JNTUA UNIVERSITY
PREVIOUS QUESTION PAPERS
Part - A
(Compulsory Question)

1. Answer the following: (10 x 02 = 20 Marks)
   (a) What is the effect of positive feedback on stability?
   (b) Draw the speed-torque characteristics of AC servo motor.
   (c) What are the time response characteristics of first order system \( G(s) = \frac{1}{1+st} \) with unit step input?
   (d) Why derivative controller is not used alone in control systems?
   (e) What is the necessary and sufficient condition for stability in Routh’s stability criterion?
   (f) Define relative stability and mention the techniques which will be used for the measurement of relative stability.
   (g) What is the condition for stability in Bode diagram?
   (h) In minimum phase system, how the start and end of polar plot are identified?
   (i) State various properties of state transition matrix.
   (j) Define controllability.

Part - B
(Answer all five units, 5 x 10 = 50 Marks)

2. (a) What is meant by open loop and closed loop control systems? Differentiate both.
   (b) Find the closed loop transfer function of the following block diagram using block diagram reduction technique.

3. (a) With the help of necessary equations, derive the transfer function of DC servo motor.
   (b) With neat diagram, explain the operation of Synchro transmitter-receiver pair.

4. (a) Derive the expression for peak time and rise time in terms of \( \xi \) and \( \omega_n \) for a second order system.
   (b) Measurements conducted on a servomechanism shows the system response to be \( C(t) = 1 + 0.2e^{-0.1t} - 1.2e^{-10t} \) when subject to a unit step input. Obtain an expression for the closed loop transfer function. Determine the undamped natural frequency and damping ratio.

   Or

Contd. in page 2
5 (a) What is meant by transient response and steady state response? Explain in detail about various time domain specifications.

(b) Find the various static error constants for a unity feedback control system whose open loop transfer function is: \[ G(s) = \frac{10(s + 2)}{s^2(s + 1)}. \]

**UNIT – III**

6 With the help of Routh’s stability criterion find the stability of the following systems represented by the characteristic equations:

(i) \[ s^4 + 8s^3 + 18s^2 + 16s + 5 = 0. \]
(ii) \[ s^4 + 2s^5 + 8s^4 + 12s^3 + 20s^2 + 16s + 16 = 0. \]
(iii) \[ s^5 + s^4 + 2s^3 + 2s^2 + 3s + 5 = 0. \]

OR

7 Sketch the root locus of the system whose open loop transfer function is:

\[ G(s) = K/[s(s + 2)(s + 4)] \]

Find the value of \( K \) so that the damping ratio of the closed loop system is 0.5.

**