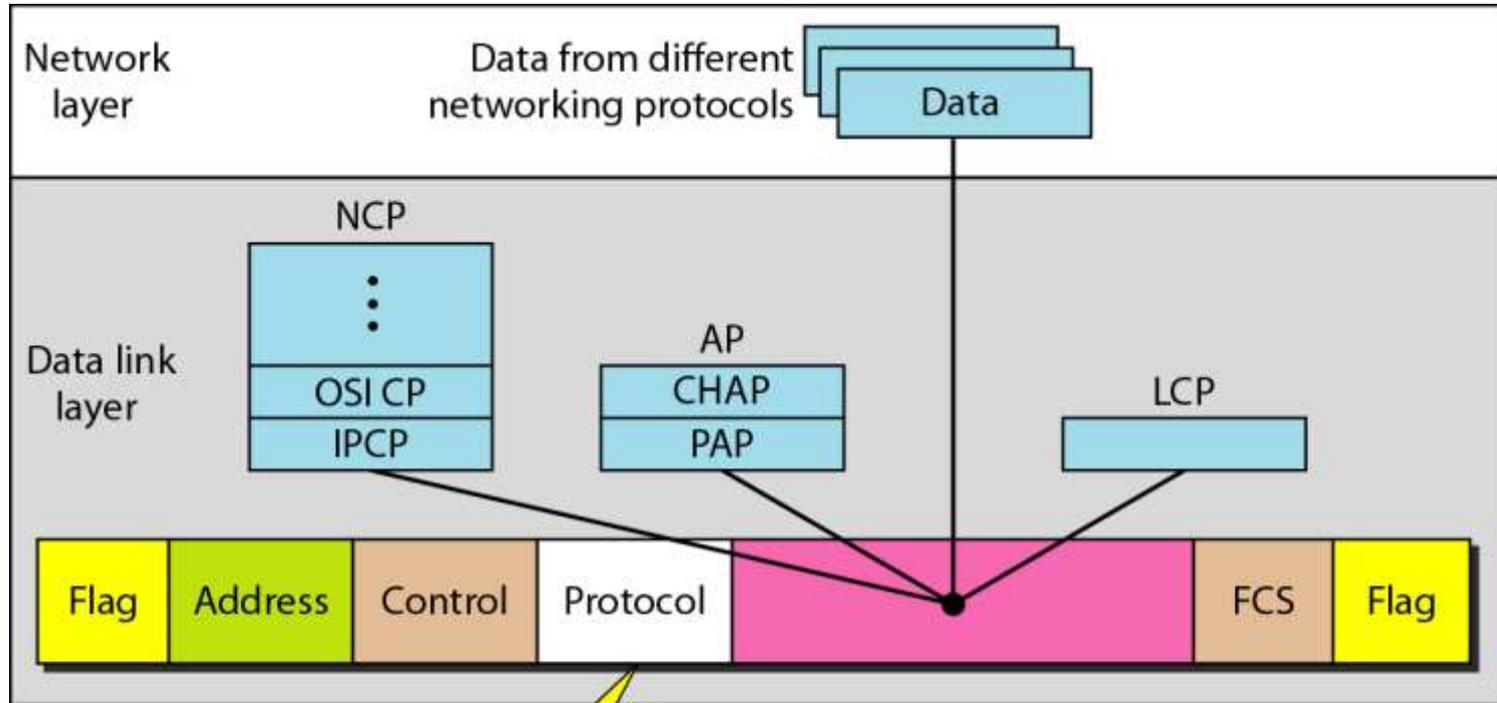
*Note*

**PPP is a byte-oriented protocol using  
byte stuffing with the escape byte  
0111101.**

**Figure 11.33** *Transition phases*



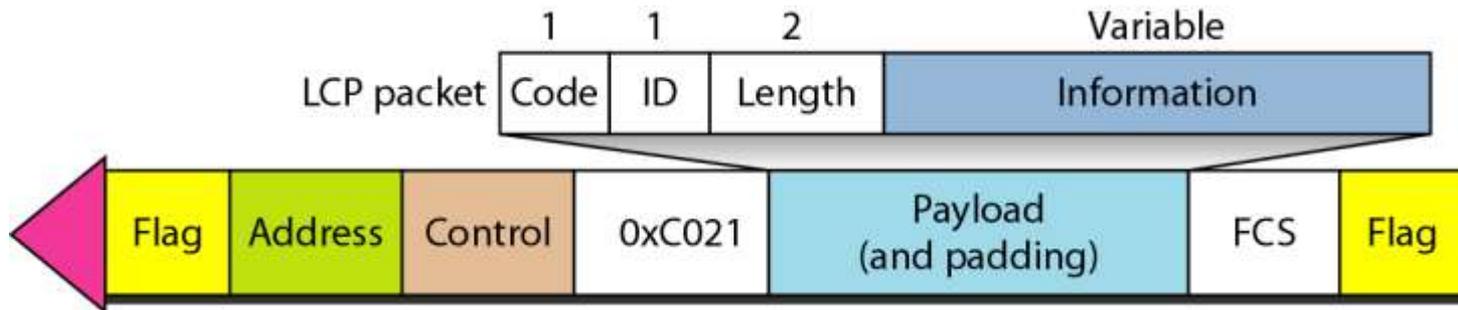
**Figure 11.34** *Multiplexing in PPP*



LCP: 0xC021  
AP: 0xC023 and 0xC223  
NCP: 0x8021 and ....  
Data: 0x0021 and ....

LCP: Link Control Protocol  
AP: Authentication Protocol  
NCP: Network Control Protocol

**Figure 11.35** *LCP packet encapsulated in a frame*



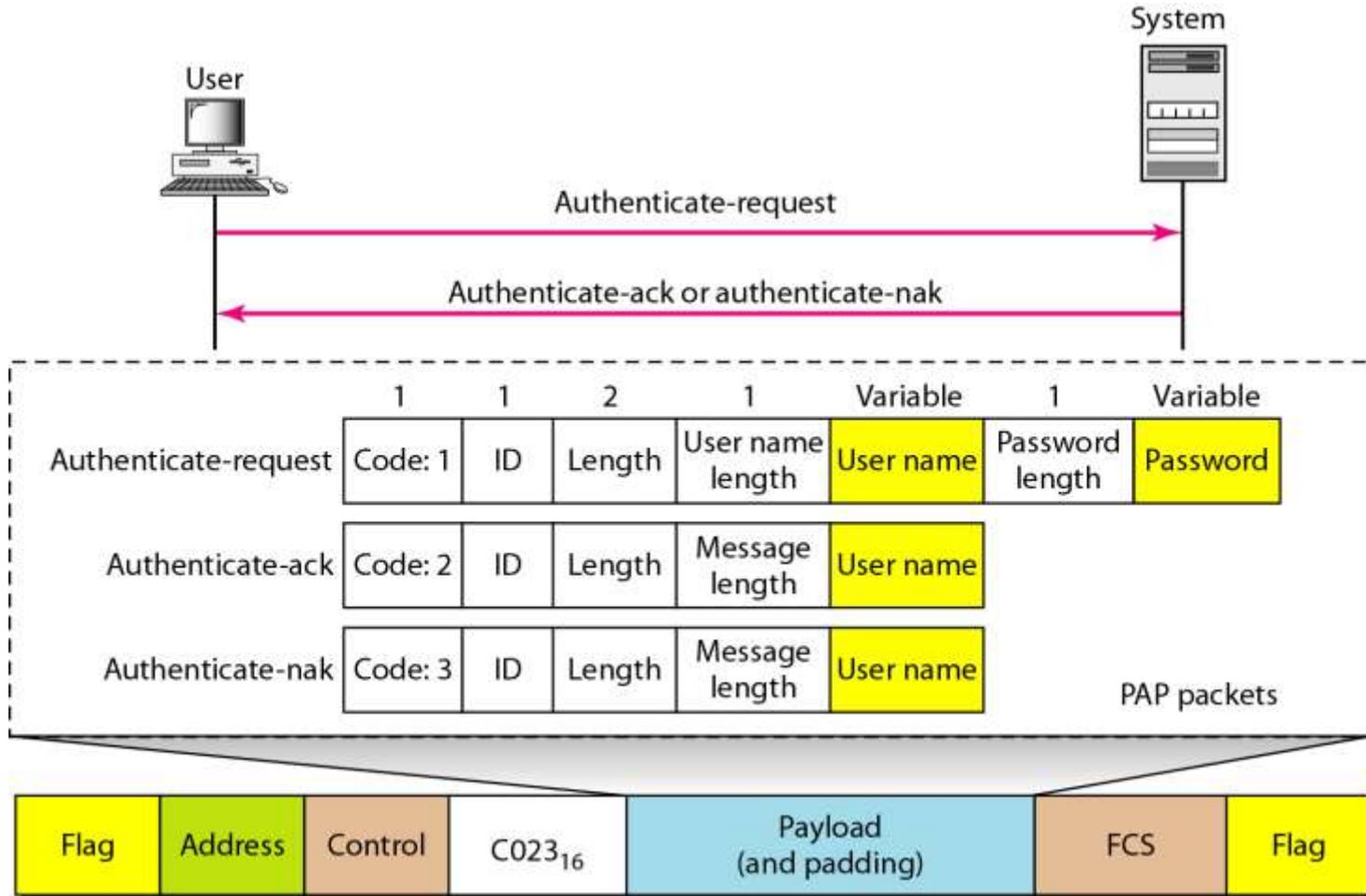
**Table 11.2** *LCP packets*

<i>Code</i>	<i>Packet Type</i>	<i>Description</i>
0x01	Configure-request	Contains the list of proposed options and their values
0x02	Configure-ack	Accepts all options proposed
0x03	Configure-nak	Announces that some options are not acceptable
0x04	Configure-reject	Announces that some options are not recognized
0x05	Terminate-request	Request to shut down the line
0x06	Terminate-ack	Accept the shutdown request
0x07	Code-reject	Announces an unknown code
0x08	Protocol-reject	Announces an unknown protocol
0x09	Echo-request	A type of hello message to check if the other end is alive
0x0A	Echo-reply	The response to the echo-request message
0x0B	Discard-request	A request to discard the packet

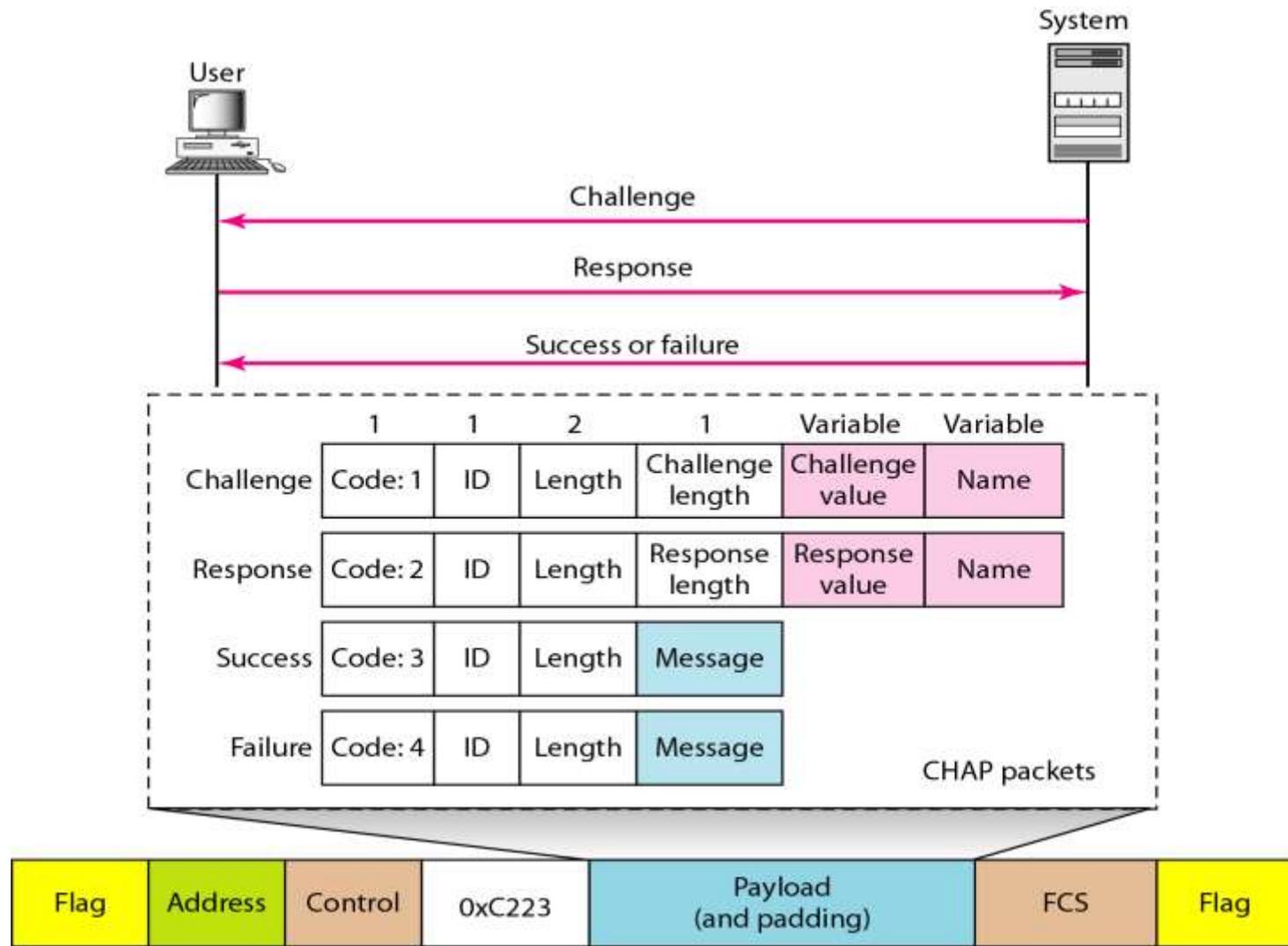
**Table 11.3** *Common options*

<i>Option</i>	<i>Default</i>
Maximum receive unit (payload field size)	1500
Authentication protocol	None
Protocol field compression	Off
Address and control field compression	Off

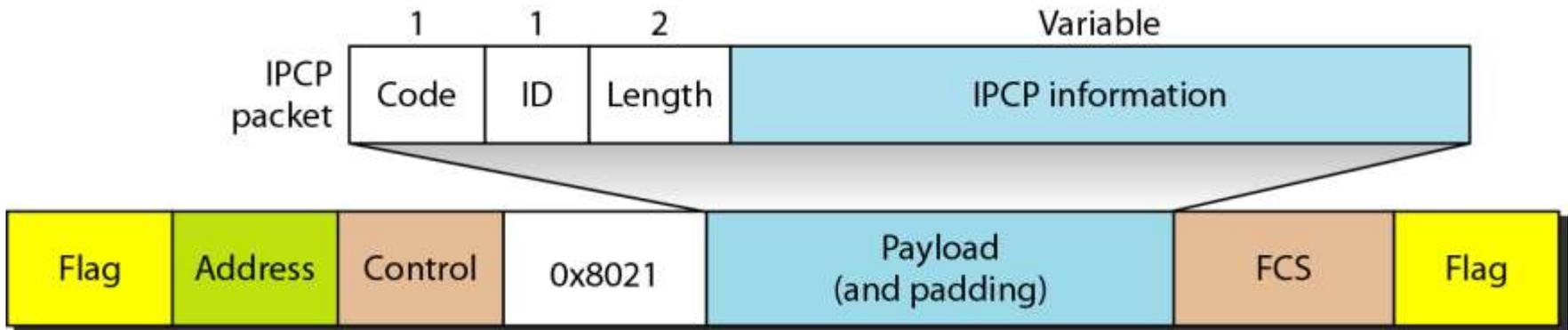
**Figure 11.36** *PAP packets encapsulated in a PPP frame*



**Figure 11.37** CHAP packets encapsulated in a PPP frame



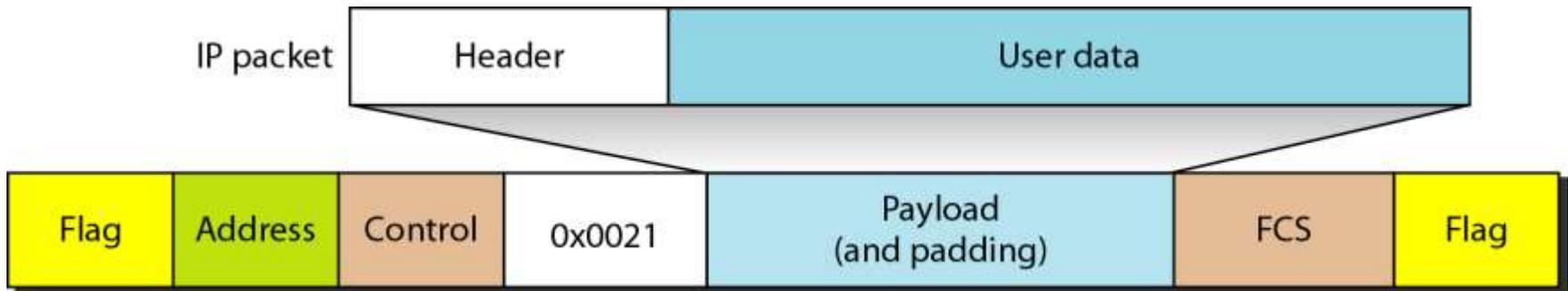
**Figure 11.38** *IPCP packet encapsulated in PPP frame*



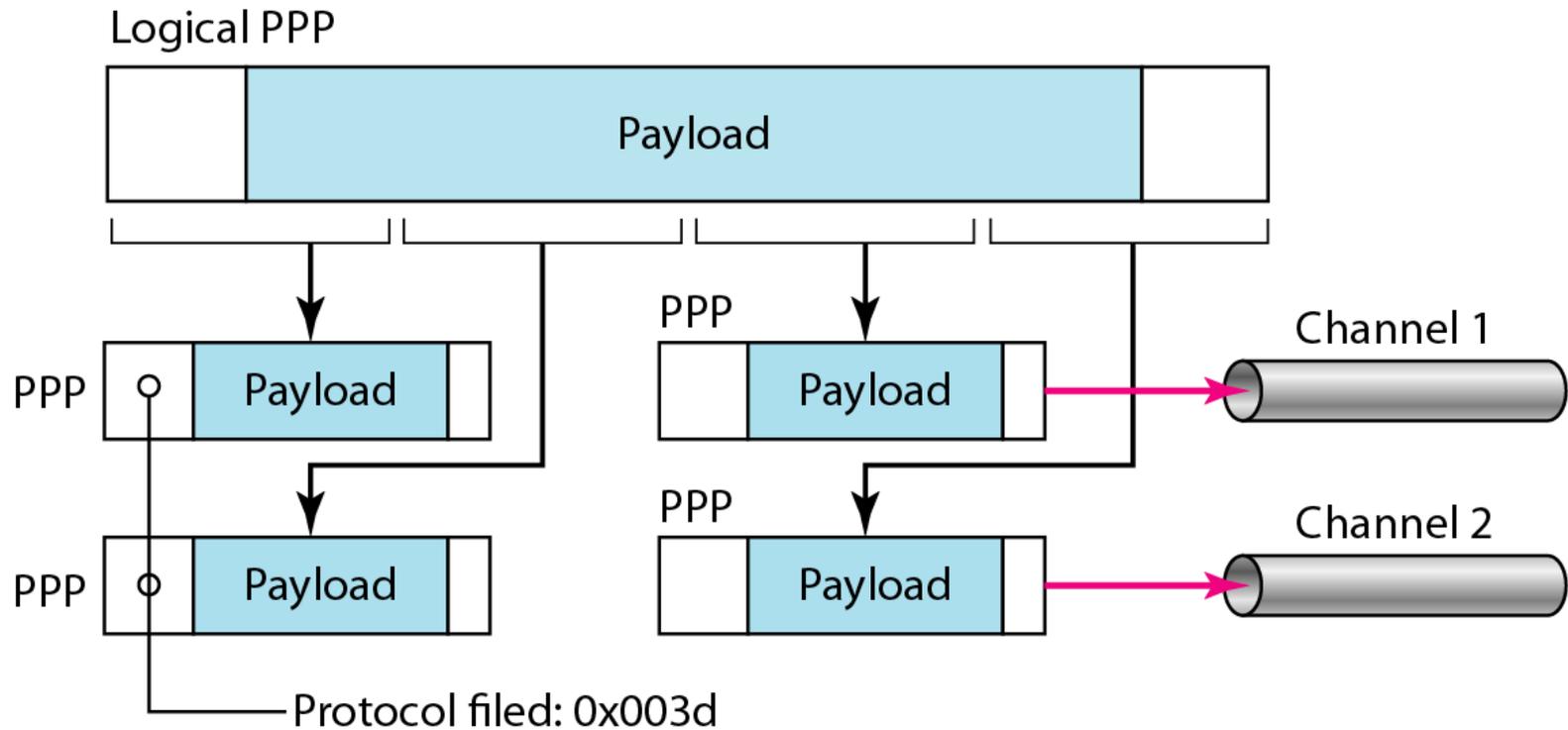
**Table 11.4** *Code value for IPCP packets*

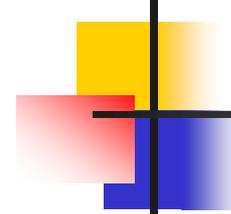
<i>Code</i>	<i>IPCP Packet</i>
0x01	Configure-request
0x02	Configure-ack
0x03	Configure-nak
0x04	Configure-reject
0x05	Terminate-request
0x06	Terminate-ack
0x07	Code-reject

**Figure 11.39** *IP datagram encapsulated in a PPP frame*



**Figure 11.40** *Multilink PPP*

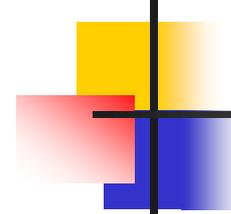




## *Example 11.12*

*Let us go through the phases followed by a network layer packet as it is transmitted through a PPP connection. Figure 11.41 shows the steps. For simplicity, we assume unidirectional movement of data from the user site to the system site (such as sending an e-mail through an ISP).*

*The first two frames show link establishment. We have chosen two options (not shown in the figure): using PAP for authentication and suppressing the address control fields. Frames 3 and 4 are for authentication. Frames 5 and 6 establish the network layer connection using IPCP.*



## *Example 11.12 (continued)*

*The next several frames show that some IP packets are encapsulated in the PPP frame. The system (receiver) may have been running several network layer protocols, but it knows that the incoming data must be delivered to the IP protocol because the NCP protocol used before the data transfer was IPCP.*

*After data transfer, the user then terminates the data link connection, which is acknowledged by the system. Of course the user or the system could have chosen to terminate the network layer IPCP and keep the data link layer running if it wanted to run another NCP protocol.*

Figure 11.41 *An example*

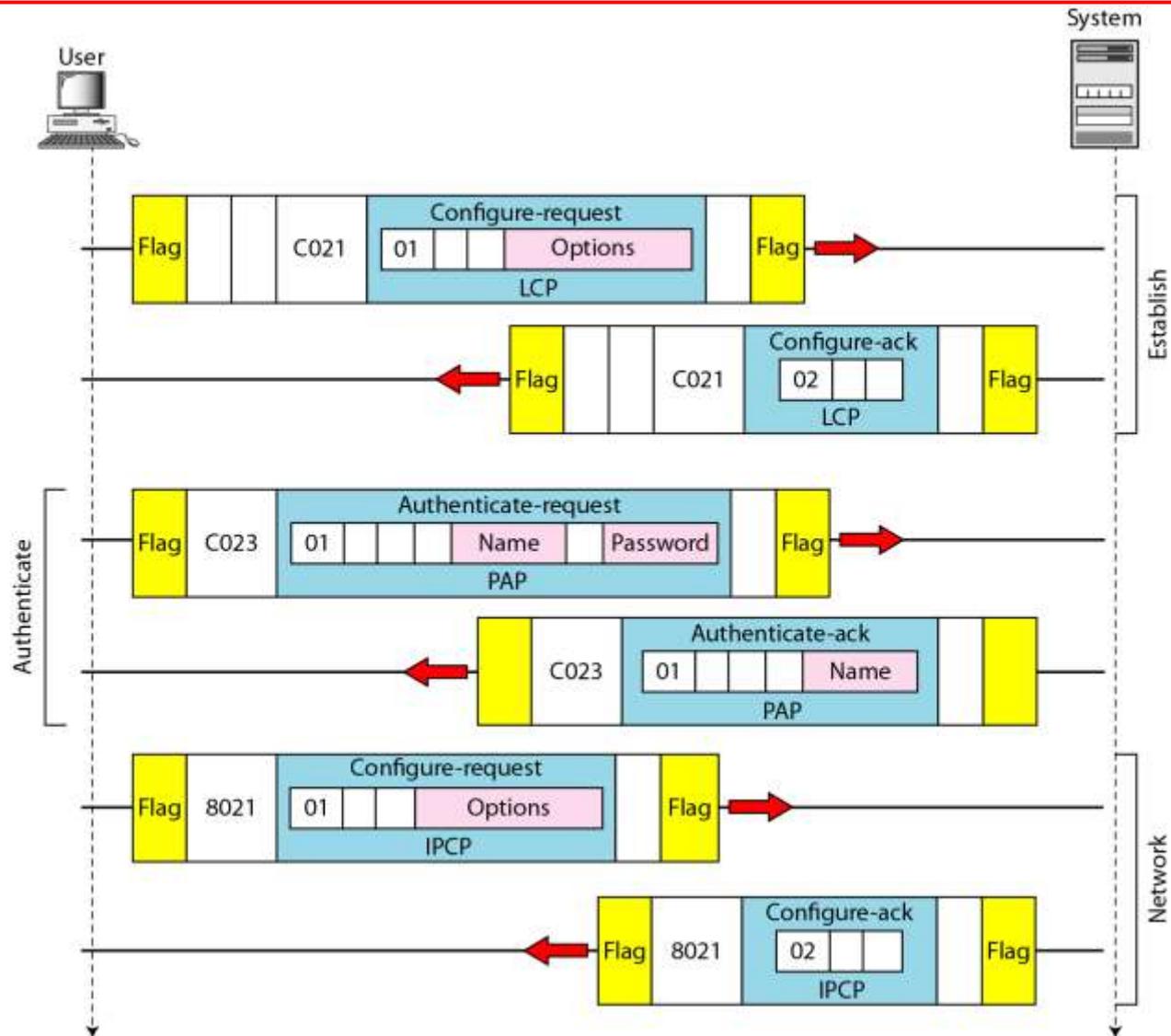
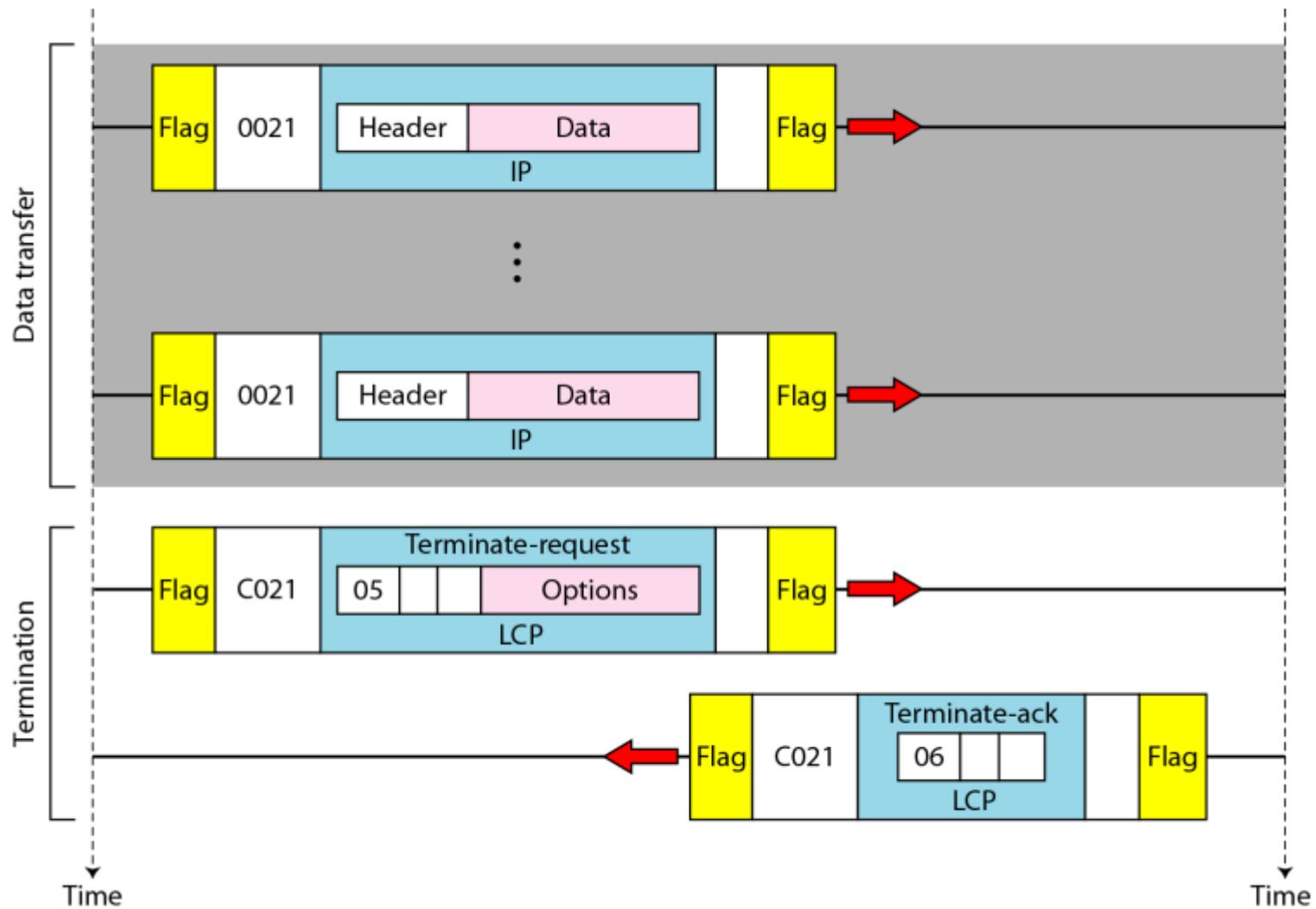


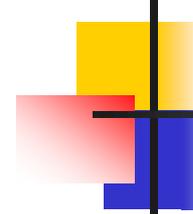
Figure 11.41 *An example (continued)*





# Chapter 10

## Error Detection and Correction



*Note*

**Data can be corrupted  
during transmission.**

**Some applications require that  
errors be detected and corrected.**

# 10-1 INTRODUCTION

*Let us first discuss some issues related, directly or indirectly, to error detection and correction.*

## *Topics discussed in this section:*

**Types of Errors**

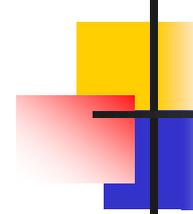
**Redundancy**

**Detection Versus Correction**

**Forward Error Correction Versus Retransmission**

**Coding**

**Modular Arithmetic**



---

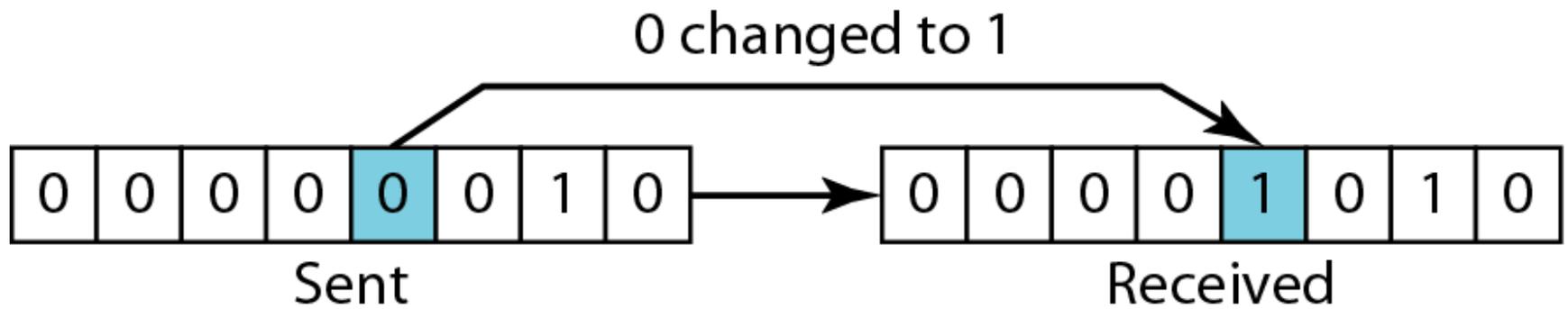
*Note*

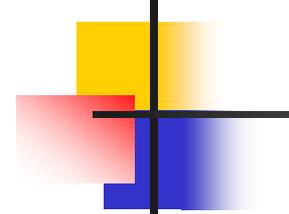
**In a single-bit error, only 1 bit in the data unit has changed.**

---

**Figure 10.1** *Single-bit error*

---

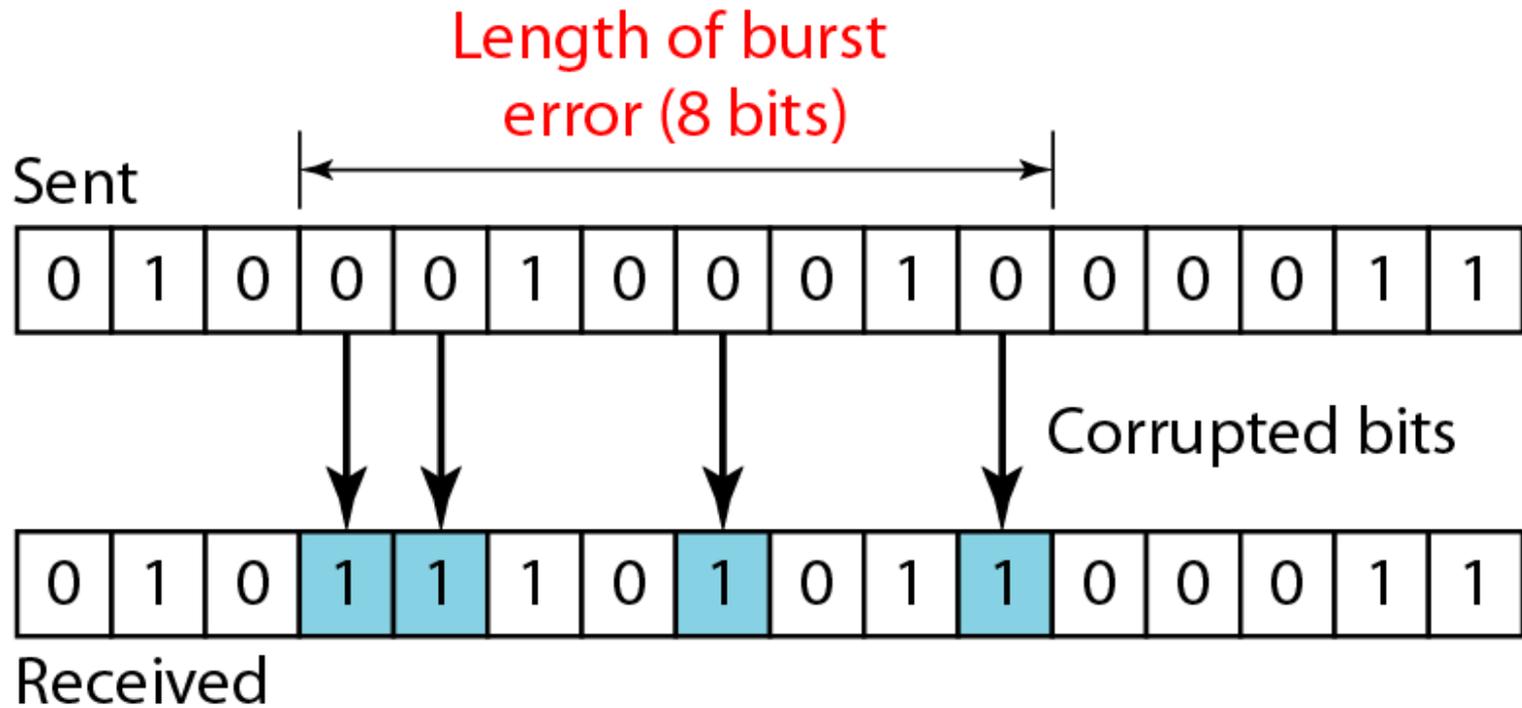


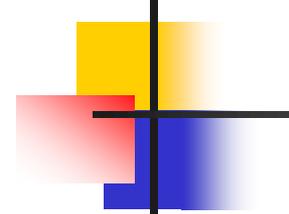


*Note*

**A burst error means that 2 or more bits in the data unit have changed.**

**Figure 10.2** *Burst error of length 8*



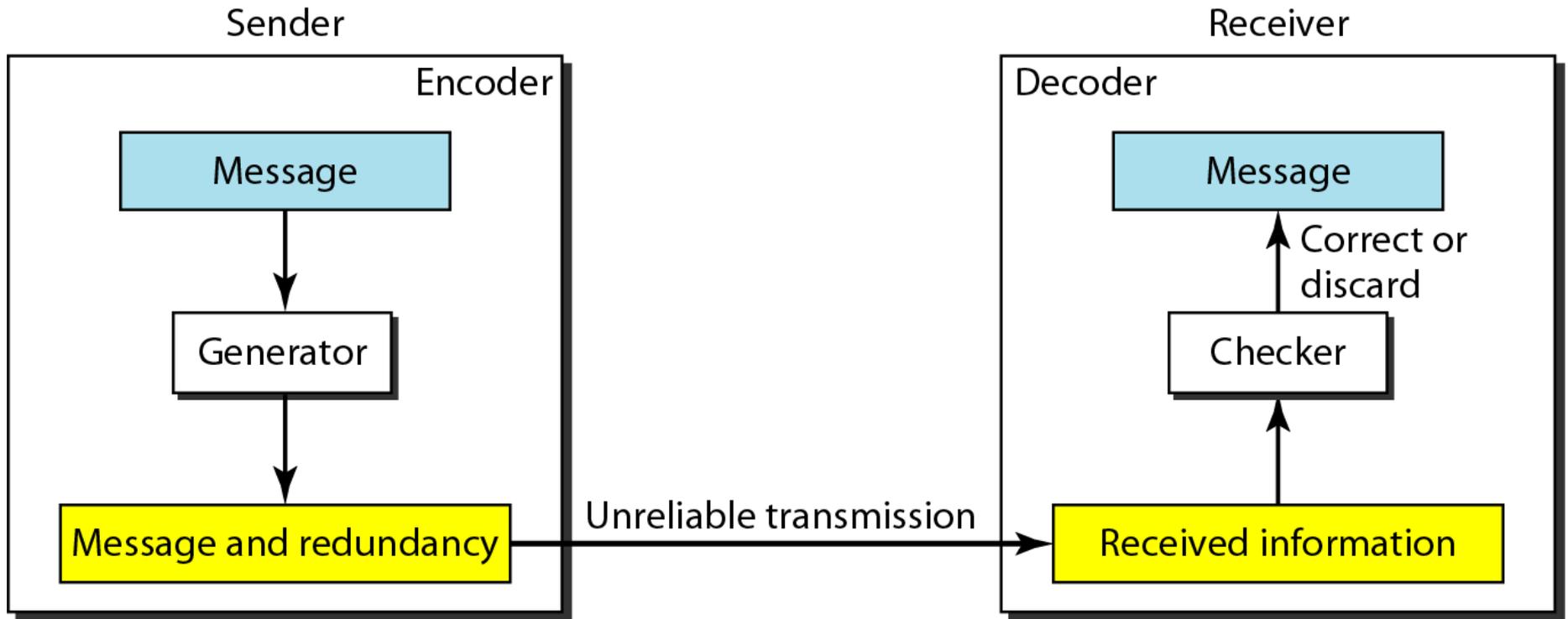


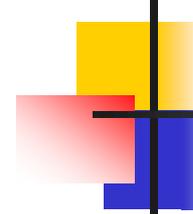
---

*Note*

**To detect or correct errors, we need to send extra (redundant) bits with data.**

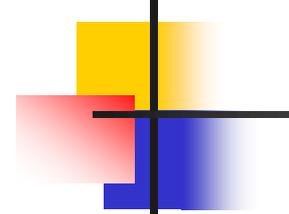
**Figure 10.3** *The structure of encoder and decoder*





*Note*

**In this book, we concentrate on block codes; we leave convolution codes to advanced texts.**



*Note*

**In modulo-N arithmetic, we use only the integers in the range 0 to  $N - 1$ , inclusive.**

## Figure 10.4 *XORing of two single bits or two words*

$$0 \oplus 0 = 0$$

$$1 \oplus 1 = 0$$

a. Two bits are the same, the result is 0.

$$0 \oplus 1 = 1$$

$$1 \oplus 0 = 1$$

b. Two bits are different, the result is 1.

	1	0	1	1	0
$\oplus$	1	1	1	0	0
<hr/>					
	0	1	0	1	0

c. Result of XORing two patterns

## 10-2 BLOCK CODING

*In block coding, we divide our message into blocks, each of  $k$  bits, called **datawords**. We add  $r$  redundant bits to each block to make the length  $n = k + r$ . The resulting  $n$ -bit blocks are called **codewords**.*

### *Topics discussed in this section:*

**Error Detection**

**Error Correction**

**Hamming Distance**

**Minimum Hamming Distance**

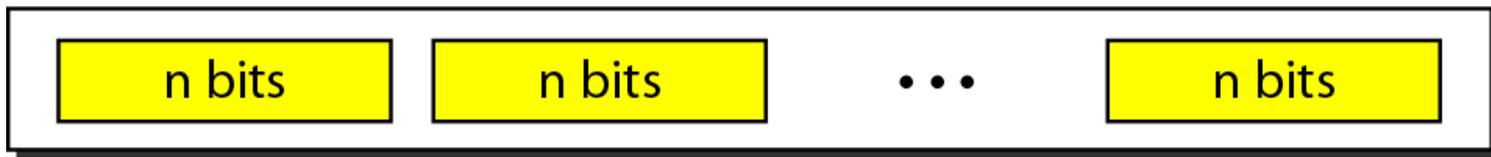
---

**Figure 10.5** *Datawords and codewords in block coding*

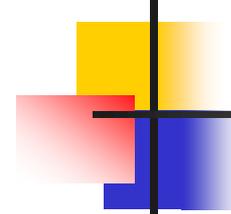
---



$2^k$  Datawords, each of  $k$  bits



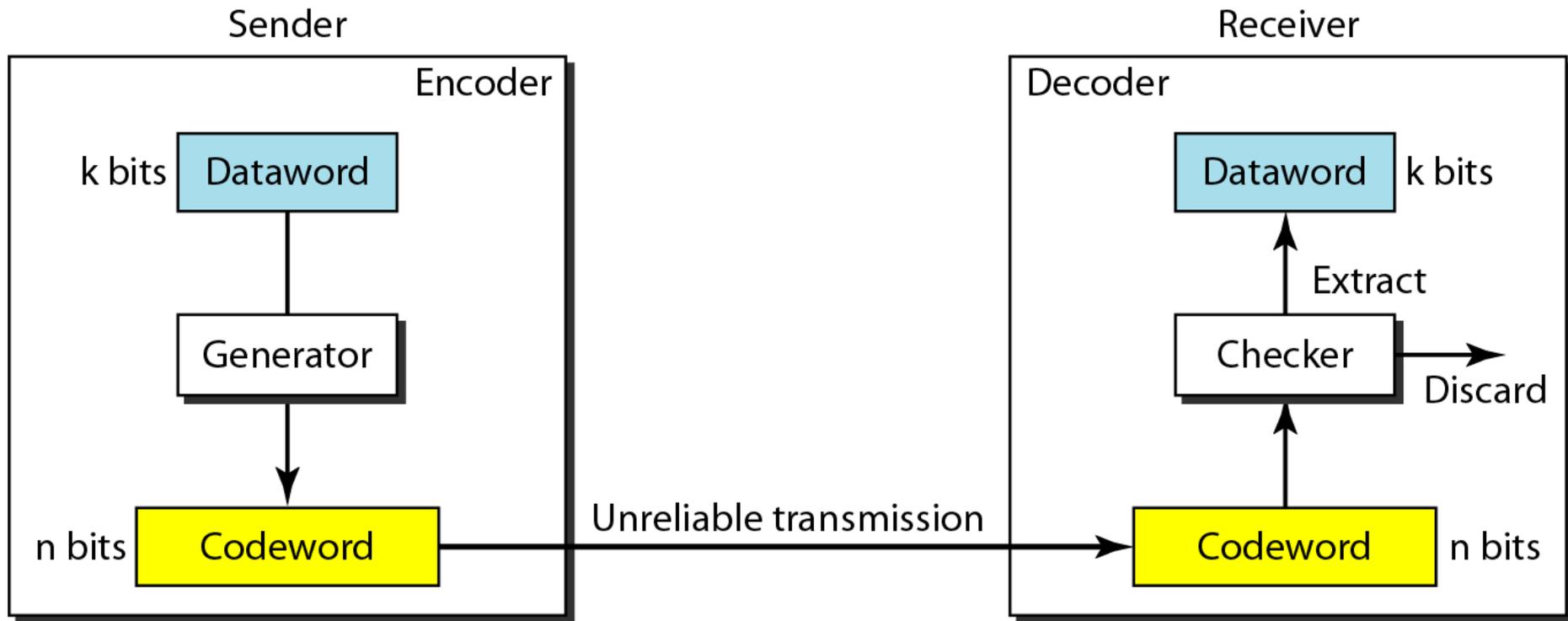
$2^n$  Codewords, each of  $n$  bits (only  $2^k$  of them are valid)

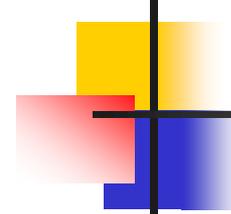


## *Example 10.1*

*The 4B/5B block coding discussed in Chapter 4 is a good example of this type of coding. In this coding scheme,  $k = 4$  and  $n = 5$ . As we saw, we have  $2^k = 16$  datawords and  $2^n = 32$  codewords. We saw that 16 out of 32 codewords are used for message transfer and the rest are either used for other purposes or unused.*

**Figure 10.6** *Process of error detection in block coding*





## *Example 10.2*

*Let us assume that  $k = 2$  and  $n = 3$ . Table 10.1 shows the list of datawords and codewords. Later, we will see how to derive a codeword from a dataword.*

*Assume the sender encodes the dataword 01 as 011 and sends it to the receiver. Consider the following cases:*

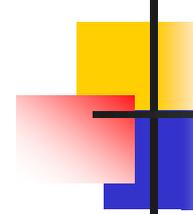
- 1. The receiver receives 011. It is a valid codeword. The receiver extracts the dataword 01 from it.*

## *Example 10.2 (continued)*

- 2. The codeword is corrupted during transmission, and 111 is received. This is not a valid codeword and is discarded.*
- 3. The codeword is corrupted during transmission, and 000 is received. This is a valid codeword. The receiver incorrectly extracts the dataword 00. Two corrupted bits have made the error undetectable.*

**Table 10.1** *A code for error detection (Example 10.2)*

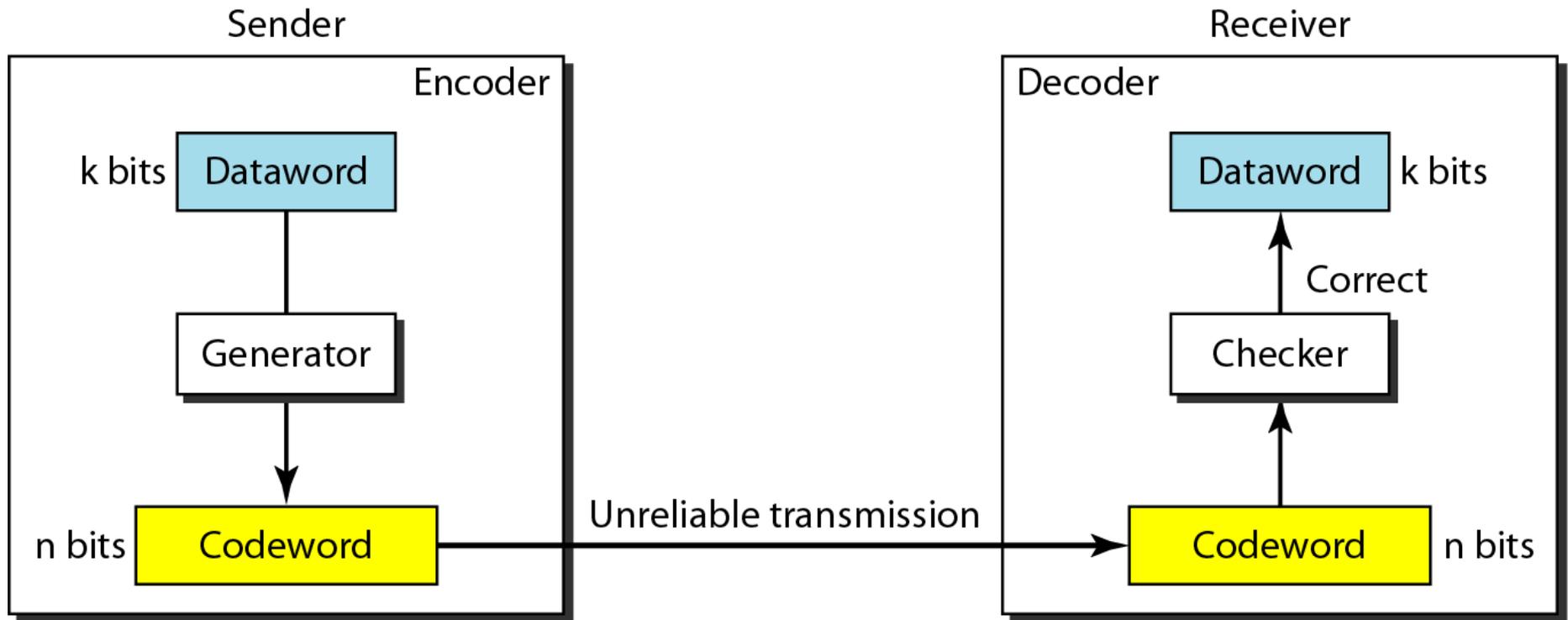
<i>Datawords</i>	<i>Codewords</i>
00	000
01	011
10	101
11	110

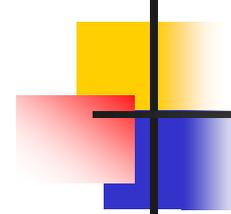


*Note*

**An error-detecting code can detect only the types of errors for which it is designed; other types of errors may remain undetected.**

**Figure 10.7** *Structure of encoder and decoder in error correction*





## *Example 10.3*

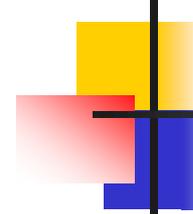
*Let us add more redundant bits to Example 10.2 to see if the receiver can correct an error without knowing what was actually sent. We add 3 redundant bits to the 2-bit dataword to make 5-bit codewords. Table 10.2 shows the datawords and codewords. Assume the dataword is 01. The sender creates the codeword 01011. The codeword is corrupted during transmission, and 01001 is received. First, the receiver finds that the received codeword is not in the table. This means an error has occurred. The receiver, assuming that there is only 1 bit corrupted, uses the following strategy to guess the correct dataword.*

## *Example 10.3 (continued)*

- 1. Comparing the received codeword with the first codeword in the table (01001 versus 00000), the receiver decides that the first codeword is not the one that was sent because there are two different bits.*
- 2. By the same reasoning, the original codeword cannot be the third or fourth one in the table.*
- 3. The original codeword must be the second one in the table because this is the only one that differs from the received codeword by 1 bit. The receiver replaces 01001 with 01011 and consults the table to find the dataword 01.*

**Table 10.2** *A code for error correction (Example 10.3)*

<i>Dataword</i>	<i>Codeword</i>
00	00000
01	01011
10	10101
11	11110



*Note*

**The Hamming distance between two words is the number of differences between corresponding bits.**

## Example 10.4

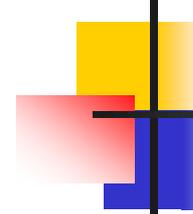
*Let us find the Hamming distance between two pairs of words.*

**1.** *The Hamming distance  $d(000, 011)$  is 2 because*

$$000 \oplus 011 \text{ is } 011 \text{ (two 1s)}$$

**2.** *The Hamming distance  $d(10101, 11110)$  is 3 because*

$$10101 \oplus 11110 \text{ is } 01011 \text{ (three 1s)}$$



*Note*

**The minimum Hamming distance is the smallest Hamming distance between all possible pairs in a set of words.**

## *Example 10.5*

*Find the minimum Hamming distance of the coding scheme in Table 10.1.*

### *Solution*

*We first find all Hamming distances.*

$$\begin{array}{llll} d(000, 011) = 2 & d(000, 101) = 2 & d(000, 110) = 2 & d(011, 101) = 2 \\ d(011, 110) = 2 & d(101, 110) = 2 & & \end{array}$$

*The  $d_{\min}$  in this case is 2.*

## *Example 10.6*

*Find the minimum Hamming distance of the coding scheme in Table 10.2.*

### *Solution*

*We first find all the Hamming distances.*

$$d(00000, 01011) = 3$$

$$d(00000, 10101) = 3$$

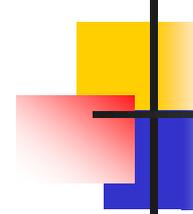
$$d(00000, 11110) = 4$$

$$d(01011, 10101) = 4$$

$$d(01011, 11110) = 3$$

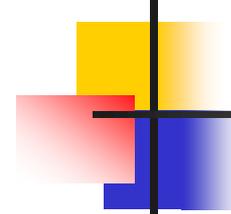
$$d(10101, 11110) = 3$$

*The  $d_{min}$  in this case is 3.*



*Note*

**To guarantee the detection of up to  $s$  errors in all cases, the minimum Hamming distance in a block code must be  $d_{\min} = s + 1$ .**



## *Example 10.7*

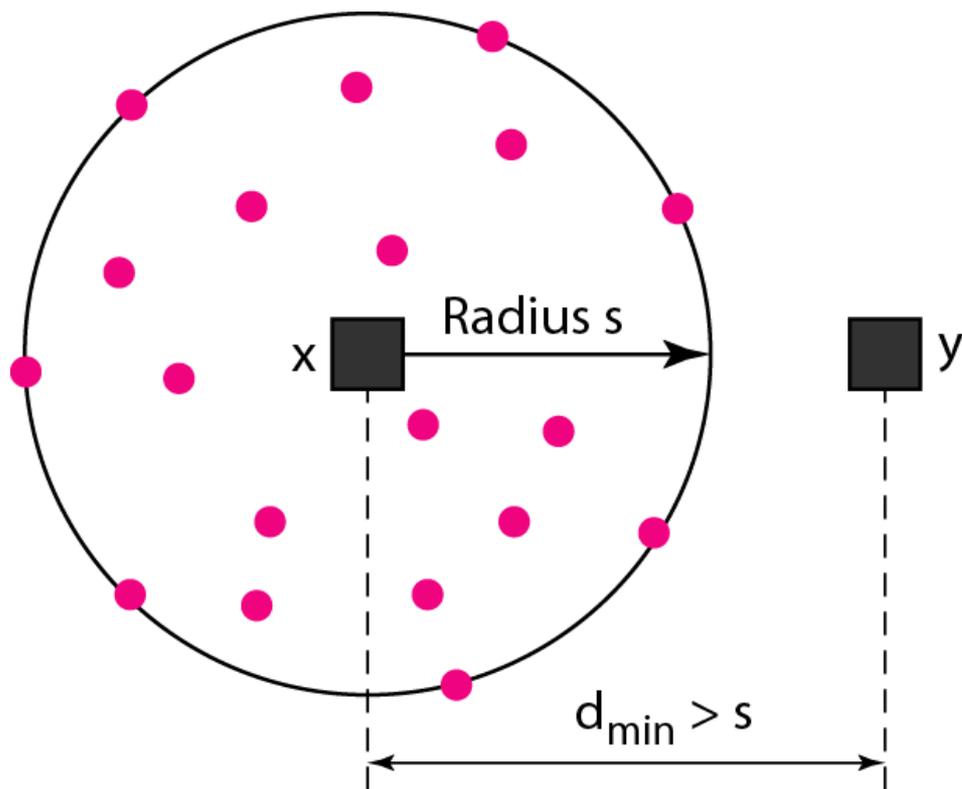
*The minimum Hamming distance for our first code scheme (Table 10.1) is 2. This code guarantees detection of only a single error. For example, if the third codeword (101) is sent and one error occurs, the received codeword does not match any valid codeword. If two errors occur, however, the received codeword may match a valid codeword and the errors are not detected.*

## *Example 10.8*

*Our second block code scheme (Table 10.2) has  $d_{min} = 3$ . This code can detect up to two errors. Again, we see that when any of the valid codewords is sent, two errors create a codeword which is not in the table of valid codewords. The receiver cannot be fooled.*

*However, some combinations of three errors change a valid codeword to another valid codeword. The receiver accepts the received codeword and the errors are undetected.*

**Figure 10.8** *Geometric concept for finding  $d_{min}$  in error detection*



Legend

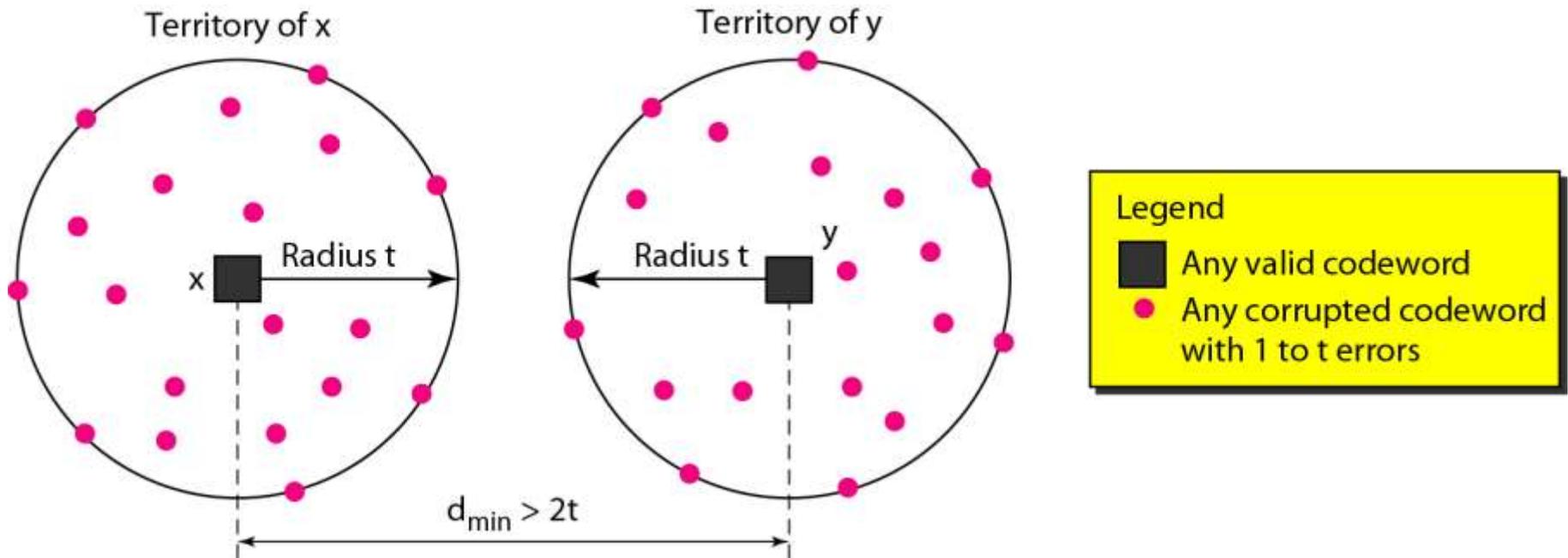


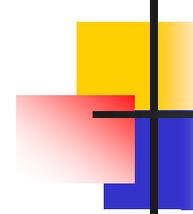
Any valid codeword



Any corrupted codeword  
with 0 to  $s$  errors

**Figure 10.9** *Geometric concept for finding  $d_{min}$  in error correction*





*Note*

**To guarantee correction of up to  $t$  errors in all cases, the minimum Hamming distance in a block code must be  $d_{\min} = 2t + 1$ .**

## Example 10.9

*A code scheme has a Hamming distance  $d_{min} = 4$ . What is the error detection and correction capability of this scheme?*

### *Solution*

*This code guarantees the detection of up to **three** errors ( $s = 3$ ), but it can correct up to **one** error. In other words, if this code is used for error correction, part of its capability is wasted. Error correction codes need to have an odd minimum distance (3, 5, 7, ...).*

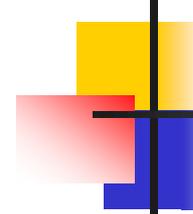
## 10-3 LINEAR BLOCK CODES

*Almost all block codes used today belong to a subset called **linear block codes**. A linear block code is a code in which the exclusive OR (addition modulo-2) of two valid codewords creates another valid codeword.*

*Topics discussed in this section:*

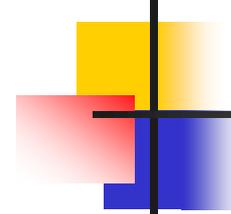
**Minimum Distance for Linear Block Codes**

**Some Linear Block Codes**



*Note*

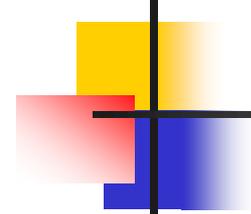
**In a linear block code, the exclusive OR (XOR) of any two valid codewords creates another valid codeword.**



## *Example 10.10*

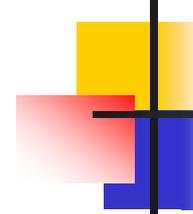
*Let us see if the two codes we defined in Table 10.1 and Table 10.2 belong to the class of linear block codes.*

- 1. The scheme in Table 10.1 is a linear block code because the result of XORing any codeword with any other codeword is a valid codeword. For example, the XORing of the second and third codewords creates the fourth one.*
- 2. The scheme in Table 10.2 is also a linear block code. We can create all four codewords by XORing two other codewords.*



## *Example 10.11*

*In our first code (Table 10.1), the numbers of 1s in the nonzero codewords are 2, 2, and 2. So the minimum Hamming distance is  $d_{min} = 2$ . In our second code (Table 10.2), the numbers of 1s in the nonzero codewords are 3, 3, and 4. So in this code we have  $d_{min} = 3$ .*



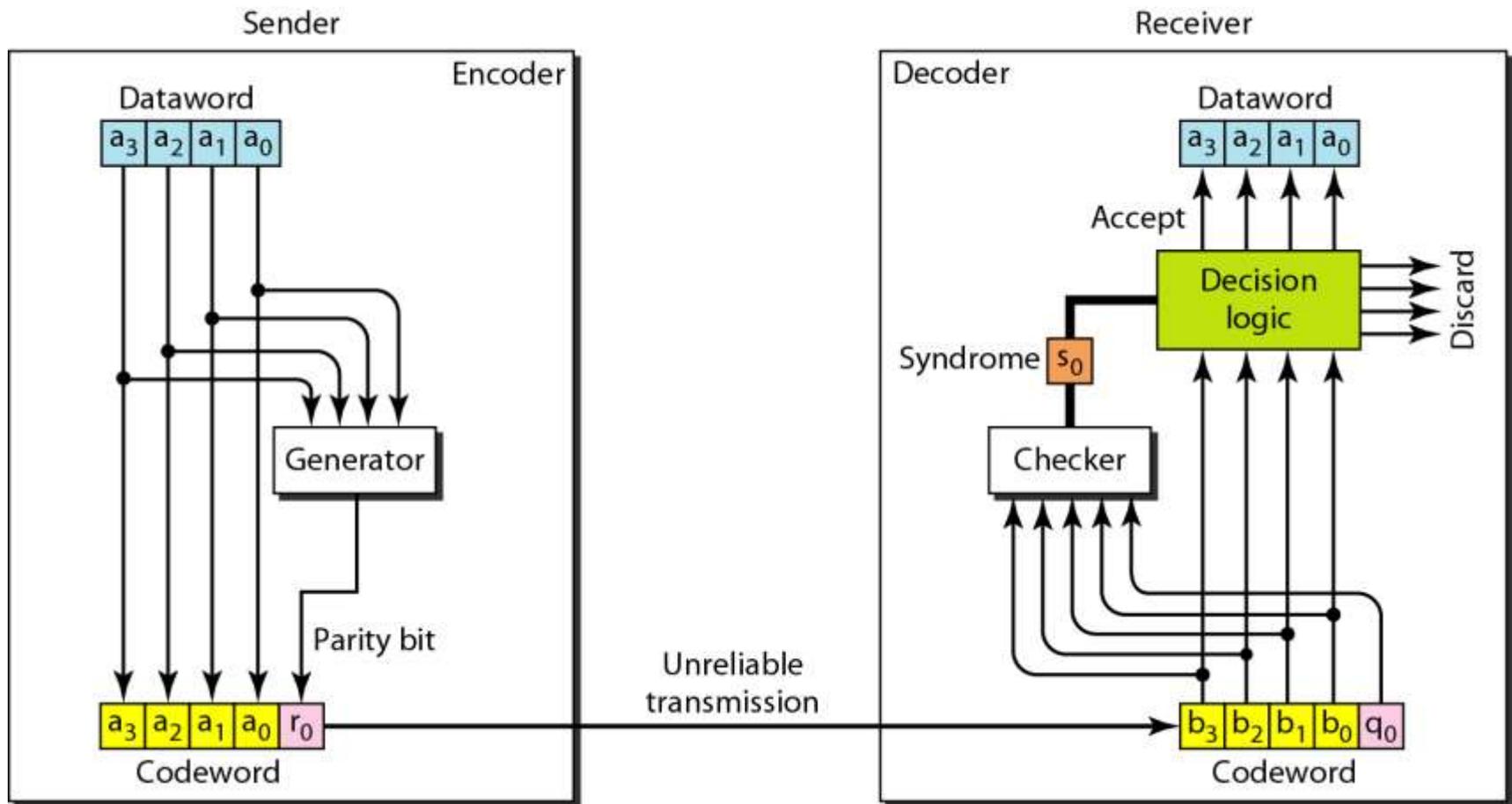
*Note*

**A simple parity-check code is a  
single-bit error-detecting  
code in which  
 $n = k + 1$  with  $d_{\min} = 2$ .**

**Table 10.3** *Simple parity-check code C(5, 4)*

<i>Datawords</i>	<i>Codewords</i>	<i>Datawords</i>	<i>Codewords</i>
0000	00000	1000	10001
0001	00011	1001	10010
0010	00101	1010	10100
0011	00110	1011	10111
0100	01001	1100	11000
0101	01010	1101	11011
0110	01100	1110	11101
0111	01111	1111	11110

**Figure 10.10** *Encoder and decoder for simple parity-check code*



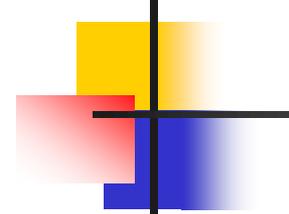
## *Example 10.12*

*Let us look at some transmission scenarios. Assume the sender sends the dataword 1011. The codeword created from this dataword is 10111, which is sent to the receiver. We examine five cases:*

- 1. No error occurs; the received codeword is 10111. The syndrome is 0. The dataword 1011 is created.*
- 2. One single-bit error changes  $a_1$ . The received codeword is 10011. The syndrome is 1. No dataword is created.*
- 3. One single-bit error changes  $r_0$ . The received codeword is 10110. The syndrome is 1. No dataword is created.*

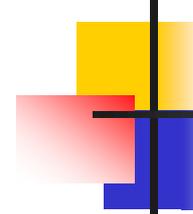
## *Example 10.12 (continued)*

- 4. An error changes  $r_0$  and a second error changes  $a_3$ . The received codeword is 00110. The syndrome is 0. The dataword 0011 is created at the receiver. Note that here the dataword is wrongly created due to the syndrome value.*
- 5. Three bits— $a_3$ ,  $a_2$ , and  $a_1$ —are changed by errors. The received codeword is 01011. The syndrome is 1. The dataword is not created. This shows that the simple parity check, guaranteed to detect one single error, can also find any odd number of errors.*



*Note*

**A simple parity-check code can detect an odd number of errors.**



*Note*

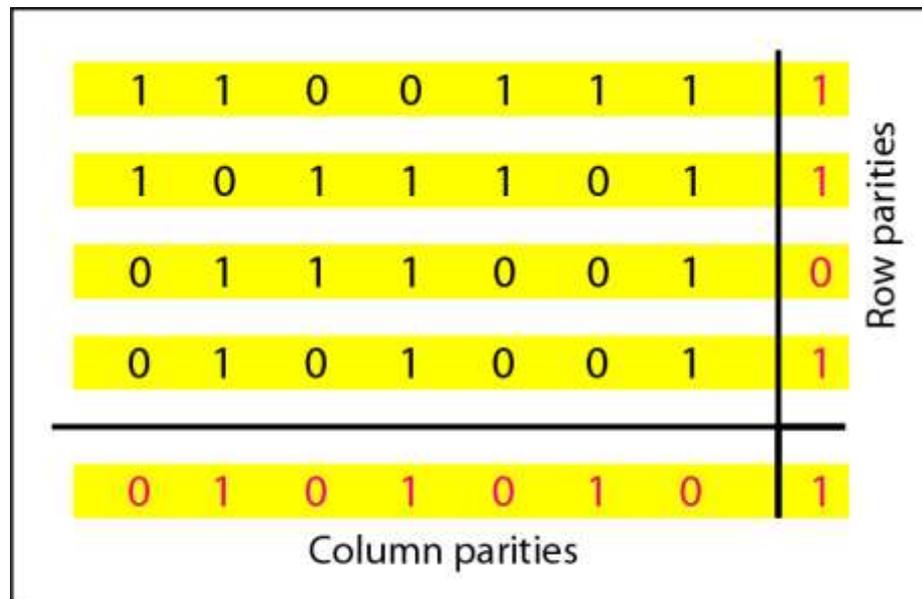
**All Hamming codes discussed in this book have  $d_{\min} = 3$ .**

**The relationship between  $m$  and  $n$  in these codes is  $n = 2m - 1$ .**

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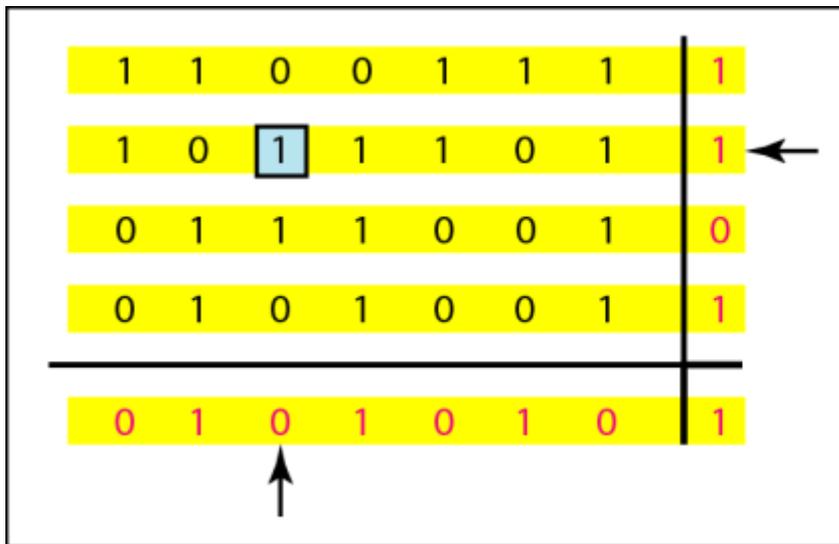
**Figure 10.11** *Two-dimensional parity-check code*

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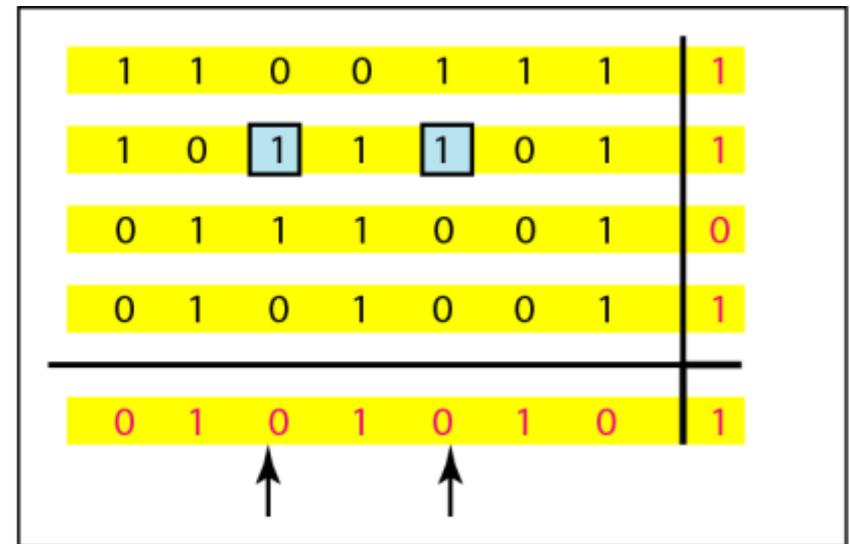


a. Design of row and column parities

**Figure 10.11** *Two-dimensional parity-check code*

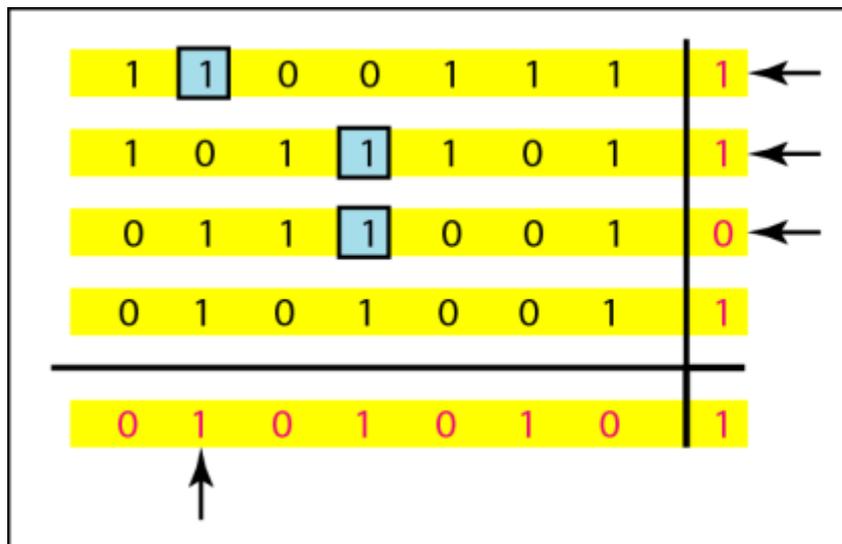


b. One error affects two parities

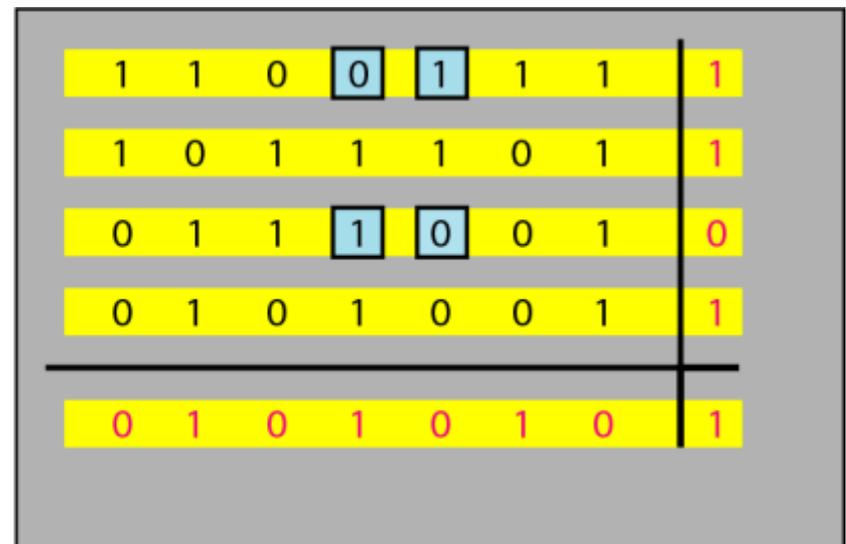


c. Two errors affect two parities

**Figure 10.11** *Two-dimensional parity-check code*



d. Three errors affect four parities

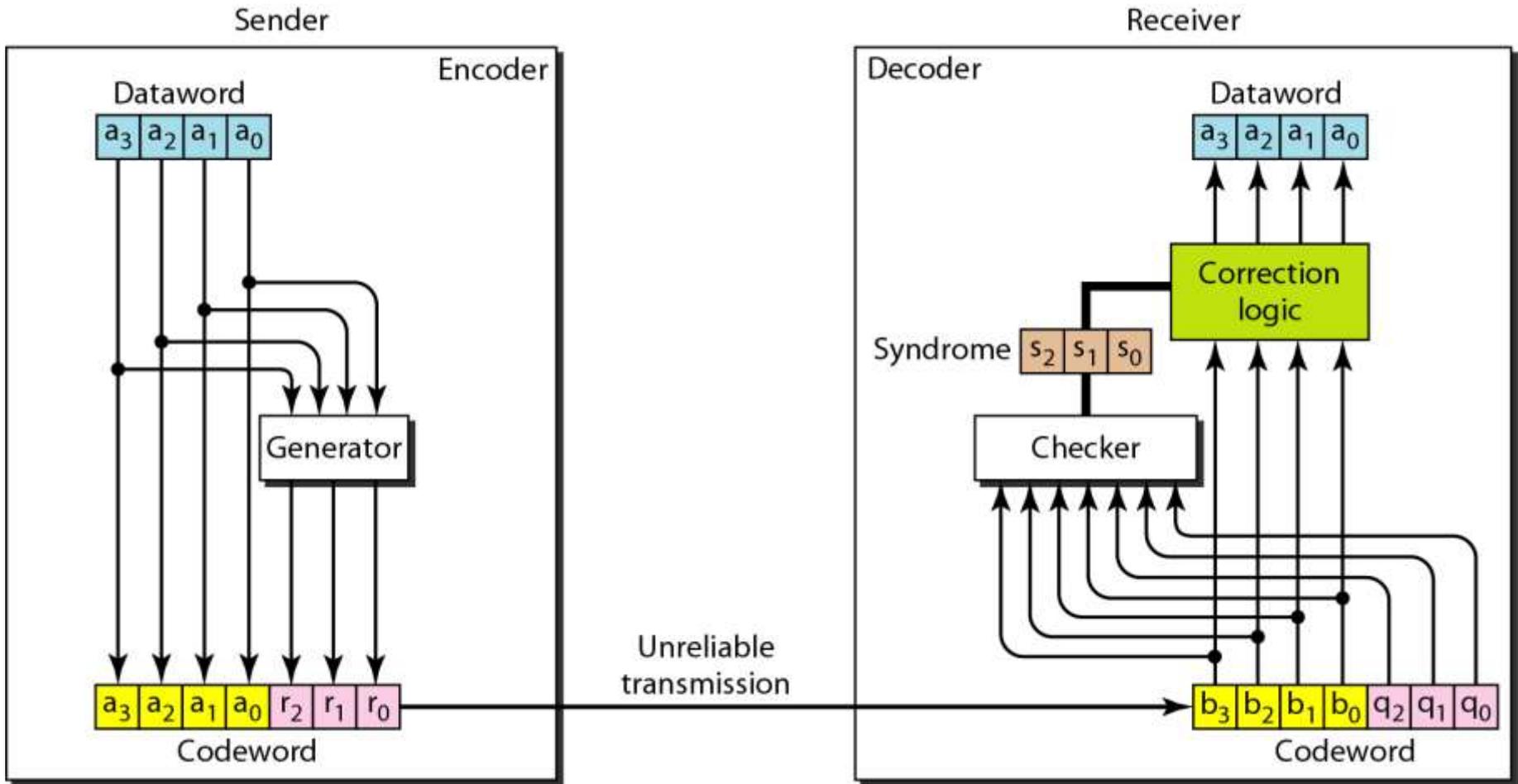


e. Four errors cannot be detected

**Table 10.4** *Hamming code C(7, 4)*

<i>Datawords</i>	<i>Codewords</i>	<i>Datawords</i>	<i>Codewords</i>
0000	0000000	1000	1000110
0001	0001101	1001	1001011
0010	0010111	1010	1010001
0011	0011010	1011	1011100
0100	0100011	1100	1100101
0101	0101110	1101	1101000
0110	0110100	1110	1110010
0111	0111001	1111	1111111

**Figure 10.12** *The structure of the encoder and decoder for a Hamming code*



**Table 10.5** *Logical decision made by the correction logic analyzer*

<i>Syndrome</i>	000	001	010	011	100	101	110	111
<i>Error</i>	None	$q_0$	$q_1$	$b_2$	$q_2$	$b_0$	$b_3$	$b_1$

## *Example 10.13*

*Let us trace the path of three datawords from the sender to the destination:*

- 1. The dataword 0100 becomes the codeword 0100011. The codeword 0100011 is received. The syndrome is 000, the final dataword is 0100.*
- 2. The dataword 0111 becomes the codeword 0111001. The syndrome is 011. After flipping  $b_2$  (changing the 1 to 0), the final dataword is 0111.*
- 3. The dataword 1101 becomes the codeword 1101000. The syndrome is 101. After flipping  $b_0$ , we get 0000, the wrong dataword. This shows that our code cannot correct two errors.*

## *Example 10.14*

*We need a dataword of at least 7 bits. Calculate values of  $k$  and  $n$  that satisfy this requirement.*

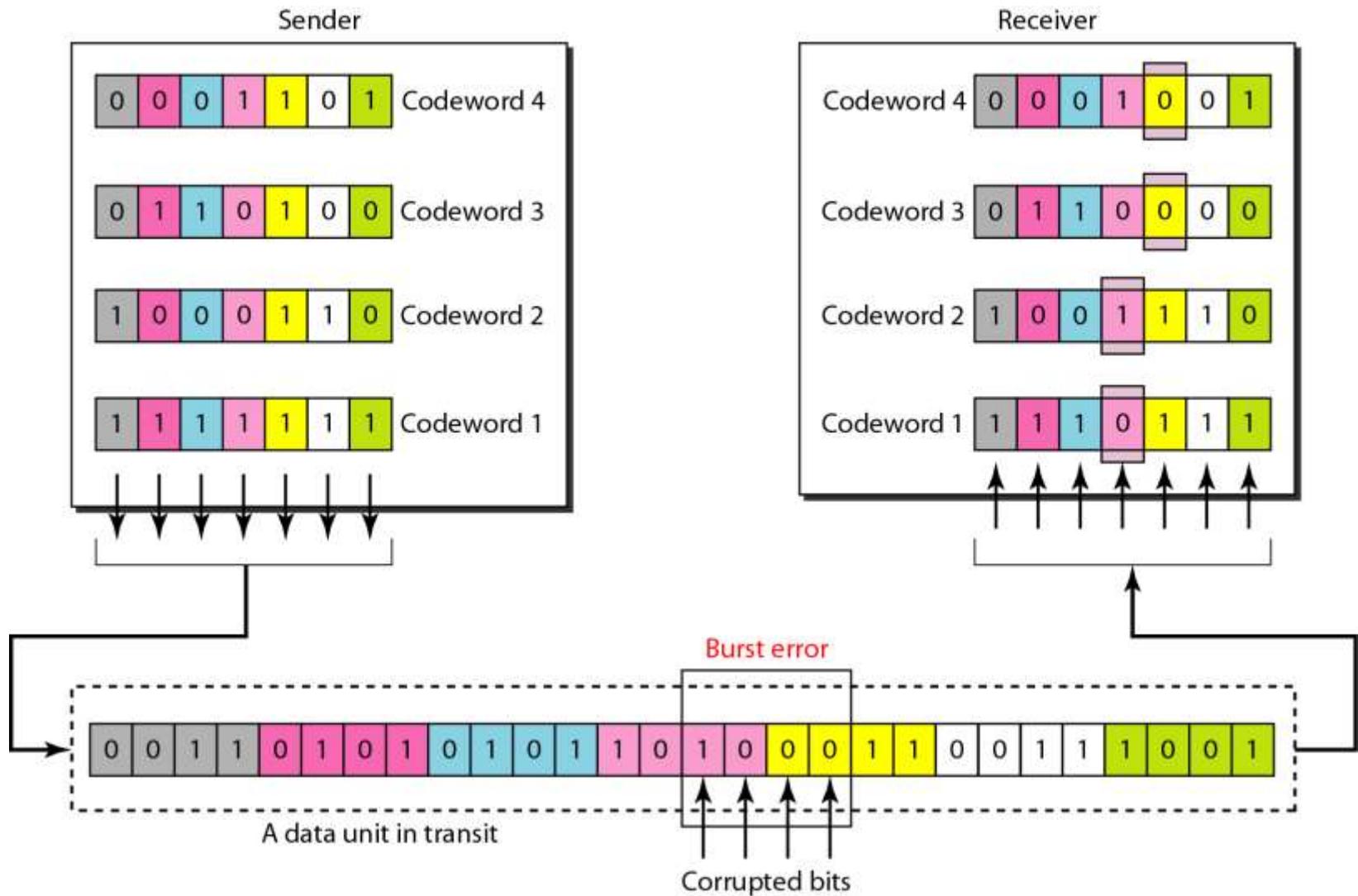
### *Solution*

*We need to make  $k = n - m$  greater than or equal to 7, or  $2^m - 1 - m \geq 7$ .*

- 1. If we set  $m = 3$ , the result is  $n = 2^3 - 1 = 7$  and  $k = 7 - 3 = 4$ , which is not acceptable.*
- 2. If we set  $m = 4$ , then  $n = 2^4 - 1 = 15$  and  $k = 15 - 4 = 11$ , which satisfies the condition. So the code is*

**$C(15, 11)$**

**Figure 10.13** *Burst error correction using Hamming code*



## 10-4 CYCLIC CODES

*Cyclic codes are special linear block codes with one extra property. In a cyclic code, if a codeword is cyclically shifted (rotated), the result is another codeword.*

### Topics discussed in this section:

Cyclic Redundancy Check

Hardware Implementation

Polynomials

Cyclic Code Analysis

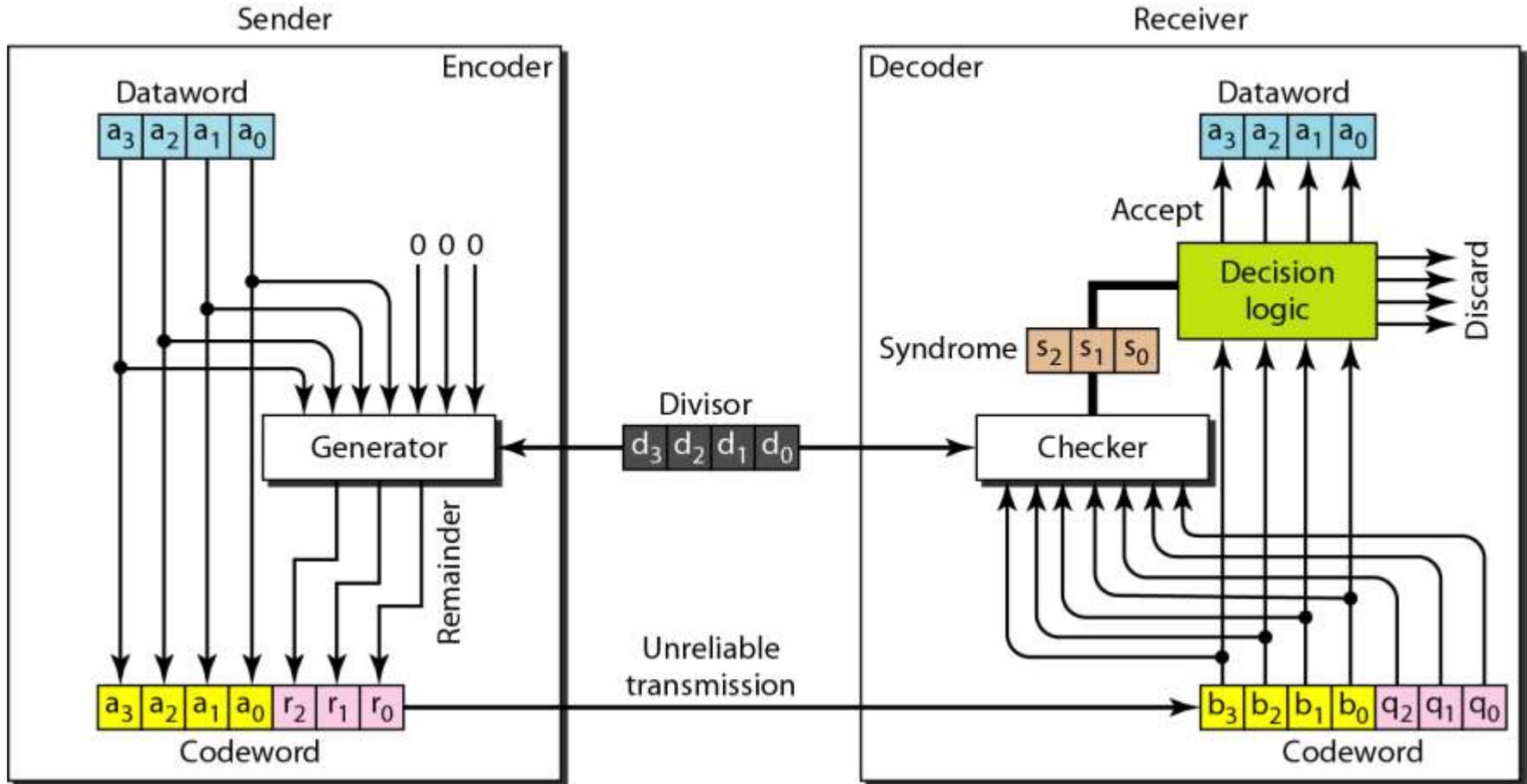
Advantages of Cyclic Codes

Other Cyclic Codes

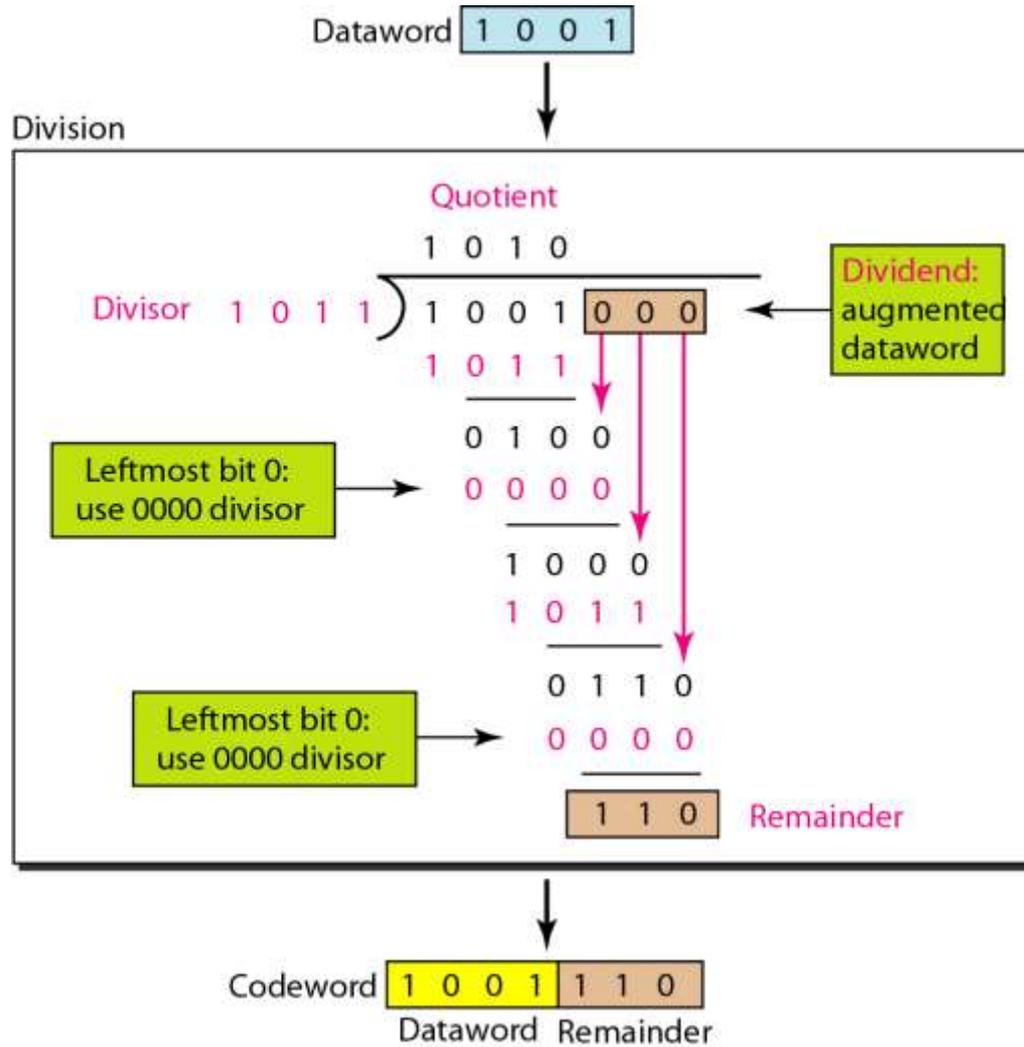
**Table 10.6** *A CRC code with  $C(7, 4)$*

<i>Dataword</i>	<i>Codeword</i>	<i>Dataword</i>	<i>Codeword</i>
0000	0000000	1000	1000101
0001	0001011	1001	1001110
0010	0010110	1010	1010011
0011	0011101	1011	1011000
0100	0100111	1100	1100010
0101	0101100	1101	1101001
0110	0110001	1110	1110100
0111	0111010	1111	1111111

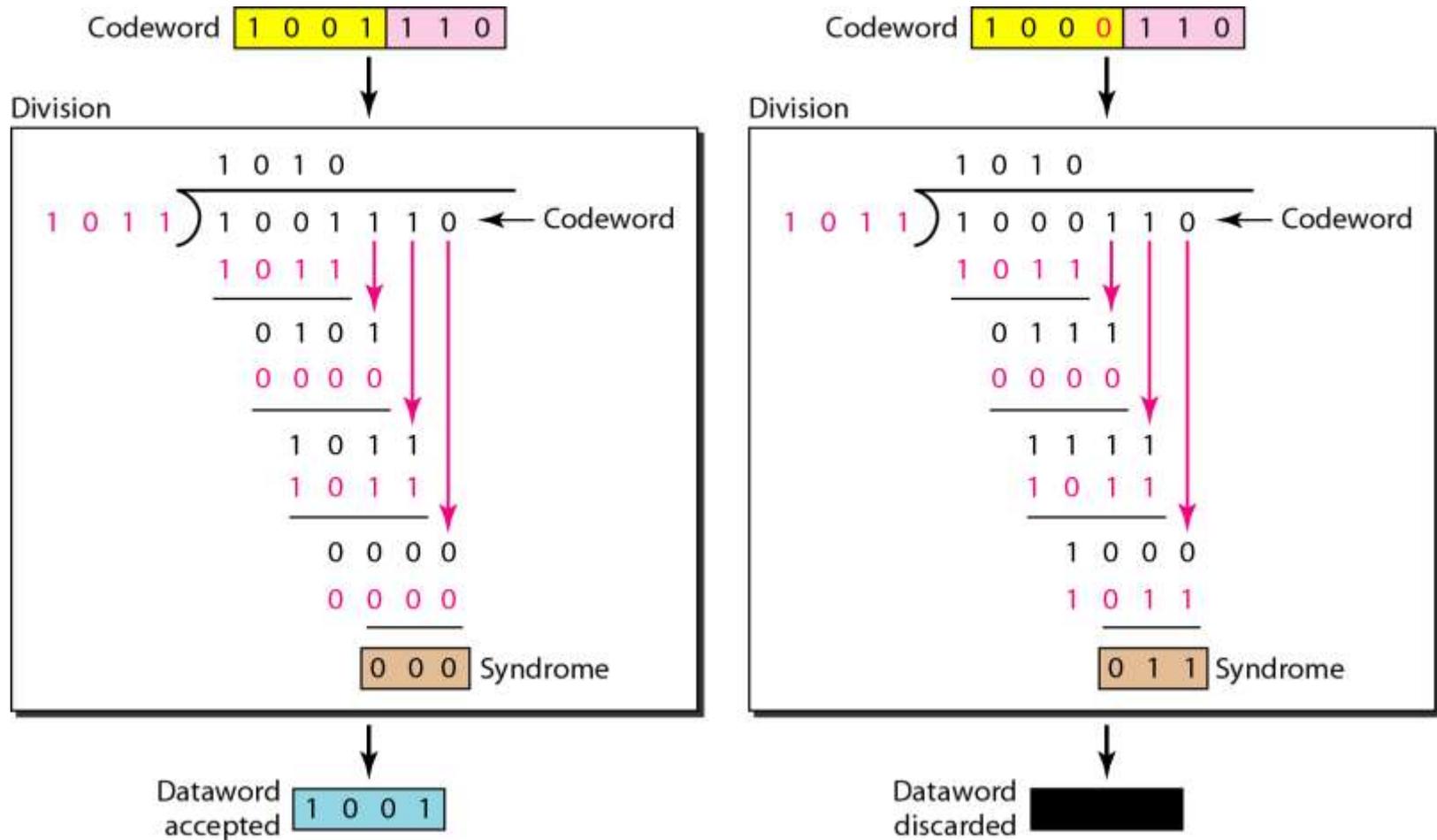
**Figure 10.14** *CRC encoder and decoder*



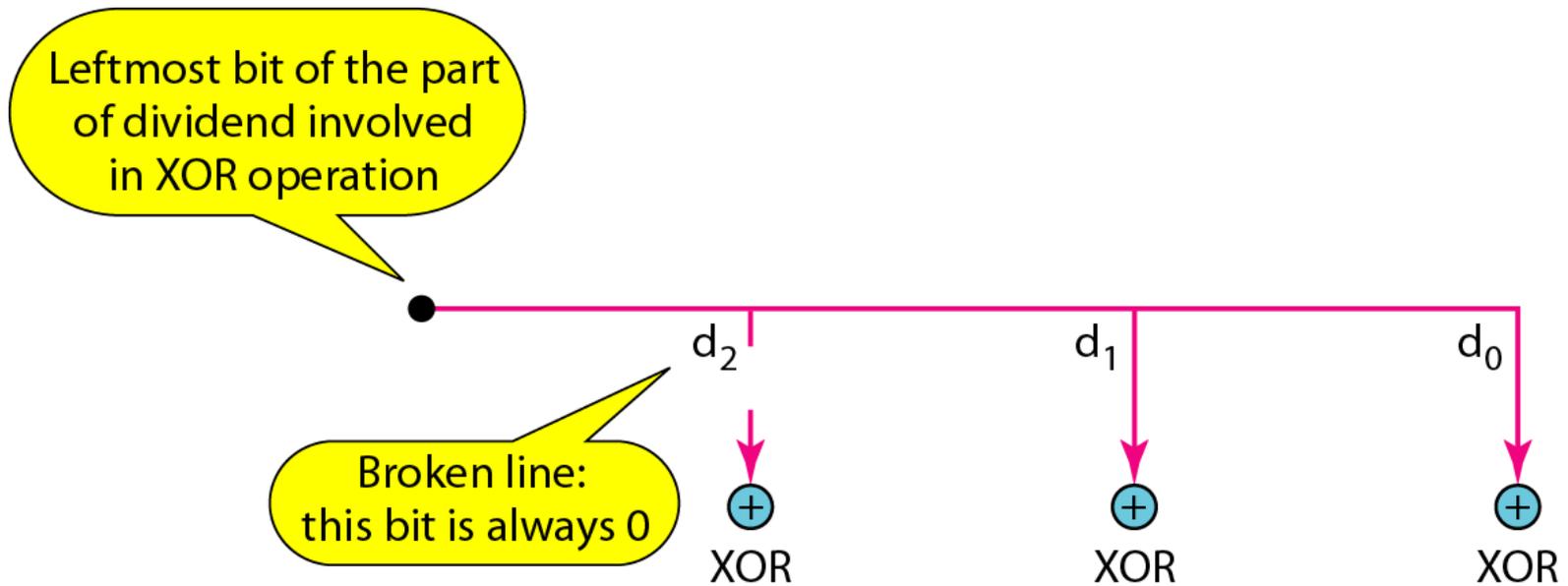
**Figure 10.15** *Division in CRC encoder*



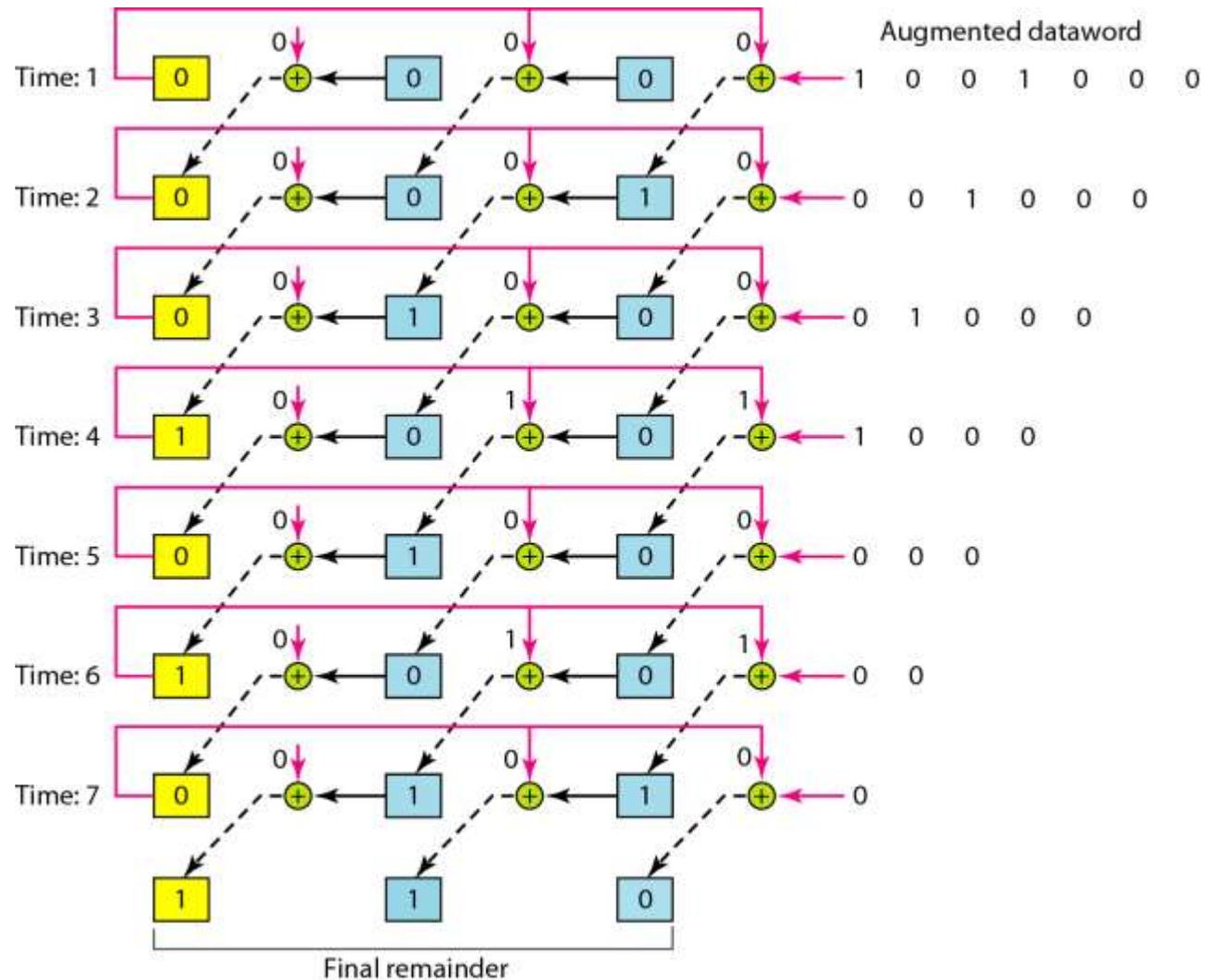
**Figure 10.16** *Division in the CRC decoder for two cases*



**Figure 10.17** *Hardwired design of the divisor in CRC*



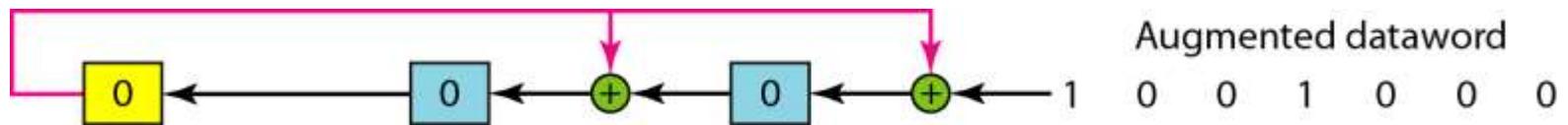
**Figure 10.18** *Simulation of division in CRC encoder*



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**Figure 10.19** *The CRC encoder design using shift registers*

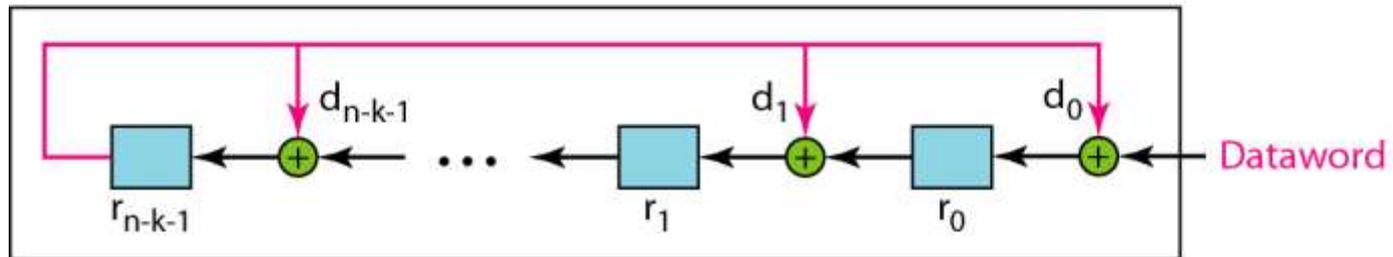
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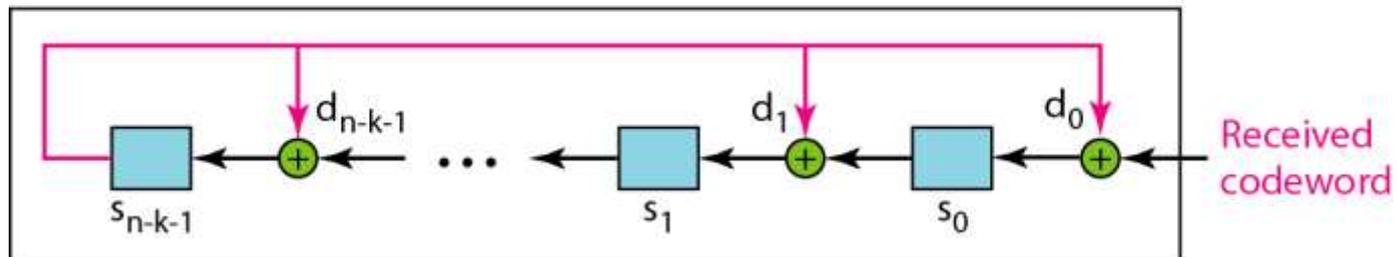
**Figure 10.20** *General design of encoder and decoder of a CRC code*

Note:

The divisor line and XOR are missing if the corresponding bit in the divisor is 0.

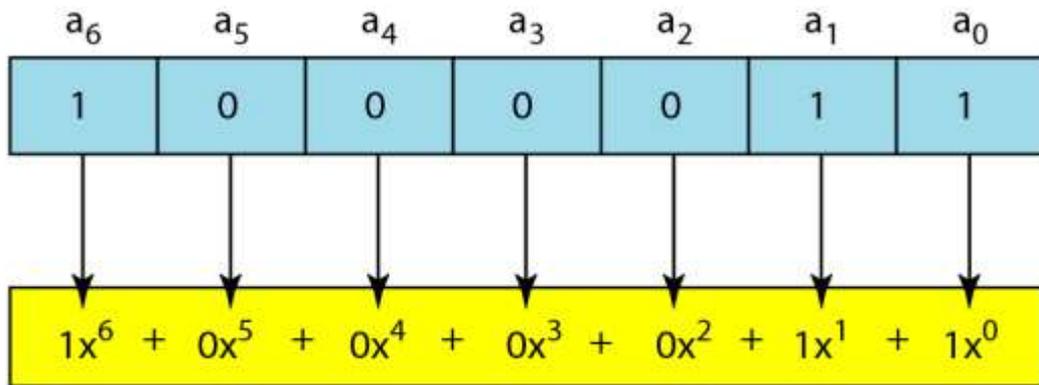


a. Encoder

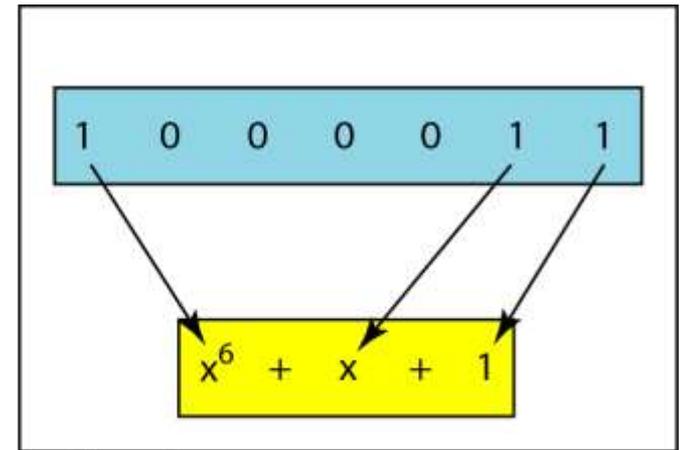


b. Decoder

**Figure 10.21** *A polynomial to represent a binary word*

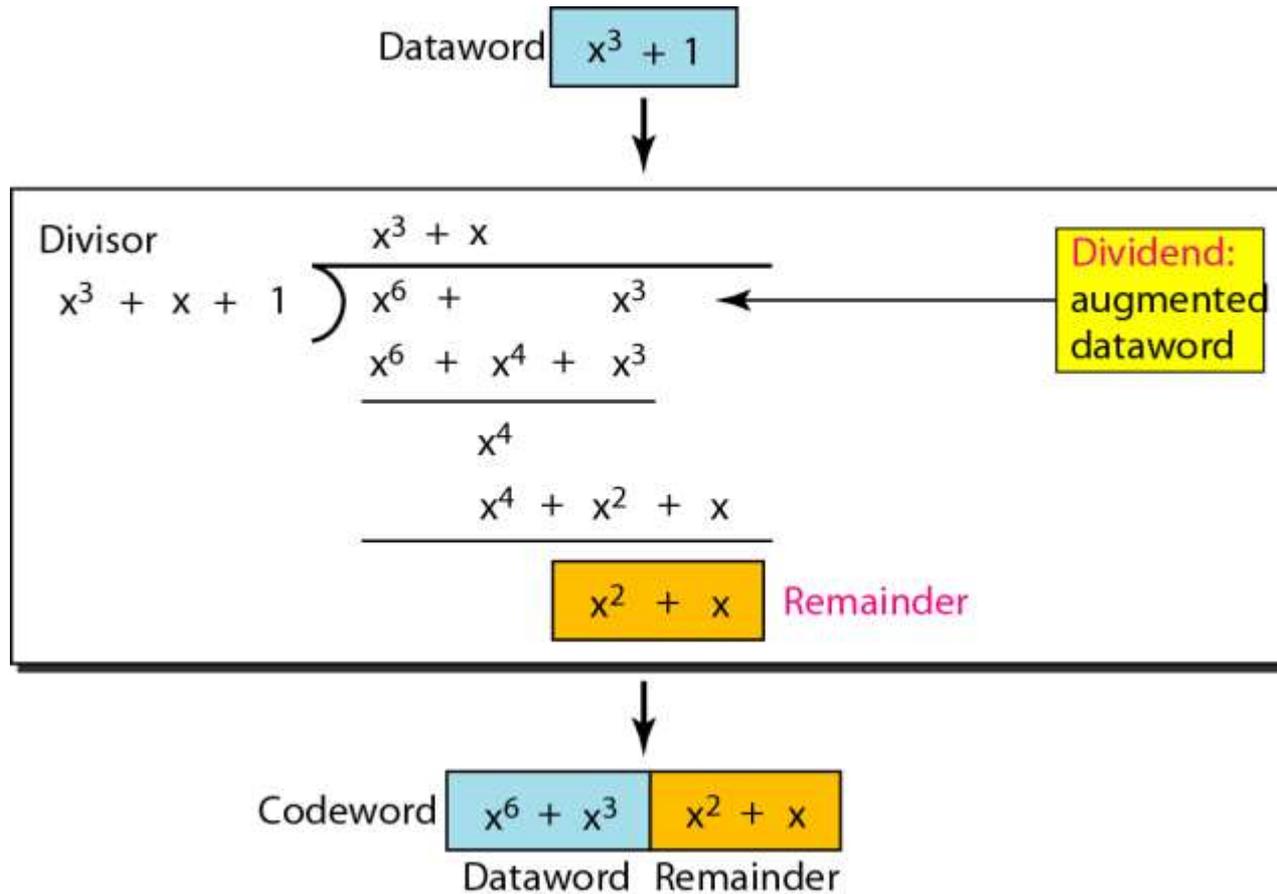


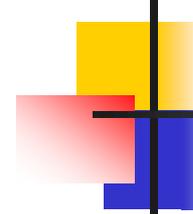
a. Binary pattern and polynomial



b. Short form

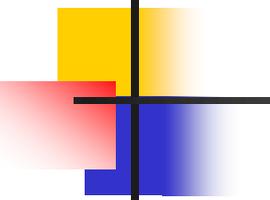
**Figure 10.22** *CRC division using polynomials*





*Note*

**The divisor in a cyclic code is normally called the generator polynomial or simply the generator.**



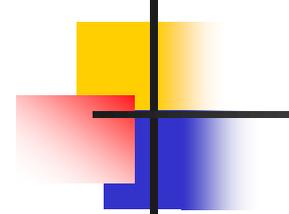
**Note**

**In a cyclic code,**

**If  $s(x) \neq 0$ , one or more bits is corrupted.**

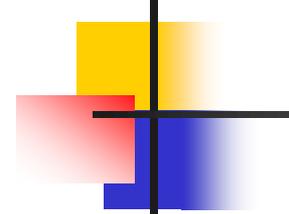
**If  $s(x) = 0$ , either**

- a. No bit is corrupted. or**
- b. Some bits are corrupted, but the decoder failed to detect them.**



*Note*

**In a cyclic code, those  $e(x)$  errors that are divisible by  $g(x)$  are not caught.**



*Note*

**If the generator has more than one term  
and the coefficient of  $x^0$  is 1,  
all single errors can be caught.**

## Example 10.15

*Which of the following  $g(x)$  values guarantees that a single-bit error is caught? For each case, what is the error that cannot be caught?*

- a.  $x + 1$       b.  $x^3$       c.  $1$*

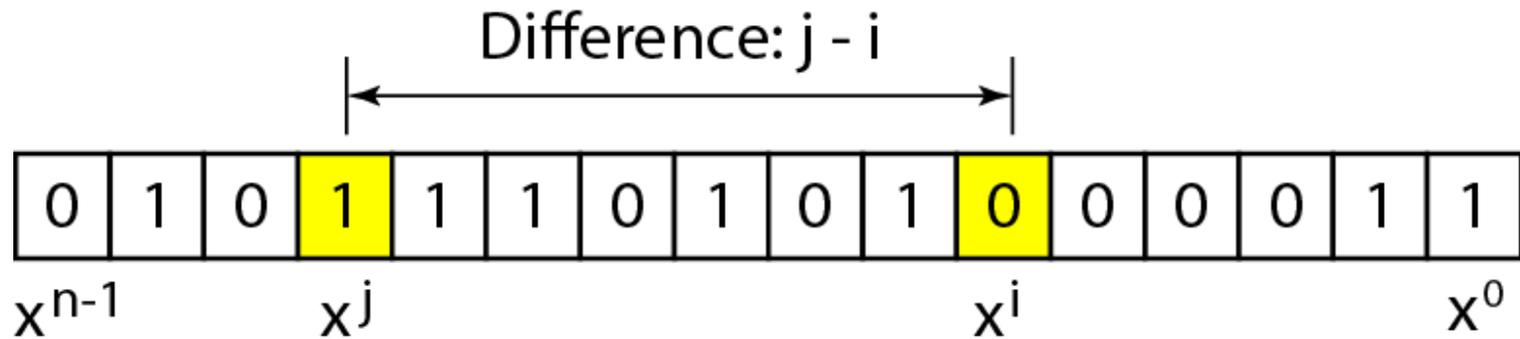
### *Solution*

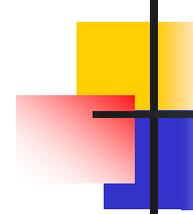
- a. No  $x^i$  can be divisible by  $x + 1$ . Any single-bit error can be caught.*
- b. If  $i$  is equal to or greater than 3,  $x^i$  is divisible by  $g(x)$ . All single-bit errors in positions 1 to 3 are caught.*
- c. All values of  $i$  make  $x^i$  divisible by  $g(x)$ . No single-bit error can be caught. This  $g(x)$  is useless.*

---

**Figure 10.23** *Representation of two isolated single-bit errors using polynomials*

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*Note*

**If a generator cannot divide  $x^t + 1$   
( $t$  between 0 and  $n - 1$ ),  
then all isolated double errors  
can be detected.**

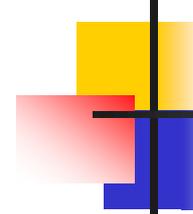
## *Example 10.16*

*Find the status of the following generators related to two isolated, single-bit errors.*

*a.  $x + 1$     b.  $x^4 + 1$     c.  $x^7 + x^6 + 1$     d.  $x^{15} + x^{14} + 1$*

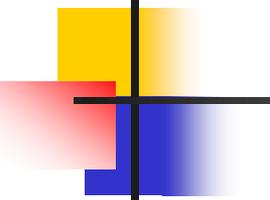
### *Solution*

- a. This is a very poor choice for a generator. Any two errors next to each other cannot be detected.*
- b. This generator cannot detect two errors that are four positions apart.*
- c. This is a good choice for this purpose.*
- d. This polynomial cannot divide  $x^t + 1$  if  $t$  is less than 32,768. A codeword with two isolated errors up to 32,768 bits apart can be detected by this generator.*



*Note*

**A generator that contains a factor of  $x + 1$  can detect all odd-numbered errors.**



*Note*

- ❑ All burst errors with  $L \leq r$  will be detected.
- ❑ All burst errors with  $L = r + 1$  will be detected with probability  $1 - (1/2)^{r-1}$ .
- ❑ All burst errors with  $L > r + 1$  will be detected with probability  $1 - (1/2)^r$ .

## *Example 10.17*

*Find the suitability of the following generators in relation to burst errors of different lengths.*

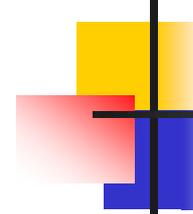
*a.*  $x^6 + 1$       *b.*  $x^{18} + x^7 + x + 1$       *c.*  $x^{32} + x^{23} + x^7 + 1$

### *Solution*

*a.* *This generator can detect all burst errors with a length less than or equal to 6 bits; 3 out of 100 burst errors with length 7 will slip by; 16 out of 1000 burst errors of length 8 or more will slip by.*

## *Example 10.17 (continued)*

- b. This generator can detect all burst errors with a length less than or equal to 18 bits; 8 out of 1 million burst errors with length 19 will slip by; 4 out of 1 million burst errors of length 20 or more will slip by.*
  
- c. This generator can detect all burst errors with a length less than or equal to 32 bits; 5 out of 10 billion burst errors with length 33 will slip by; 3 out of 10 billion burst errors of length 34 or more will slip by.*



**Note**

**A good polynomial generator needs to have the following characteristics:**

- 1. It should have at least two terms.**
- 2. The coefficient of the term  $x^0$  should be 1.**
- 3. It should not divide  $x^t + 1$ , for  $t$  between 2 and  $n - 1$ .**
- 4. It should have the factor  $x + 1$ .**

**Table 10.7** *Standard polynomials*

<i>Name</i>	<i>Polynomial</i>	<i>Application</i>
CRC-8	$x^8 + x^2 + x + 1$	ATM header
CRC-10	$x^{10} + x^9 + x^5 + x^4 + x^2 + 1$	ATM AAL
CRC-16	$x^{16} + x^{12} + x^5 + 1$	HDLC
CRC-32	$x^{32} + x^{26} + x^{23} + x^{22} + x^{16} + x^{12} + x^{11} + x^{10} + x^8 + x^7 + x^5 + x^4 + x^2 + x + 1$	LANs

## 10-5 CHECKSUM

*The last error detection method we discuss here is called the checksum. The checksum is used in the Internet by several protocols although not at the data link layer. However, we briefly discuss it here to complete our discussion on error checking*

### *Topics discussed in this section:*

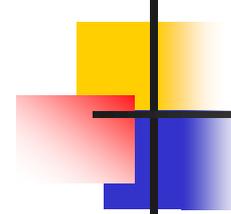
Idea

One's Complement

Internet Checksum

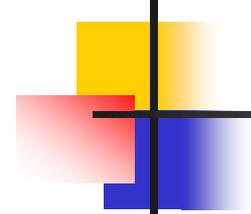
## Example 10.18

*Suppose our data is a list of five 4-bit numbers that we want to send to a destination. In addition to sending these numbers, we send the sum of the numbers. For example, if the set of numbers is (7, 11, 12, 0, 6), we send (7, 11, 12, 0, 6, 36), where 36 is the sum of the original numbers. The receiver adds the five numbers and compares the result with the sum. If the two are the same, the receiver assumes no error, accepts the five numbers, and discards the sum. Otherwise, there is an error somewhere and the data are not accepted.*



## *Example 10.19*

*We can make the job of the receiver easier if we send the negative (complement) of the sum, called the **checksum**. In this case, we send (7, 11, 12, 0, 6, **-36**). The receiver can add all the numbers received (including the checksum). If the result is 0, it assumes no error; otherwise, there is an error.*

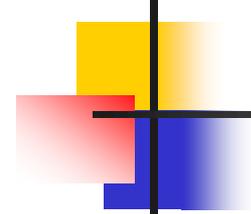


## *Example 10.20*

*How can we represent the number 21 in **one's complement arithmetic** using only four bits?*

### *Solution*

*The number 21 in binary is 10101 (it needs five bits). We can wrap the leftmost bit and add it to the four rightmost bits. We have  $(0101 + 1) = 0110$  or **6**.*



## *Example 10.21*

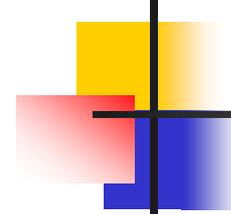
*How can we represent the number  $-6$  in one's complement arithmetic using only four bits?*

### *Solution*

*In one's complement arithmetic, the negative or complement of a number is found by inverting all bits. Positive 6 is 0110; negative 6 is 1001. If we consider only unsigned numbers, this is 9. In other words, the complement of 6 is 9. Another way to find the complement of a number in one's complement arithmetic is to subtract the number from  $2^n - 1$  ( $16 - 1$  in this case).*

## *Example 10.22*

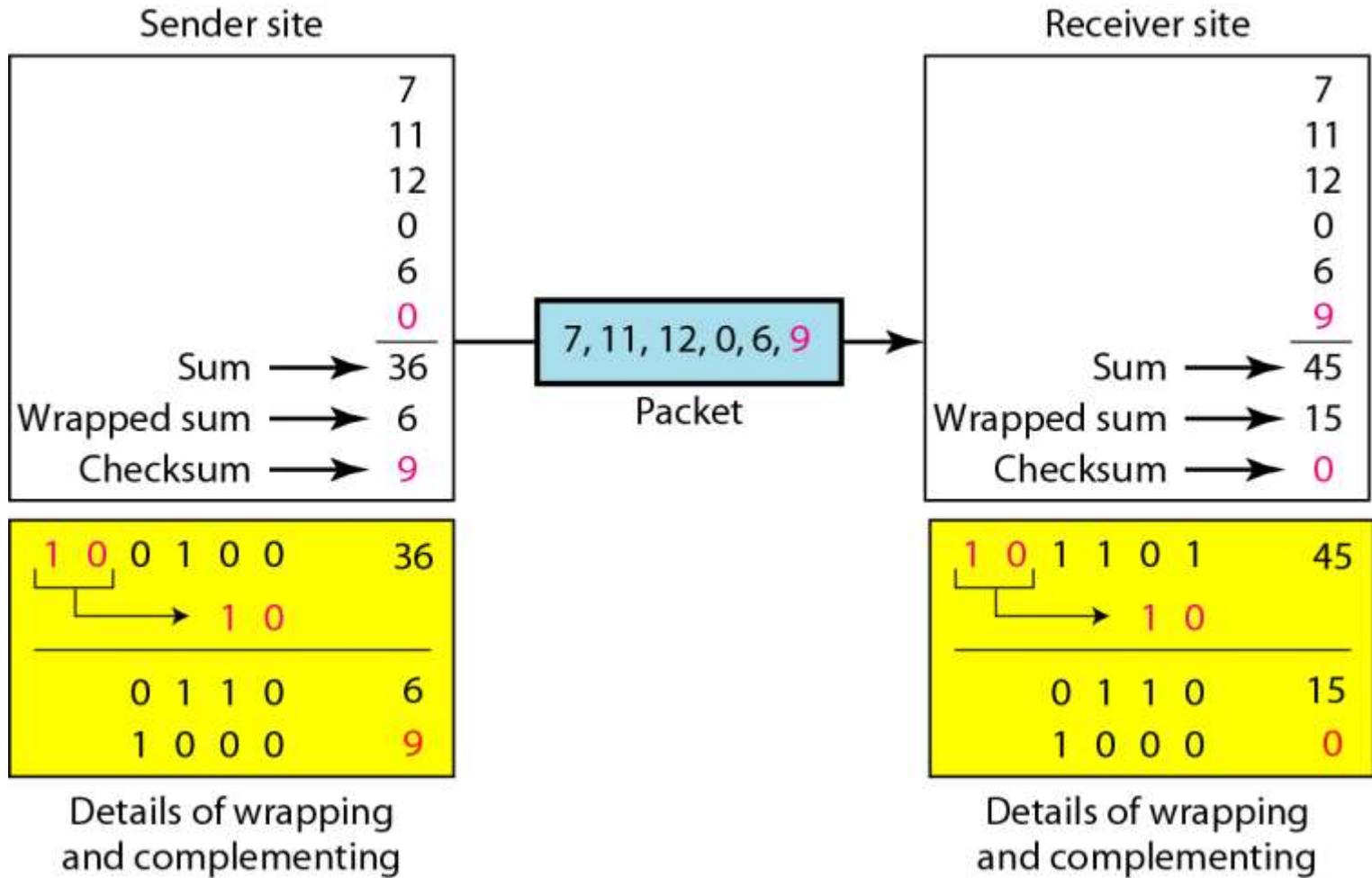
*Let us redo Exercise 10.19 using one's complement arithmetic. Figure 10.24 shows the process at the sender and at the receiver. The sender initializes the checksum to 0 and adds all data items and the checksum (the checksum is considered as one data item and is shown in color). The result is 36. However, 36 cannot be expressed in 4 bits. The extra two bits are wrapped and added with the sum to create the wrapped sum value 6. In the figure, we have shown the details in binary. The sum is then complemented, resulting in the checksum value 9 ( $15 - 6 = 9$ ). The sender now sends six data items to the receiver including the checksum 9.*

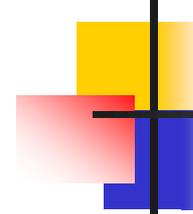


## *Example 10.22 (continued)*

*The receiver follows the same procedure as the sender. It adds all data items (including the checksum); the result is 45. The sum is wrapped and becomes 15. The wrapped sum is complemented and becomes 0. Since the value of the checksum is 0, this means that the data is not corrupted. The receiver drops the checksum and keeps the other data items. If the checksum is not zero, the entire packet is dropped.*

**Figure 10.24** *Example 10.22*

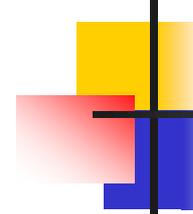




*Note*

## **Sender site:**

- 1. The message is divided into 16-bit words.**
- 2. The value of the checksum word is set to 0.**
- 3. All words including the checksum are added using one's complement addition.**
- 4. The sum is complemented and becomes the checksum.**
- 5. The checksum is sent with the data.**



*Note*

## Receiver site:

- 1.** The message (including checksum) is divided into 16-bit words.
- 2.** All words are added using one's complement addition.
- 3.** The sum is complemented and becomes the new checksum.
- 4.** If the value of checksum is 0, the message is accepted; otherwise, it is rejected.

## Example 10.23

*Let us calculate the checksum for a text of 8 characters (“Forouzan”). The text needs to be divided into 2-byte (16-bit) words. We use ASCII (see Appendix A) to change each byte to a 2-digit hexadecimal number. For example, F is represented as 0x46 and o is represented as 0x6F. Figure 10.25 shows how the checksum is calculated at the sender and receiver sites. In part a of the figure, the value of partial sum for the first column is 0x36. We keep the rightmost digit (6) and insert the leftmost digit (3) as the carry in the second column. The process is repeated for each column. Note that if there is any corruption, the checksum recalculated by the receiver is not all 0s. We leave this an exercise.*

**Figure 10.25** *Example 10.23*

1	0	1	3	Carries	
4	6	6	F	(Fo)	
7	2	6	7	(ro)	
7	5	7	A	(uz)	
6	1	6	E	(an)	
0	0	0	0		Checksum (initial)
8	F	C	6		Sum (partial)
8	F	C	7		Sum
7	0	3	8		Checksum (to send)

a. Checksum at the sender site

1	0	1	3	Carries	
4	6	6	F	(Fo)	
7	2	6	7	(ro)	
7	5	7	A	(uz)	
6	1	6	E	(an)	
7	0	3	8		Checksum (received)
F	F	F	E		Sum (partial)
8	F	C	7		Sum
0	0	0	0		Checksum (new)

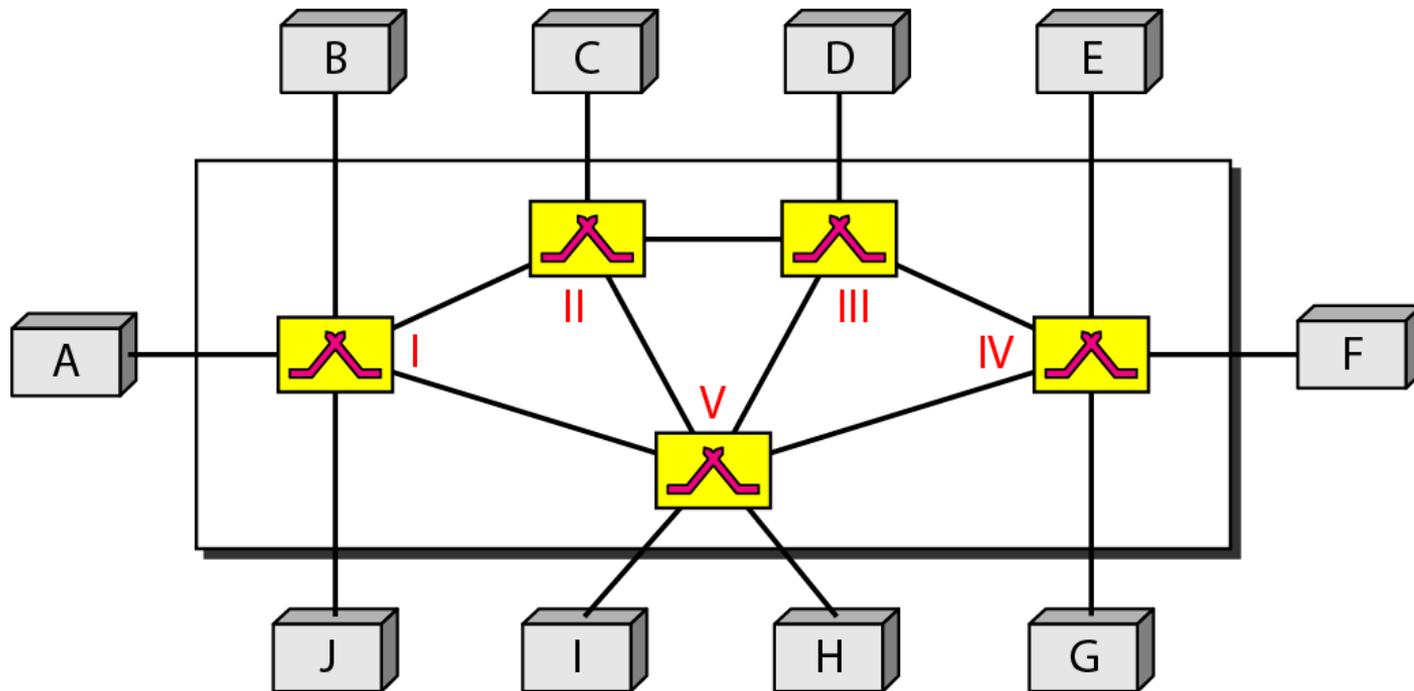
a. Checksum at the receiver site



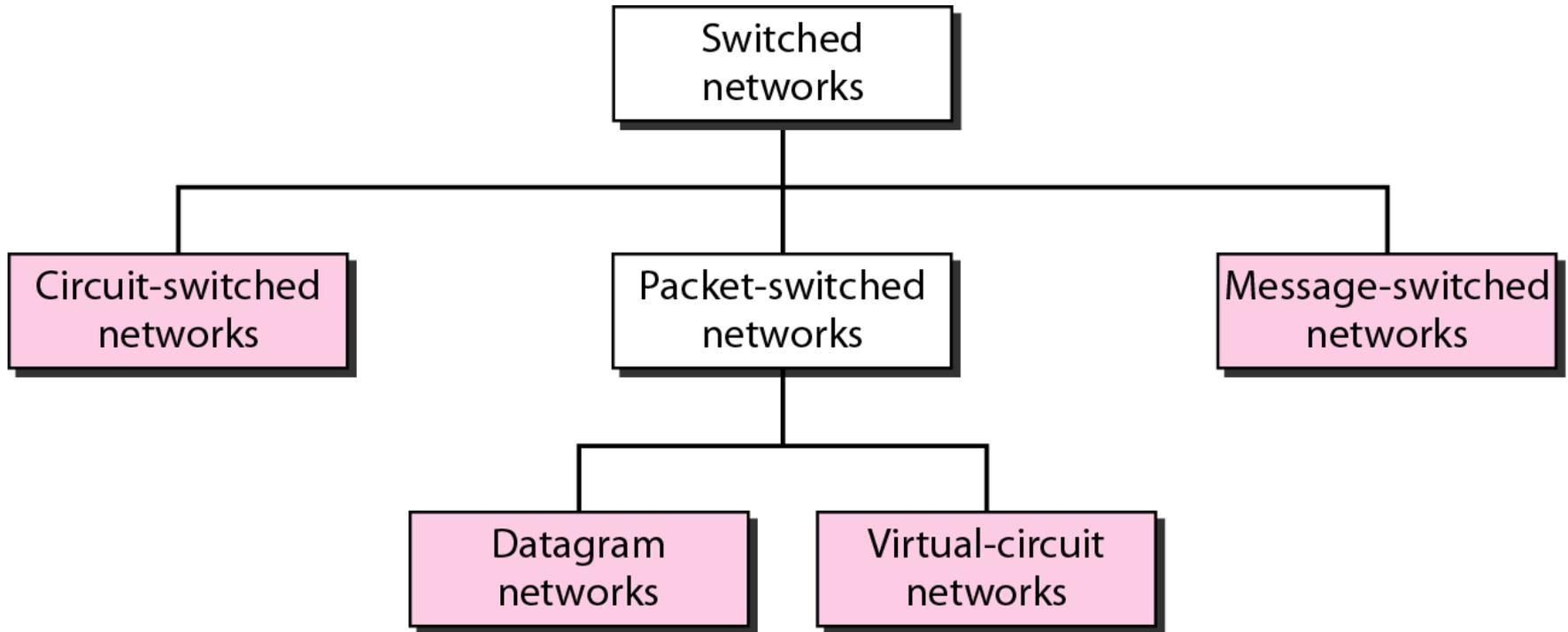
# Chapter 8

# Switching

**Figure 8.1** *Switched network*



**Figure 8.2** *Taxonomy of switched networks*



# 8-1 CIRCUIT-SWITCHED NETWORKS

*A circuit-switched network consists of a set of switches connected by physical links. A connection between two stations is a dedicated path made of one or more links. However, each connection uses only one dedicated channel on each link. Each link is normally divided into  $n$  channels by using FDM or TDM.*

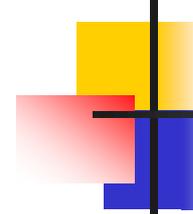
## Topics discussed in this section:

Three Phases

Efficiency

Delay

Circuit-Switched Technology in Telephone Networks

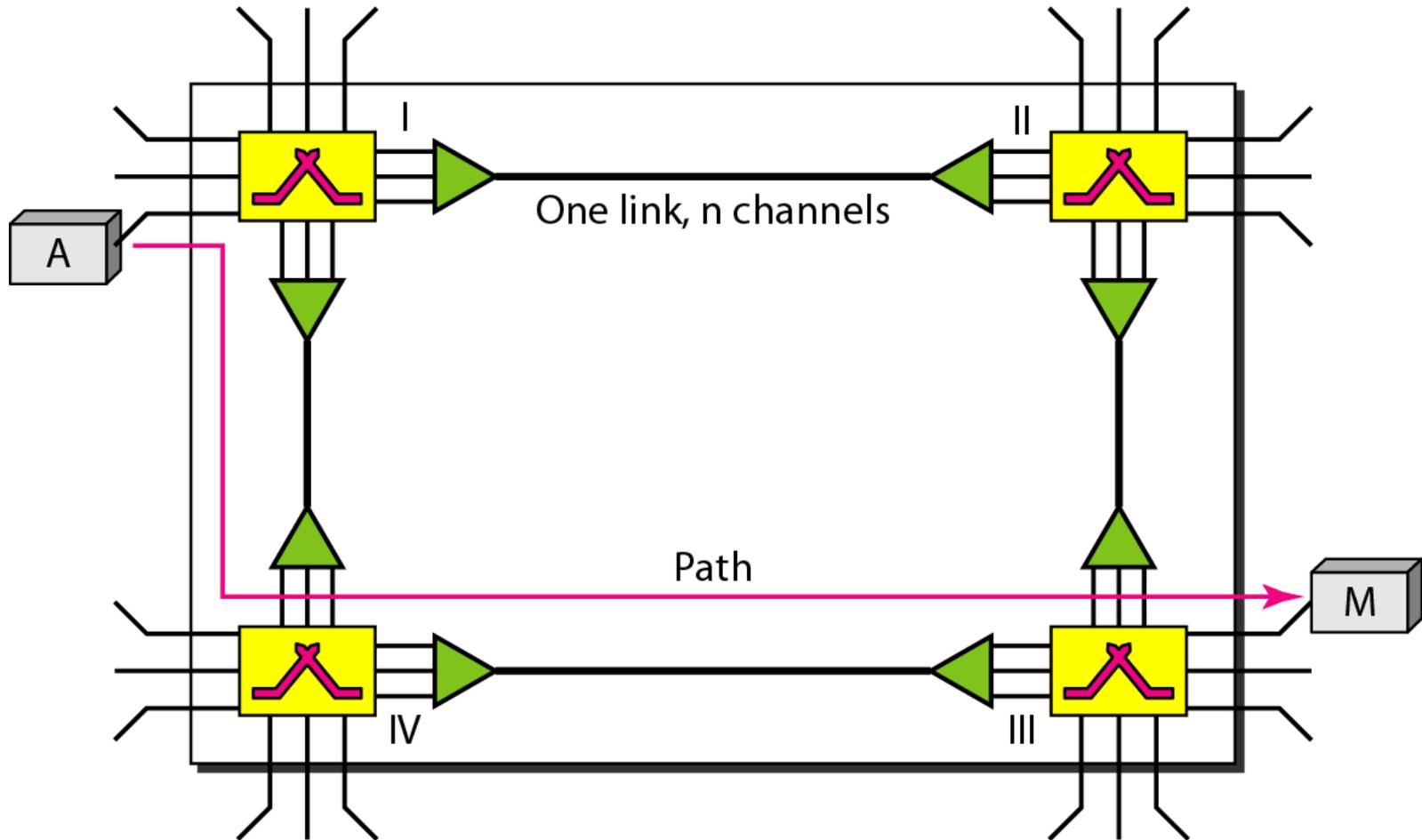


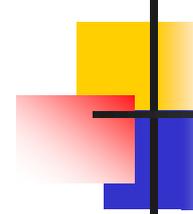
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*Note*

**A circuit-switched network is made of a set of switches connected by physical links, in which each link is divided into  $n$  channels.**

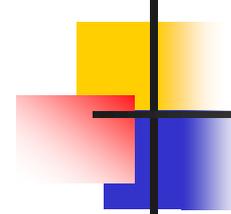
**Figure 8.3** *A trivial circuit-switched network*





*Note*

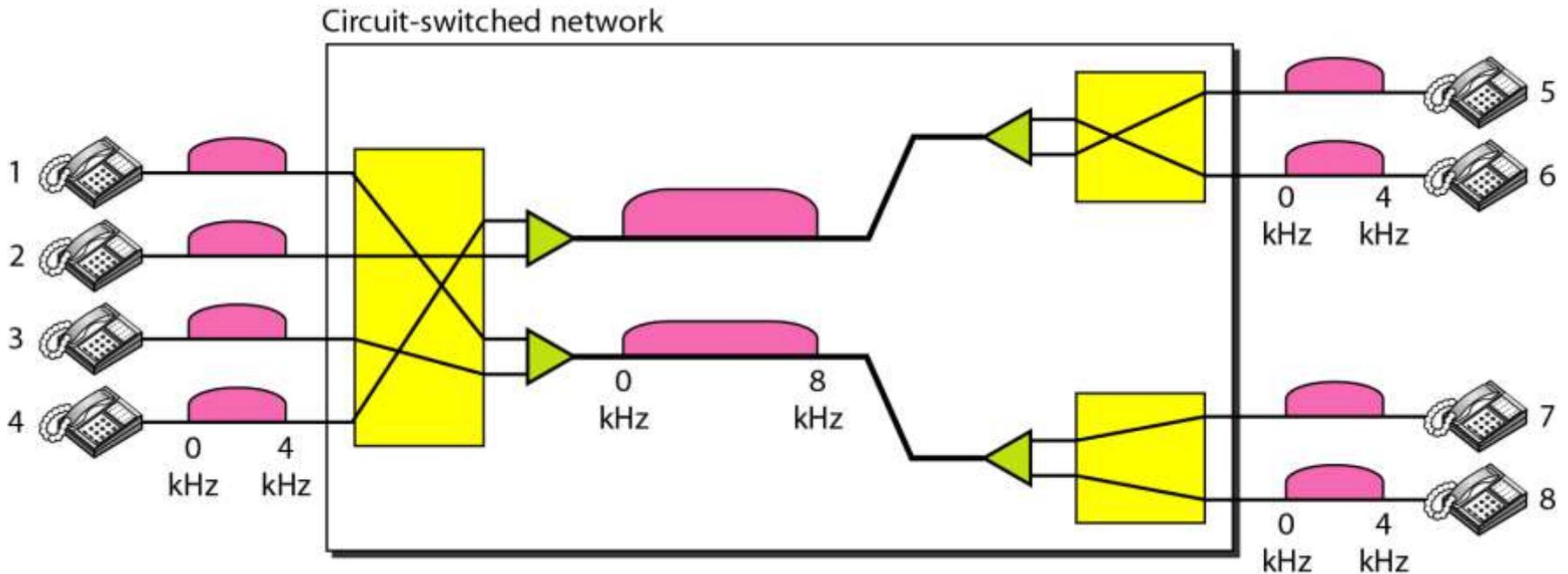
**In circuit switching, the resources need to be reserved during the setup phase; the resources remain dedicated for the entire duration of data transfer until the teardown phase.**

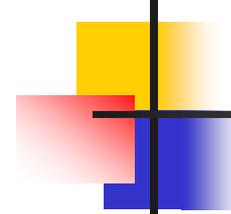


## *Example 8.1*

*As a trivial example, let us use a circuit-switched network to connect eight telephones in a small area. Communication is through 4-kHz voice channels. We assume that each link uses FDM to connect a maximum of two voice channels. The bandwidth of each link is then 8 kHz. Figure 8.4 shows the situation. Telephone 1 is connected to telephone 7; 2 to 5; 3 to 8; and 4 to 6. Of course the situation may change when new connections are made. The switch controls the connections.*

**Figure 8.4** *Circuit-switched network used in Example 8.1*

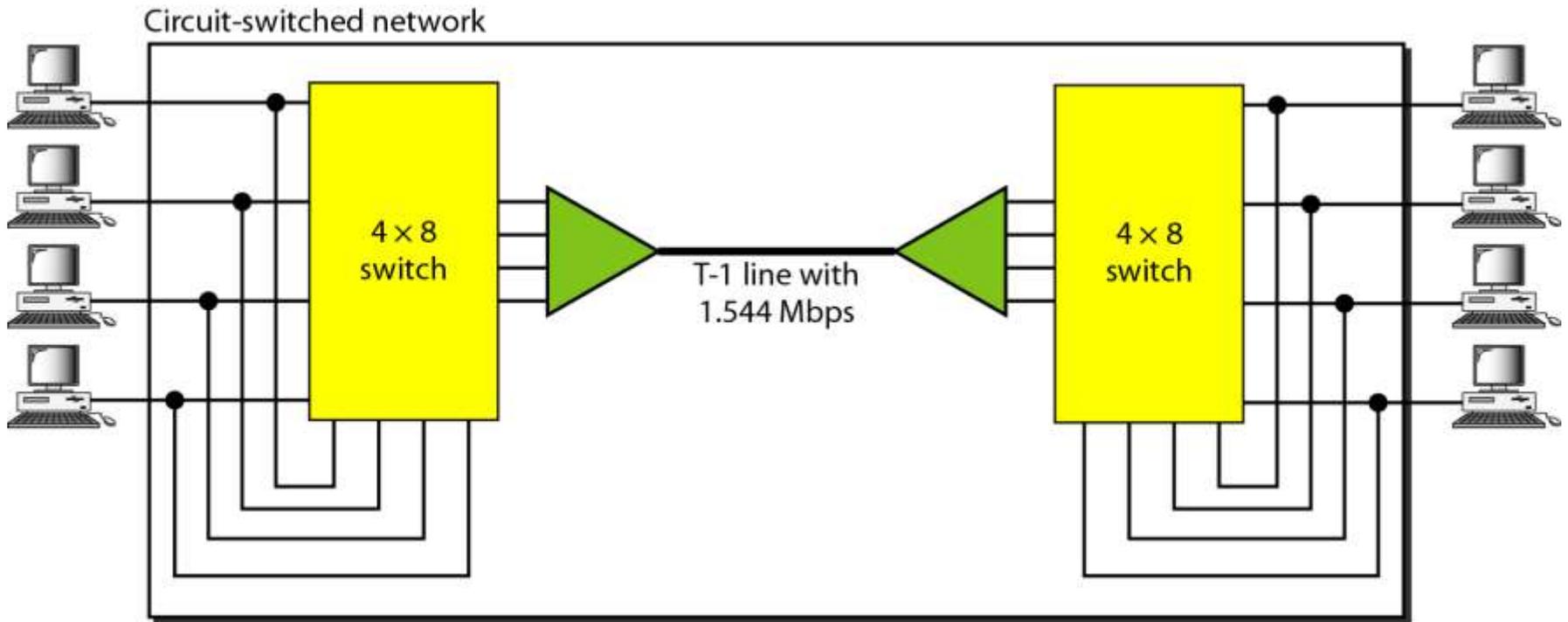




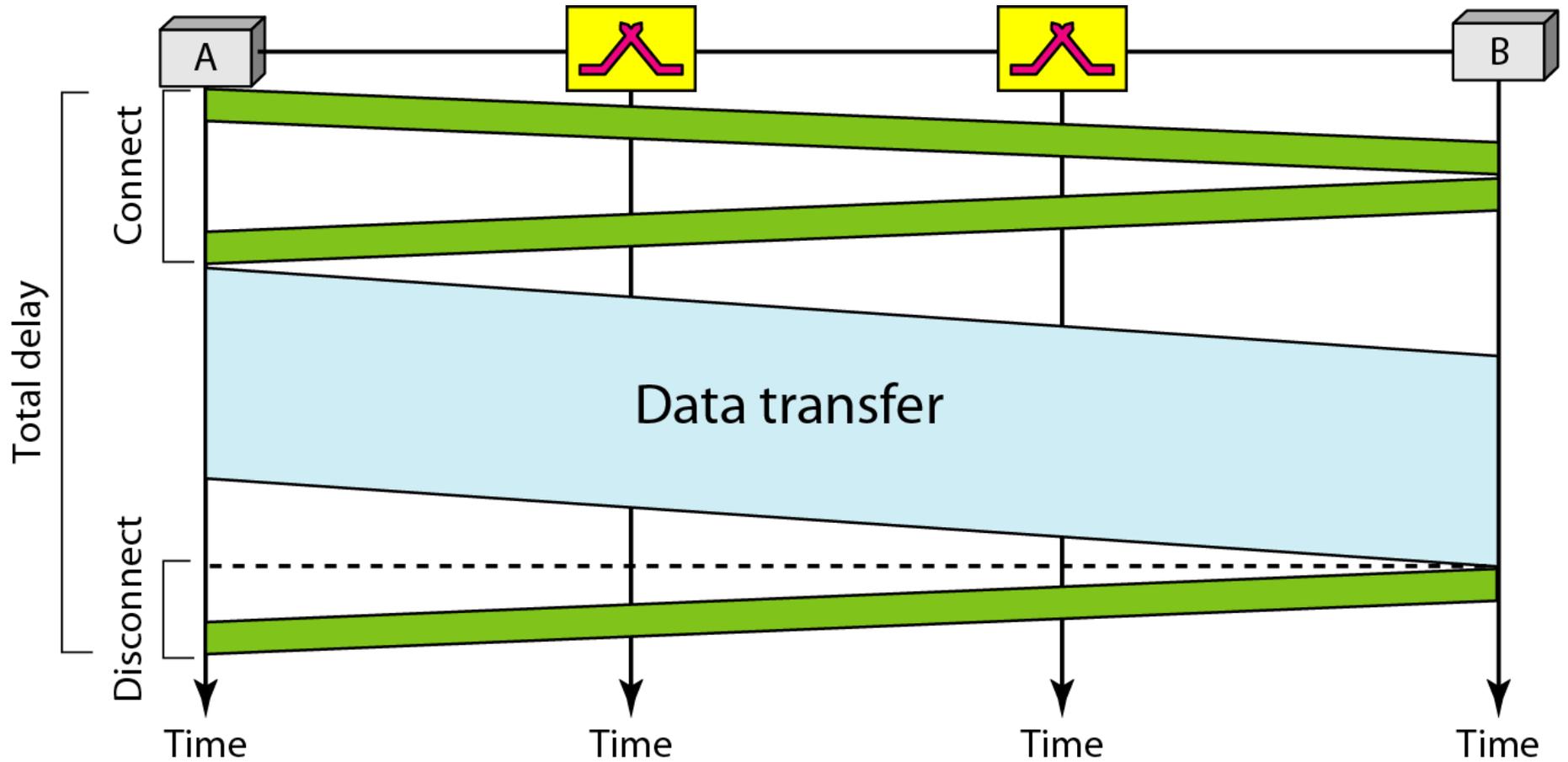
## *Example 8.2*

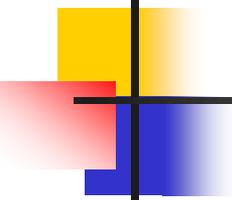
*As another example, consider a circuit-switched network that connects computers in two remote offices of a private company. The offices are connected using a T-1 line leased from a communication service provider. There are two  $4 \times 8$  (4 inputs and 8 outputs) switches in this network. For each switch, four output ports are folded into the input ports to allow communication between computers in the same office. Four other output ports allow communication between the two offices. Figure 8.5 shows the situation.*

**Figure 8.5** *Circuit-switched network used in Example 8.2*



**Figure 8.6** *Delay in a circuit-switched network*





---

*Note*

**Switching at the physical layer in the traditional telephone network uses the circuit-switching approach.**

## 8-2 DATAGRAM NETWORKS

*In data communications, we need to send messages from one end system to another. If the message is going to pass through a packet-switched network, it needs to be divided into packets of fixed or variable size. The size of the packet is determined by the network and the governing protocol.*

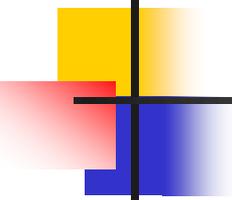
### *Topics discussed in this section:*

**Routing Table**

**Efficiency**

**Delay**

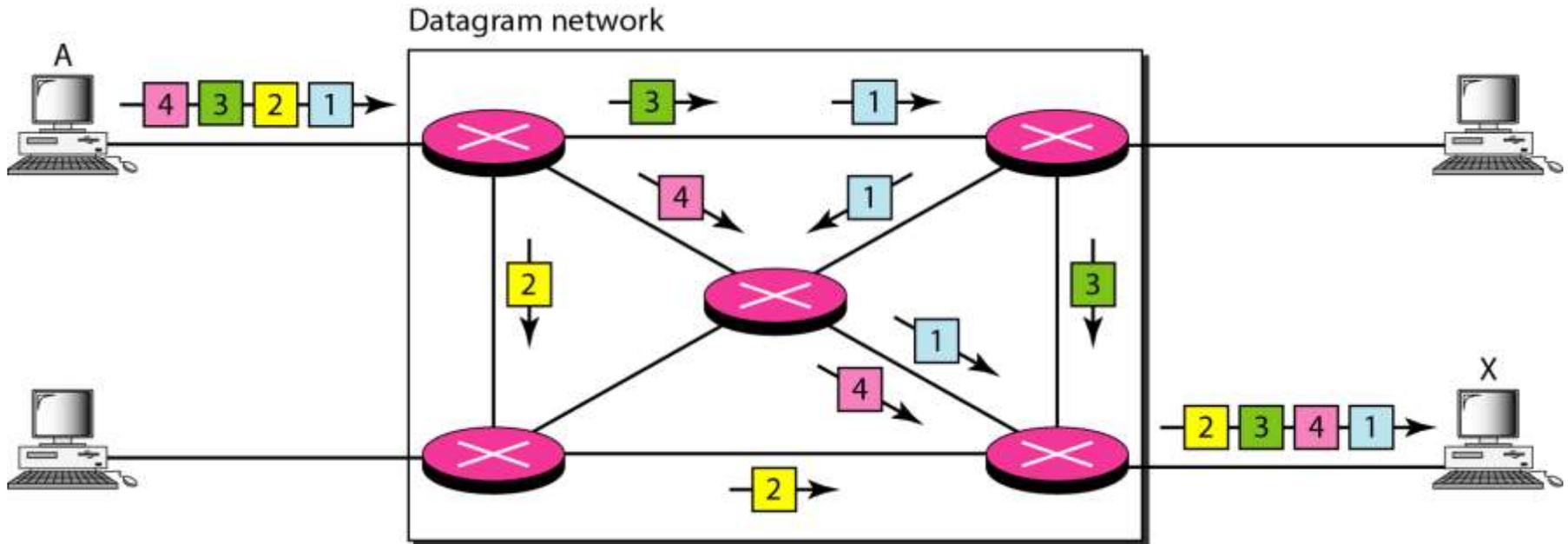
**Datagram Networks in the Internet**



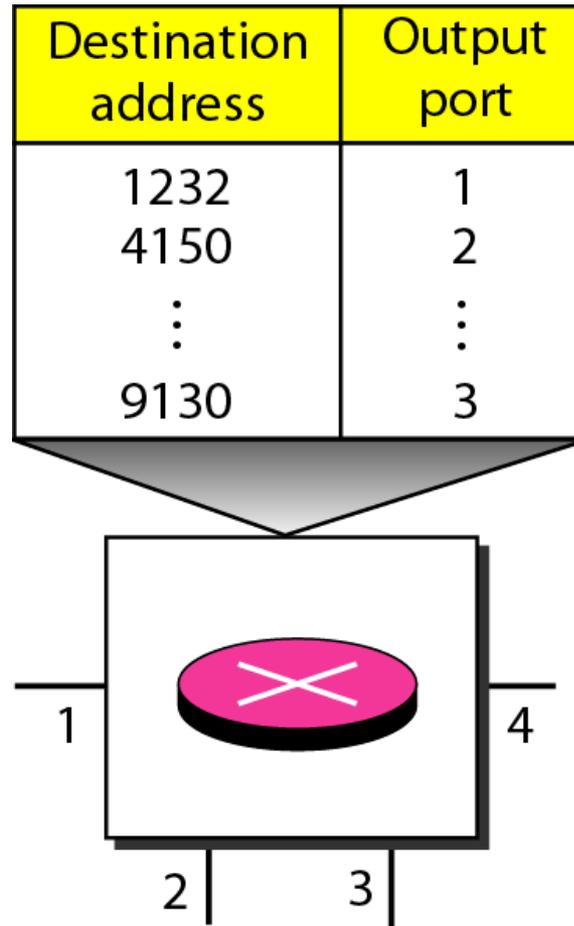
*Note*

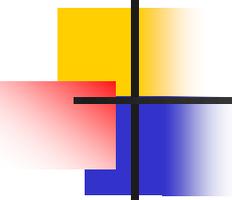
**In a packet-switched network, there is no resource reservation; resources are allocated on demand.**

**Figure 8.7** *A datagram network with four switches (routers)*



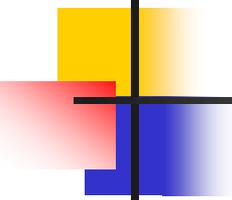
**Figure 8.8** *Routing table in a datagram network*





*Note*

**A switch in a datagram network uses a routing table that is based on the destination address.**

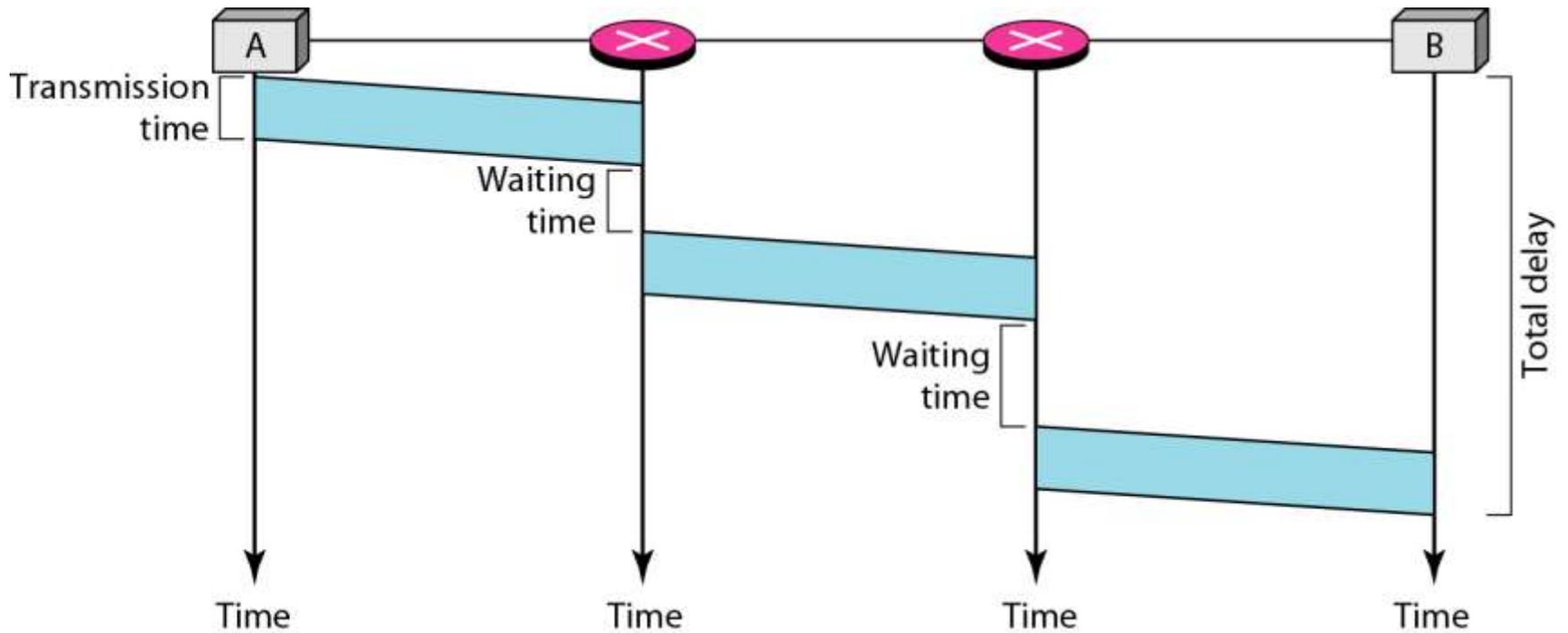


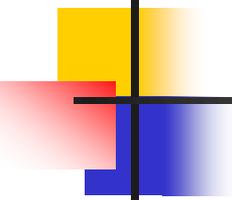
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*Note*

**The destination address in the header of a packet in a datagram network remains the same during the entire journey of the packet.**

**Figure 8.9** *Delay in a datagram network*





*Note*

**Switching in the Internet is done by using the datagram approach to packet switching at the network layer.**

## 8-3 VIRTUAL-CIRCUIT NETWORKS

*A virtual-circuit network is a cross between a circuit-switched network and a datagram network. It has some characteristics of both.*

### *Topics discussed in this section:*

Addressing

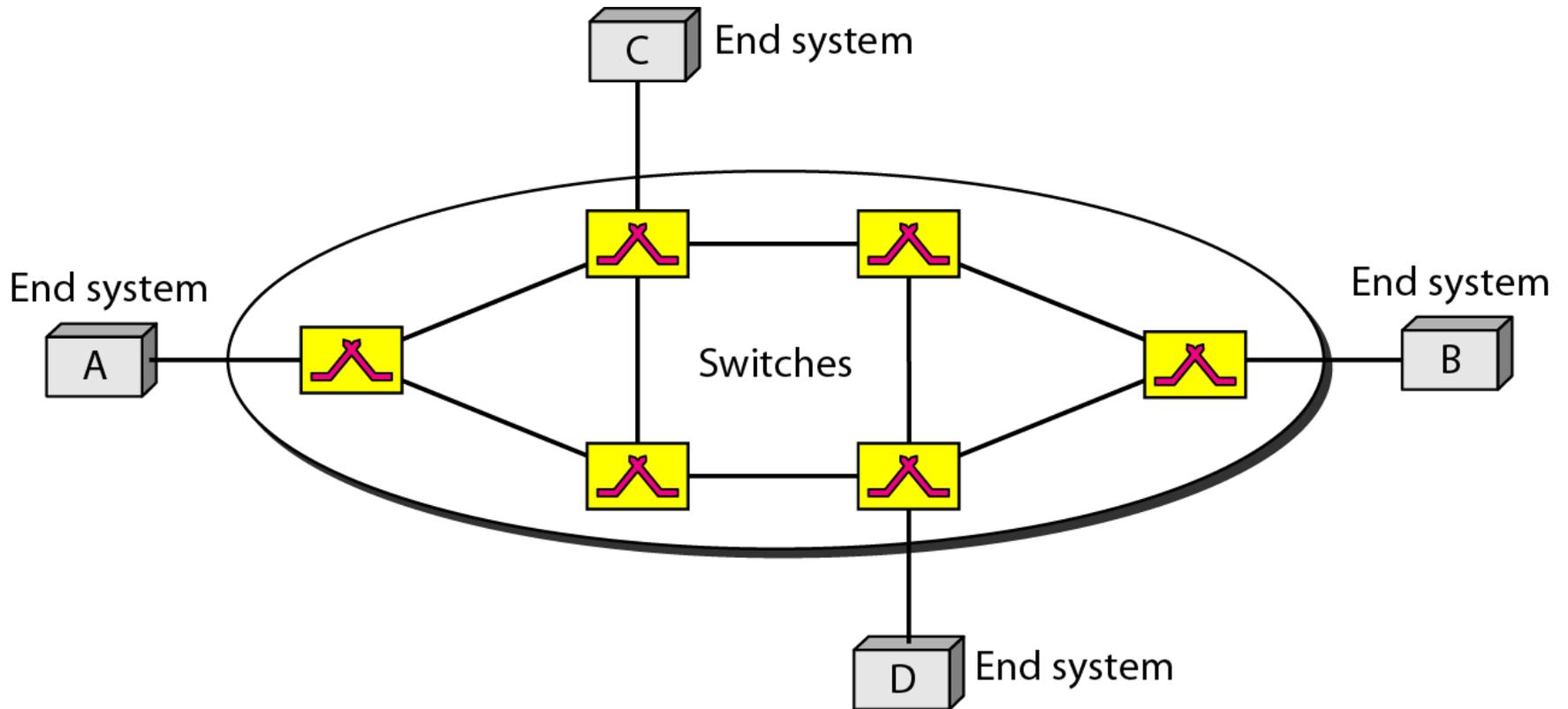
Three Phases

Efficiency

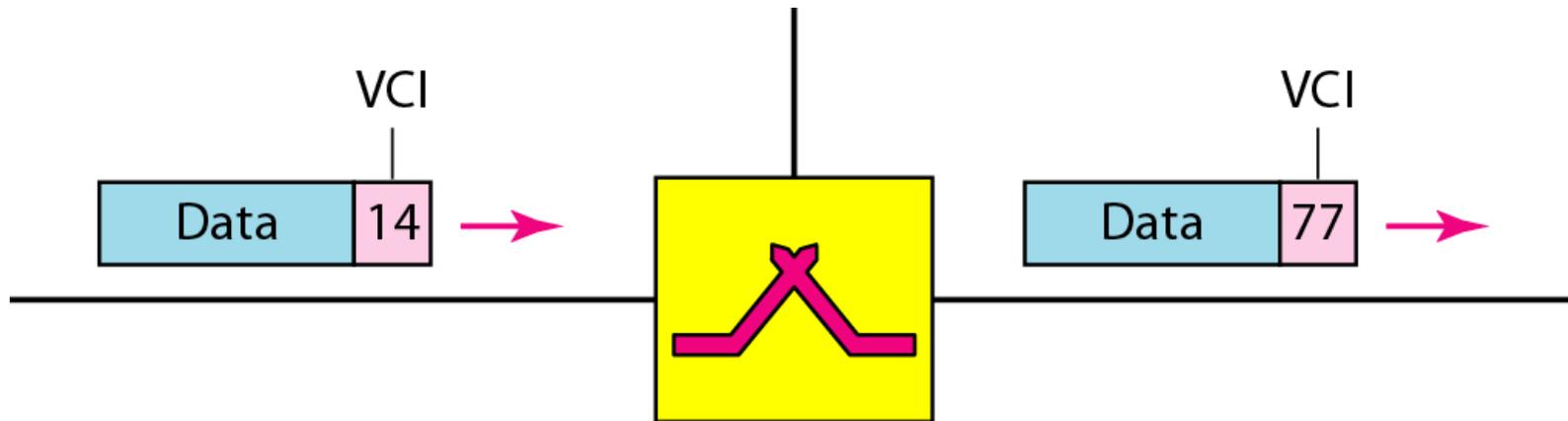
Delay

Circuit-Switched Technology in WANs

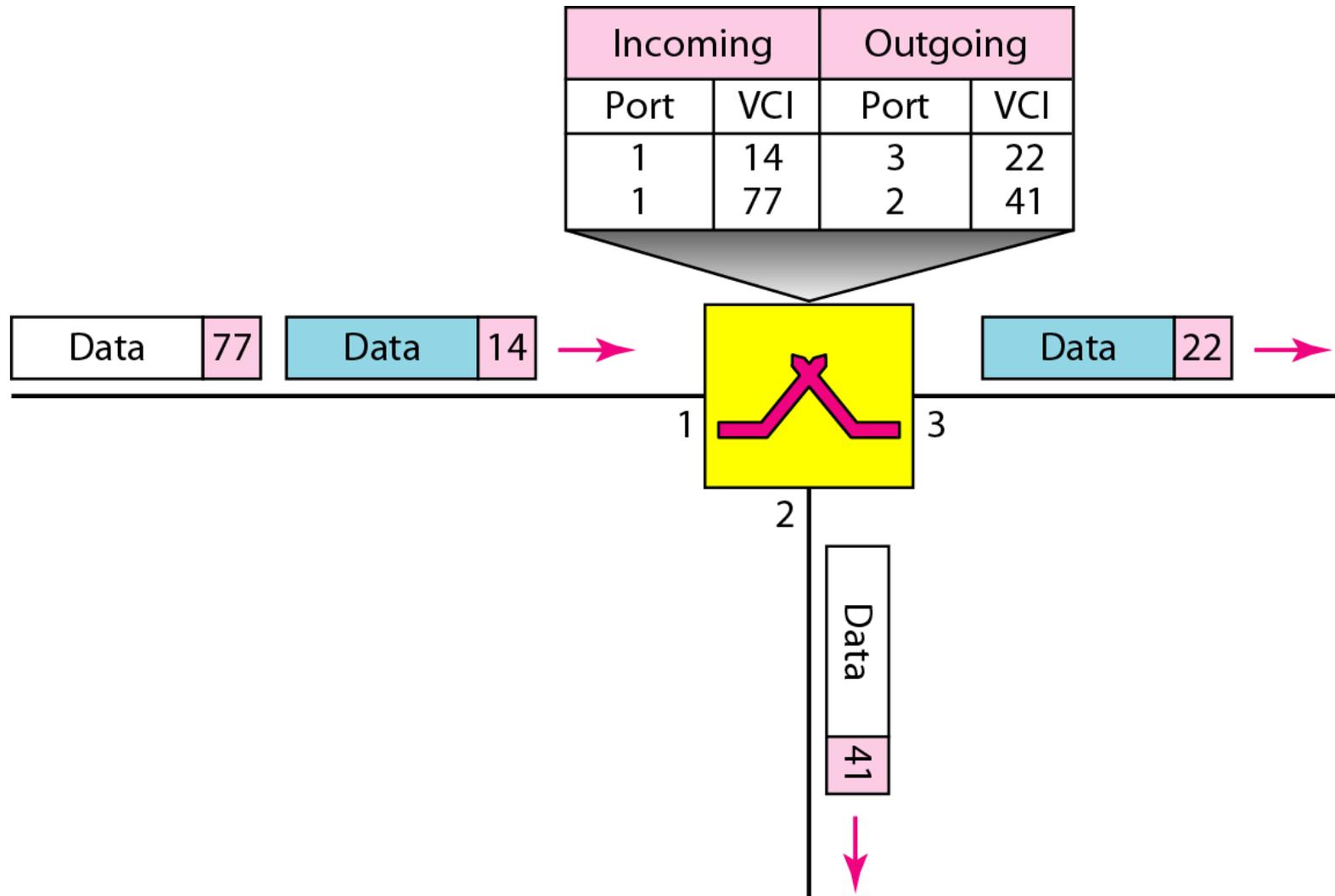
**Figure 8.10** *Virtual-circuit network*



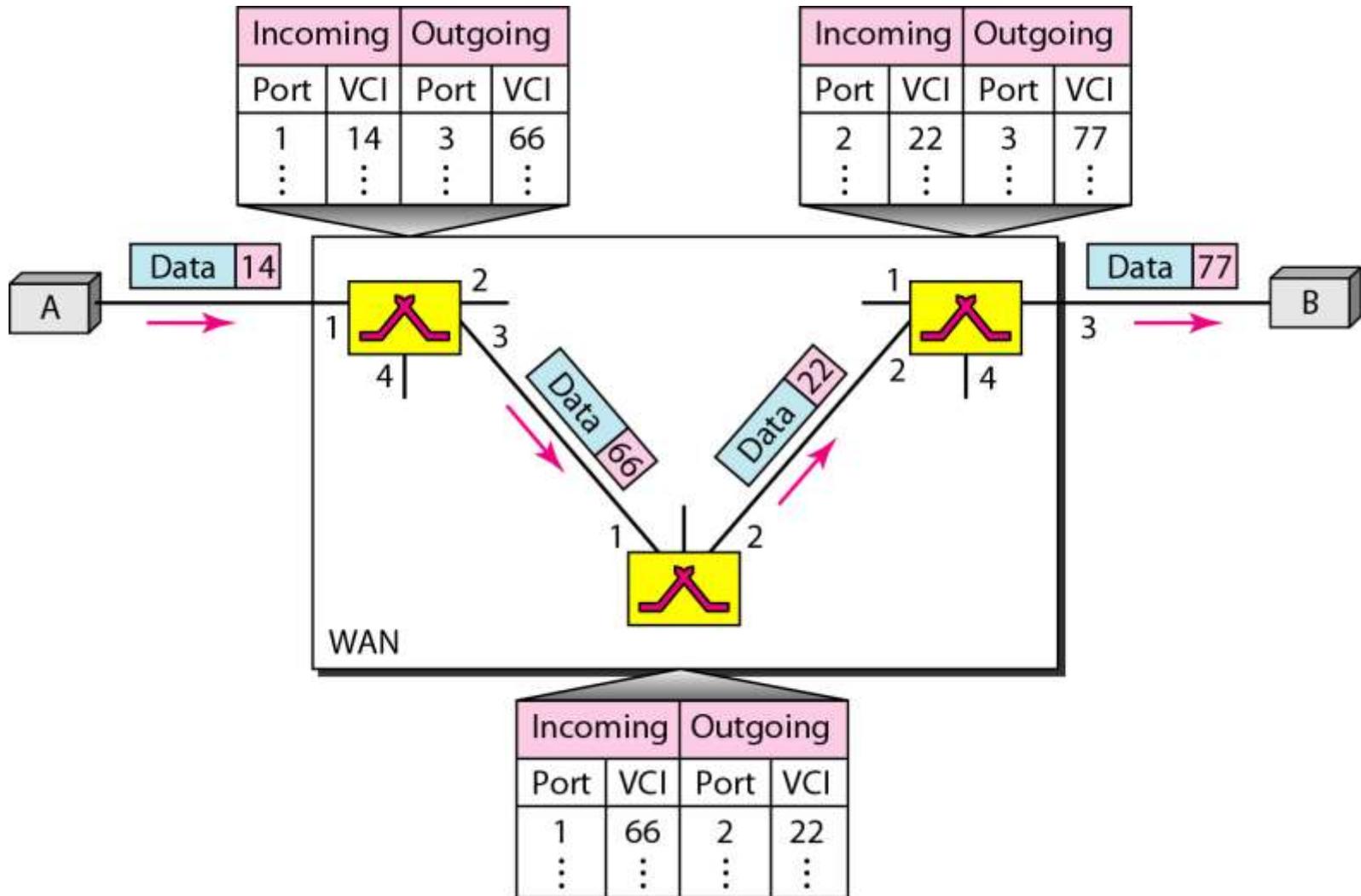
**Figure 8.11** *Virtual-circuit identifier*



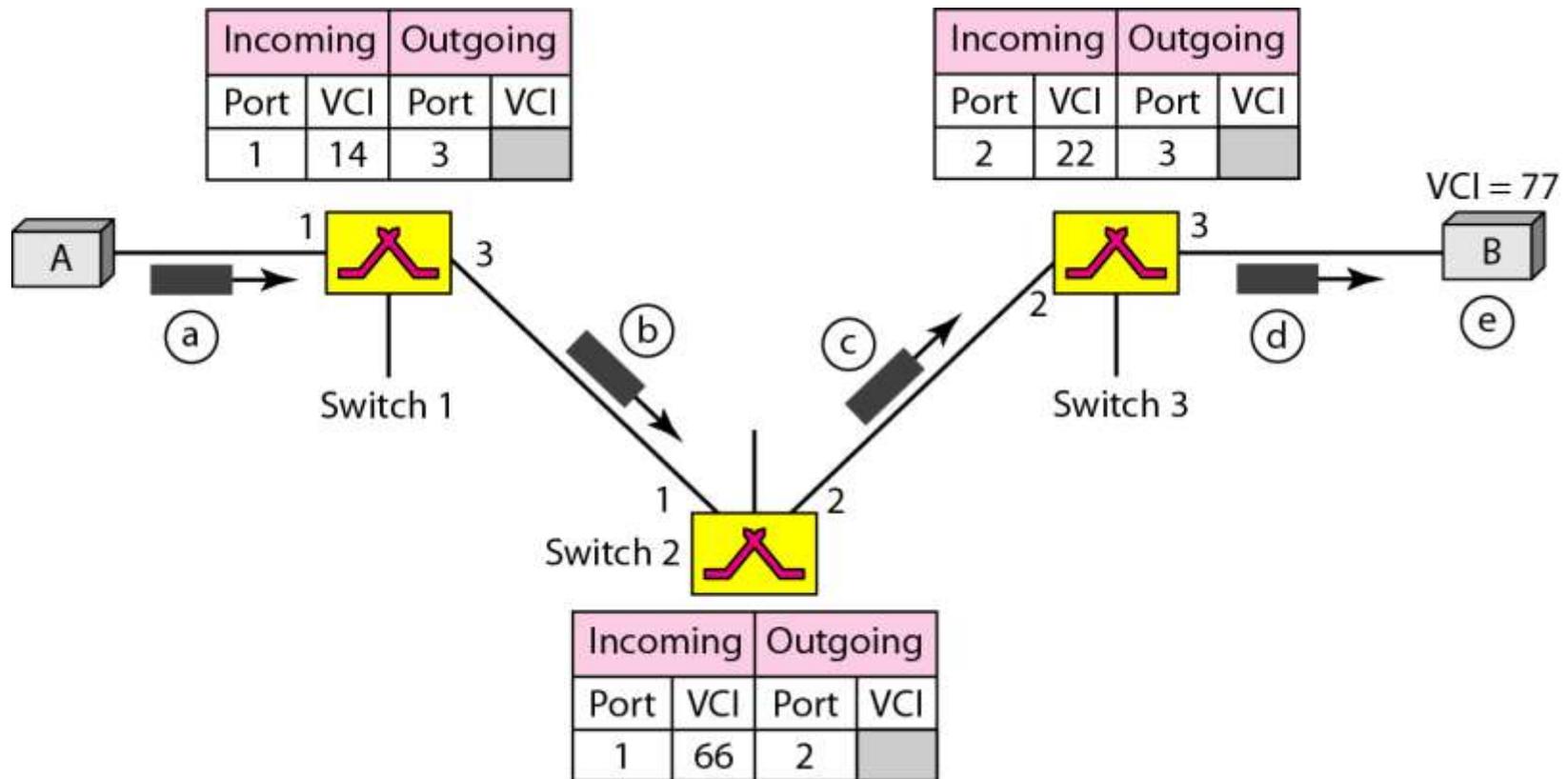
**Figure 8.12** *Switch and tables in a virtual-circuit network*



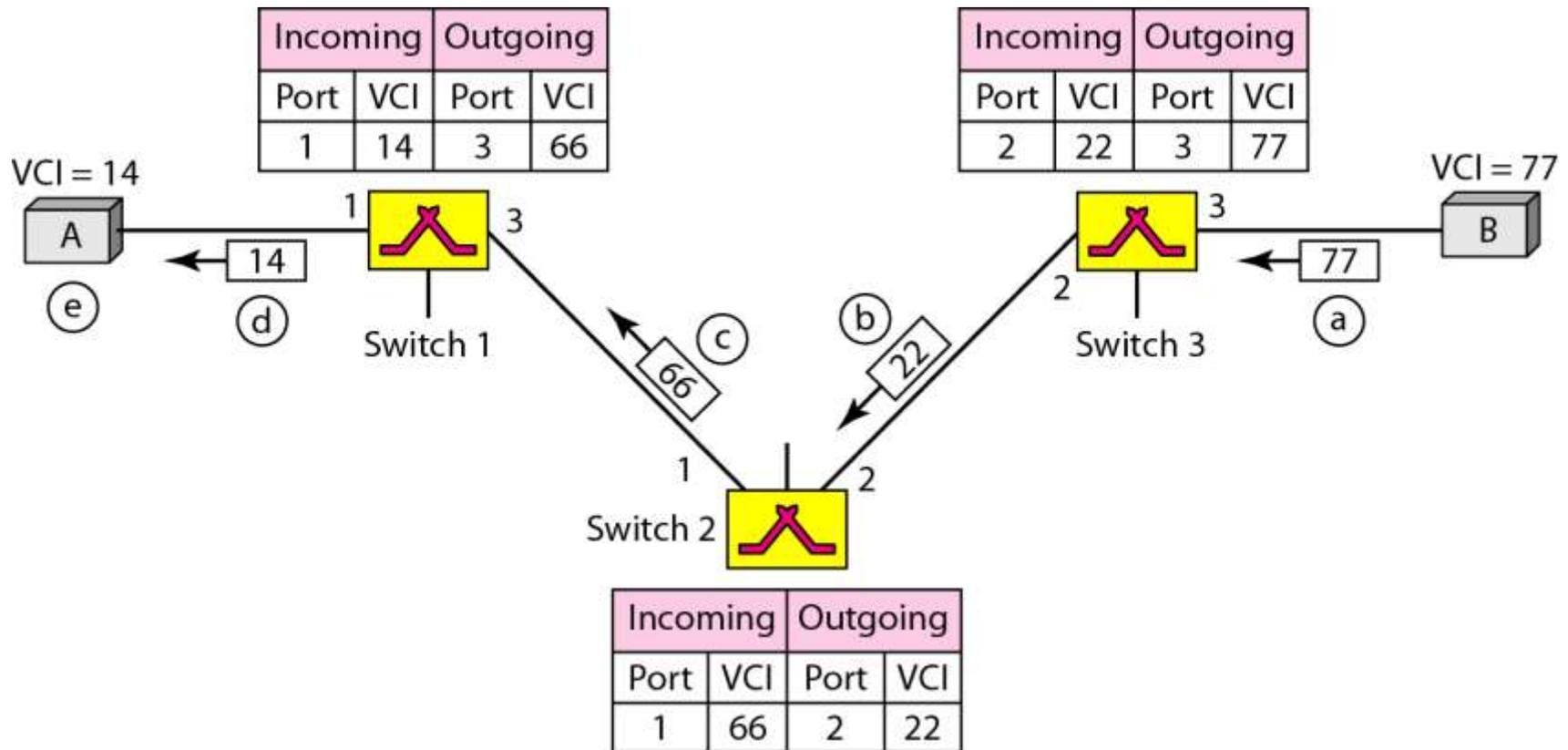
**Figure 8.13** *Source-to-destination data transfer in a virtual-circuit network*

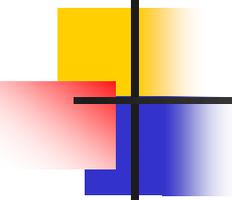


**Figure 8.14** *Setup request in a virtual-circuit network*



**Figure 8.15** *Setup acknowledgment in a virtual-circuit network*

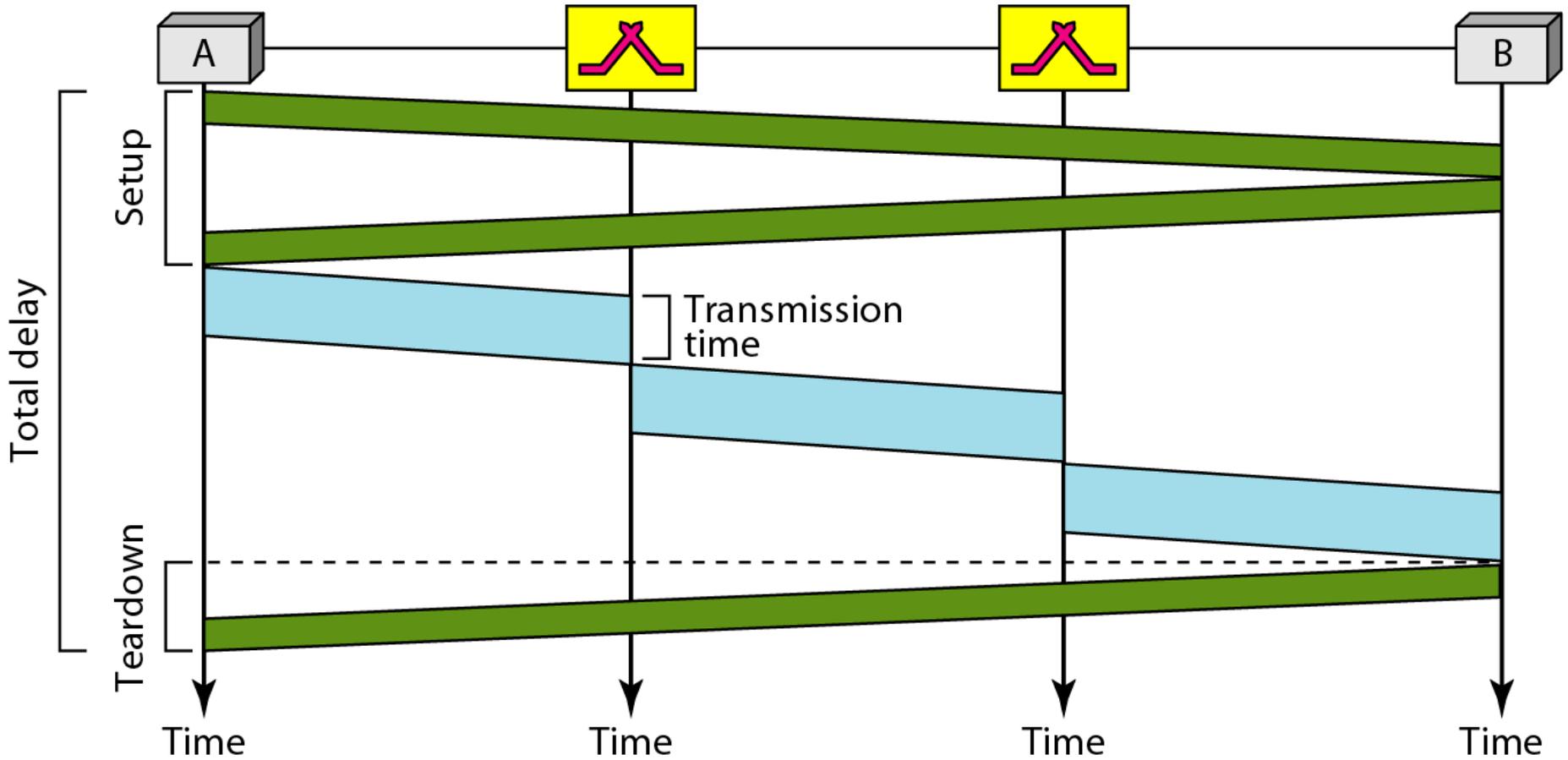


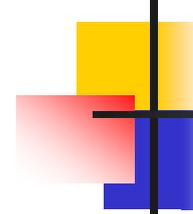


*Note*

**In virtual-circuit switching, all packets belonging to the same source and destination travel the same path; but the packets may arrive at the destination with different delays if resource allocation is on demand.**

**Figure 8.16** *Delay in a virtual-circuit network*





*Note*

**Switching at the data link layer in a switched WAN is normally implemented by using virtual-circuit techniques.**

## 8-4 STRUCTURE OF A SWITCH

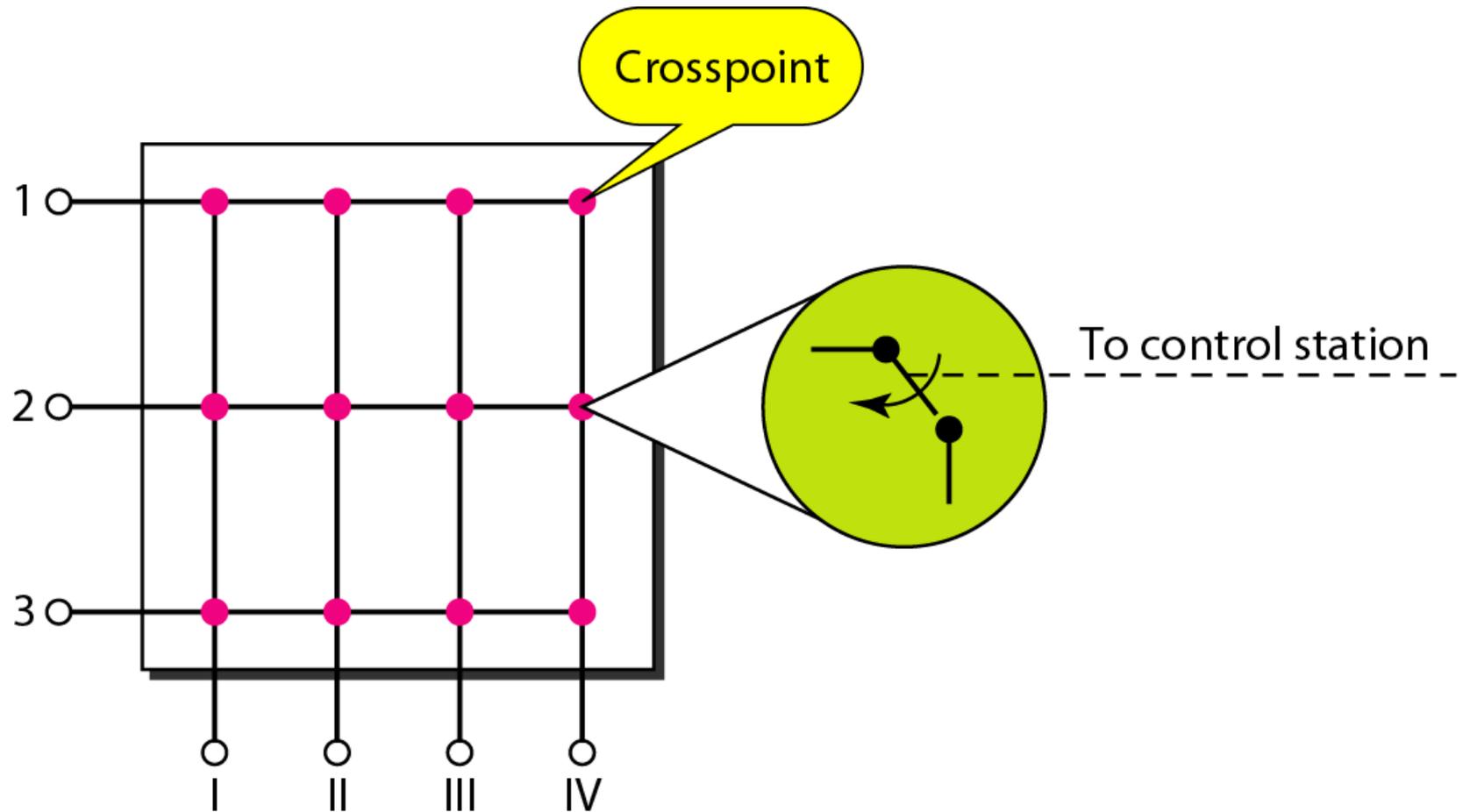
*We use switches in circuit-switched and packet-switched networks. In this section, we discuss the structures of the switches used in each type of network.*

**Topics discussed in this section:**

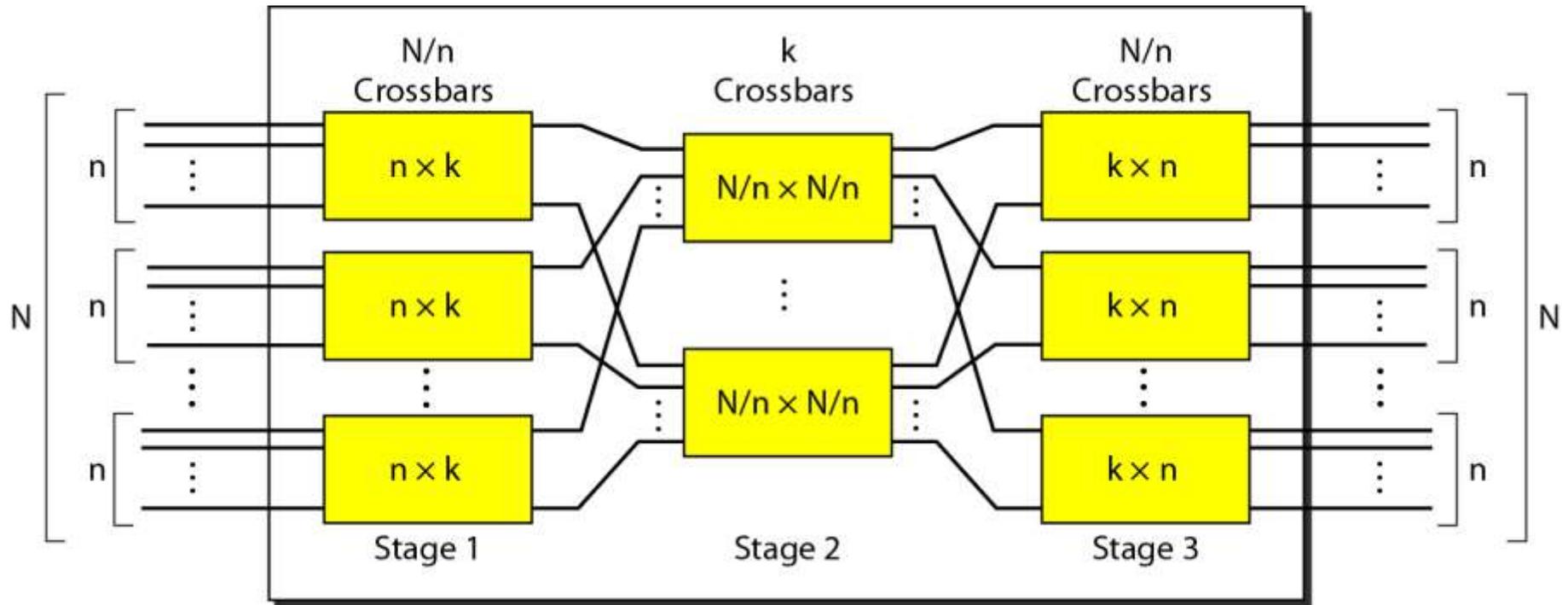
**Structure of Circuit Switches**

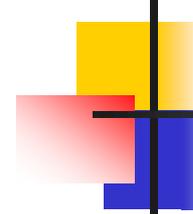
**Structure of Packet Switches**

**Figure 8.17** *Crossbar switch with three inputs and four outputs*



**Figure 8.18** *Multistage switch*



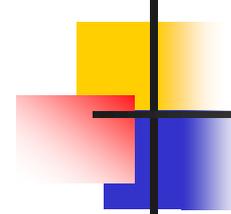


*Note*

**In a three-stage switch, the total number of crosspoints is**

$$2kN + k(N/n)^2$$

**which is much smaller than the number of crosspoints in a single-stage switch ( $N^2$ ).**

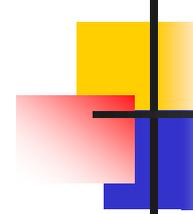


## Example 8.3

*Design a three-stage,  $200 \times 200$  switch ( $N = 200$ ) with  $k = 4$  and  $n = 20$ .*

### *Solution*

*In the first stage we have  $N/n$  or 10 crossbars, each of size  $20 \times 4$ . In the second stage, we have 4 crossbars, each of size  $10 \times 10$ . In the third stage, we have 10 crossbars, each of size  $4 \times 20$ . The total number of crosspoints is  $2kN + k(N/n)^2$ , or **2000** crosspoints. This is 5 percent of the number of crosspoints in a single-stage switch ( $200 \times 200 = 40,000$ ).*



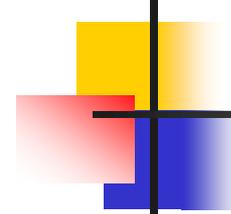
*Note*

**According to the Clos criterion:**

$$n = (N/2)^{1/2}$$

$$k > 2n - 1$$

$$\text{Crosspoints} \geq 4N [(2N)^{1/2} - 1]$$



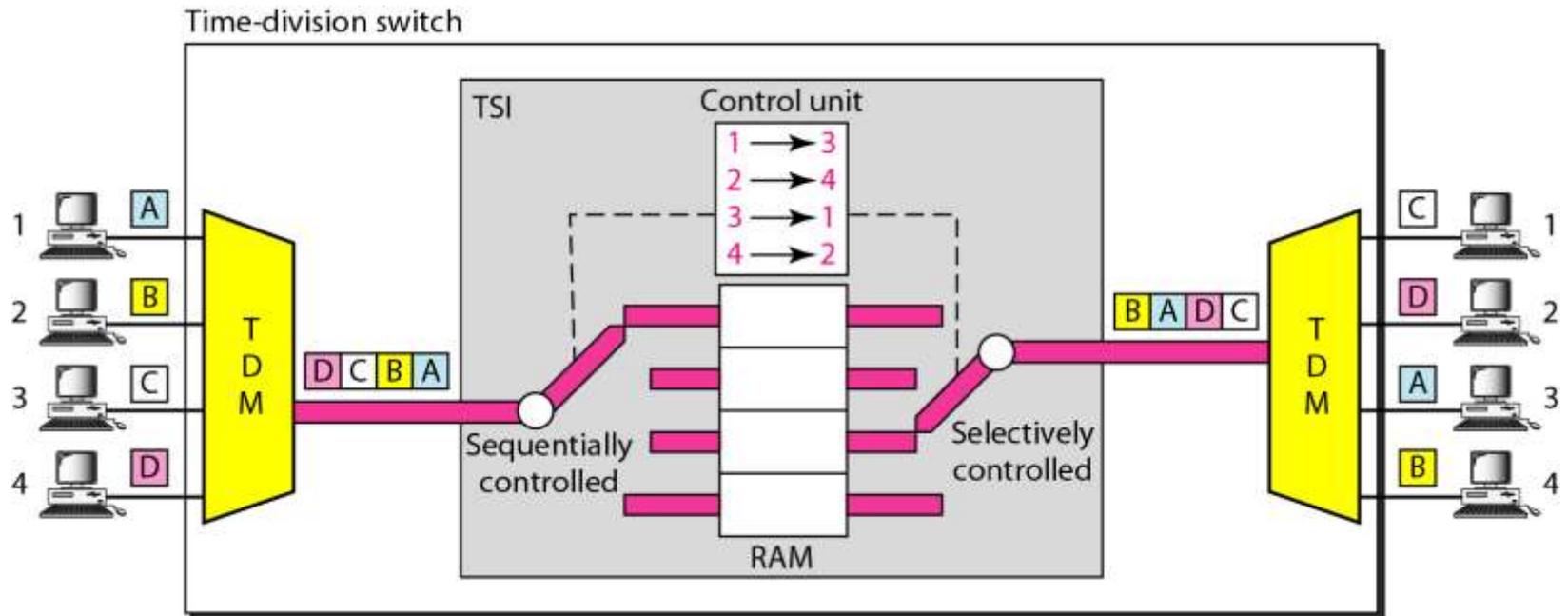
## *Example 8.4*

*Redesign the previous three-stage,  $200 \times 200$  switch, using the Clos criteria with a minimum number of crosspoints.*

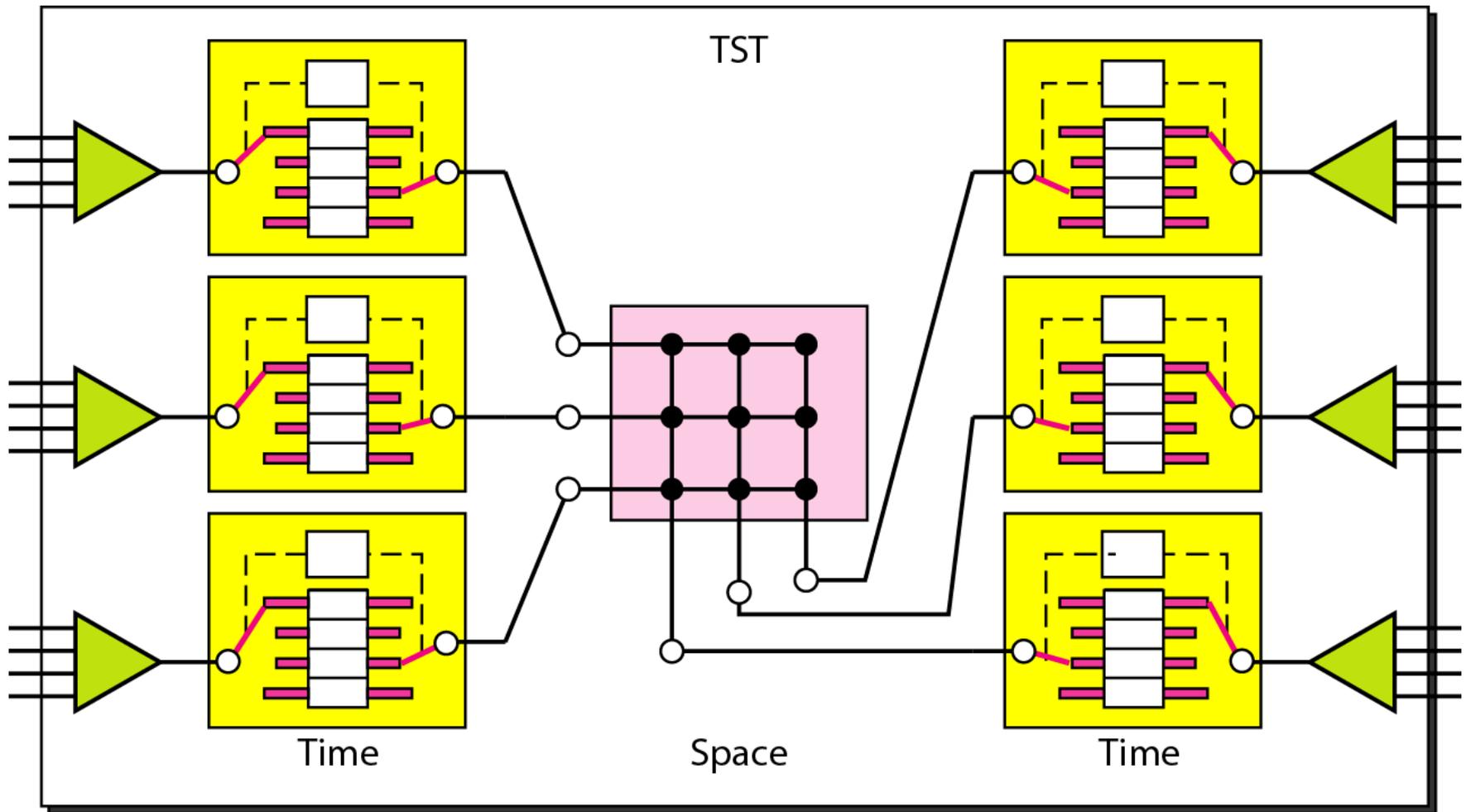
### *Solution*

*We let  $n = (200/2)^{1/2}$ , or  $n = 10$ . We calculate  $k = 2n - 1 = 19$ . In the first stage, we have  $200/10$ , or 20, crossbars, each with  $10 \times 19$  crosspoints. In the second stage, we have 19 crossbars, each with  $10 \times 10$  crosspoints. In the third stage, we have 20 crossbars each with  $19 \times 10$  crosspoints. The total number of crosspoints is  $20(10 \times 19) + 19(10 \times 10) + 20(19 \times 10) = 9500$ .*

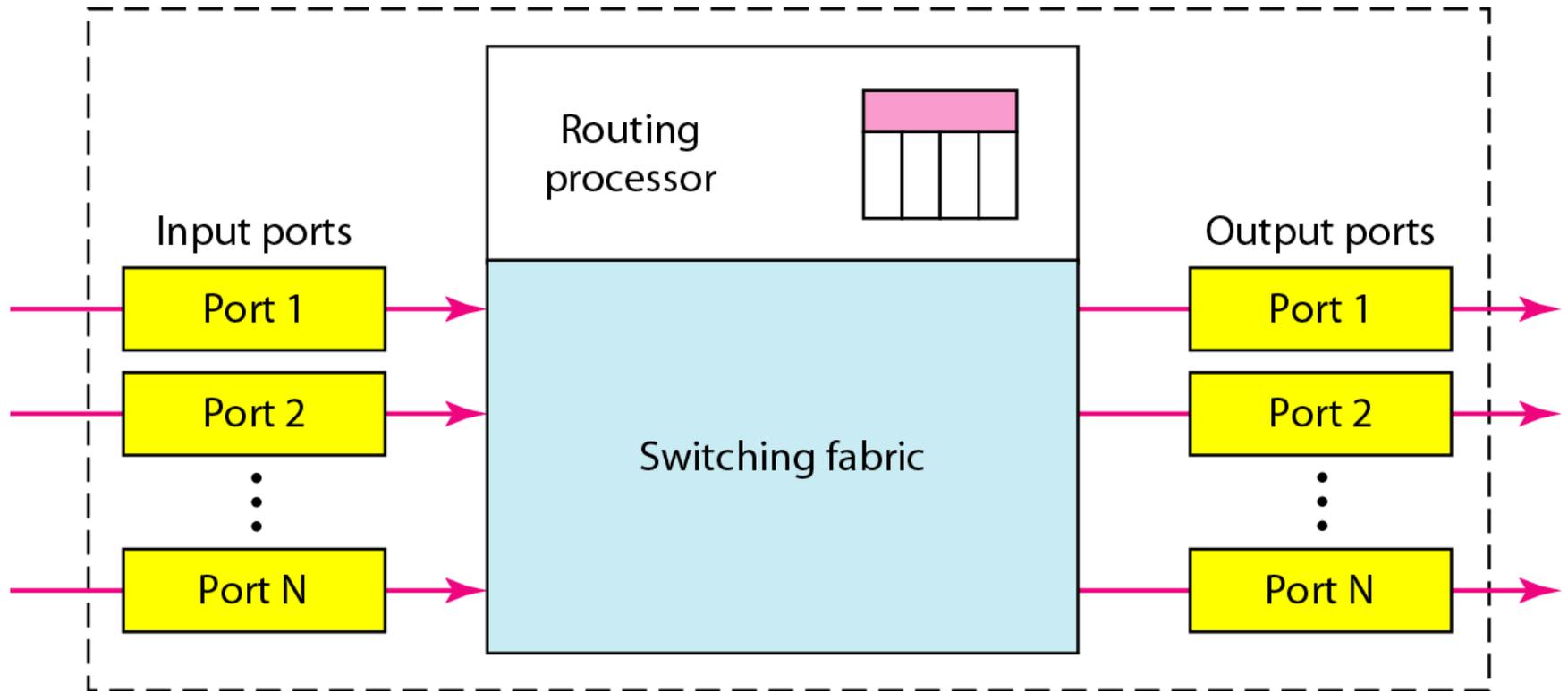
**Figure 8.19** *Time-slot interchange*



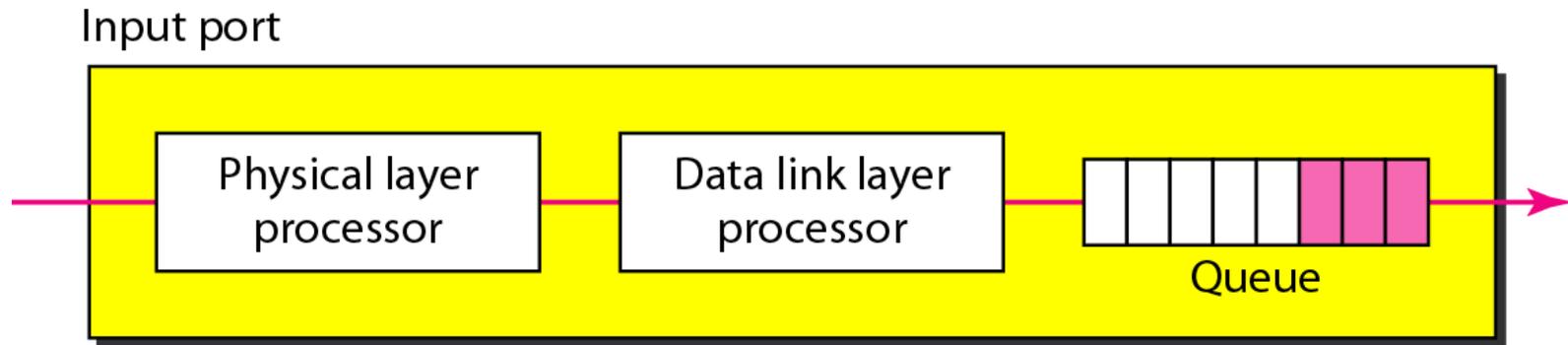
**Figure 8.20** *Time-space-time switch*



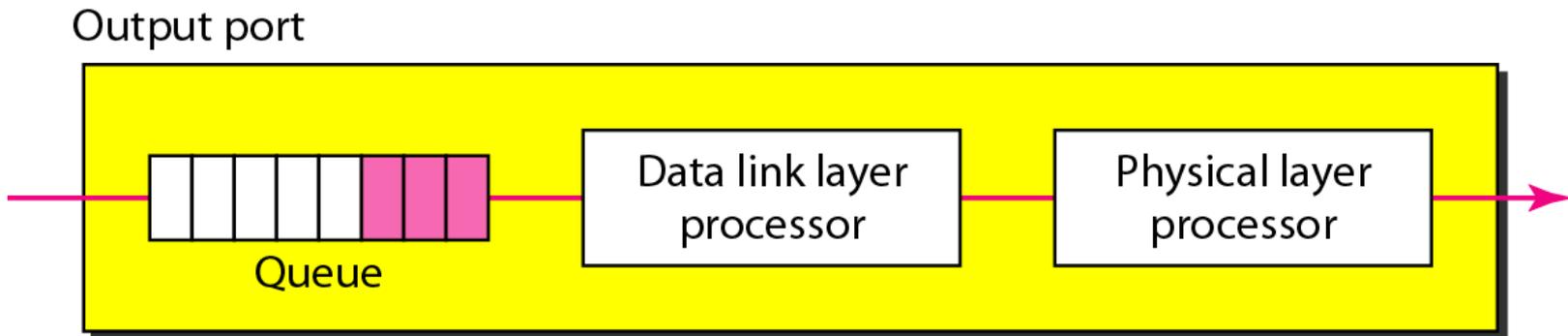
**Figure 8.21** *Packet switch components*



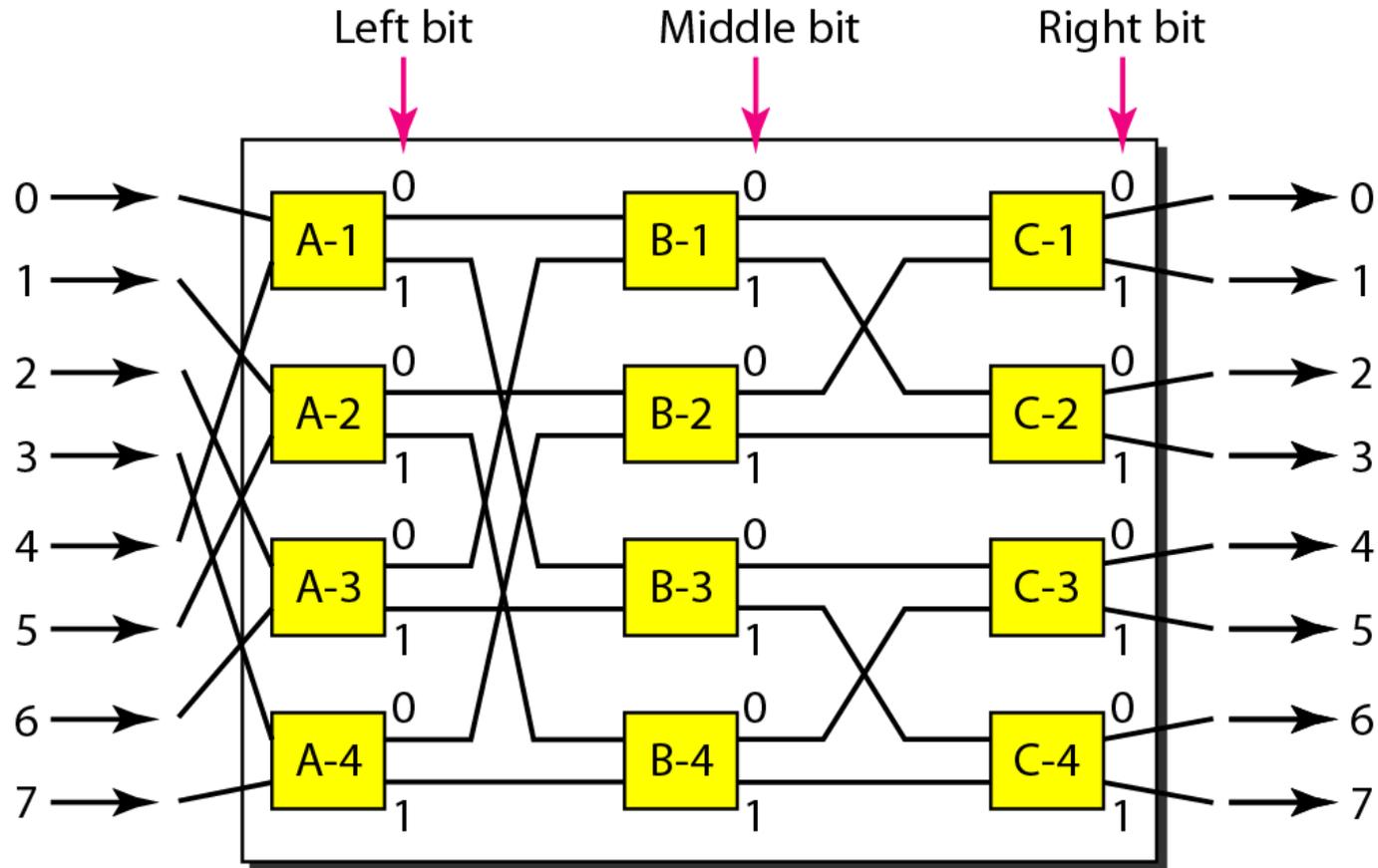
**Figure 8.22** *Input port*



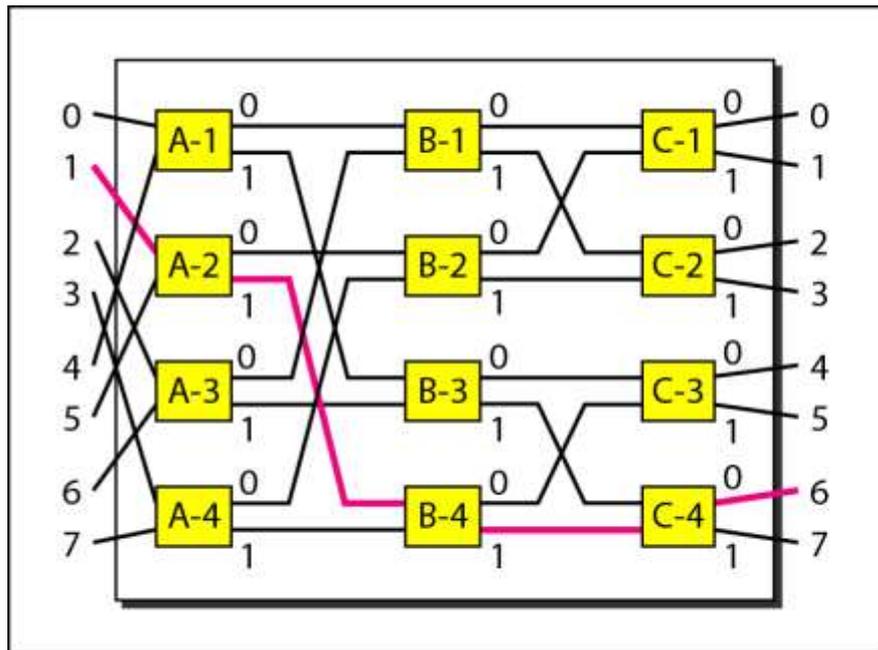
**Figure 8.23** *Output port*



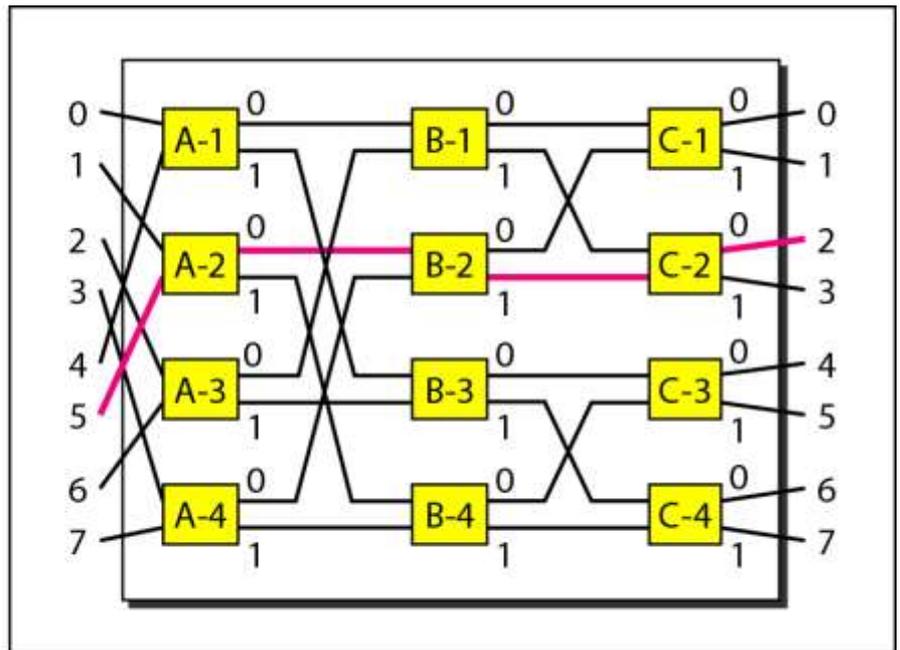
**Figure 8.24** *A banyan switch*



**Figure 8.25** *Examples of routing in a banyan switch*



a. Input 1 sending a cell to output 6 (110)



b. Input 5 sending a cell to output 2 (010)

**Figure 8.26** *Batcher-banyan switch*

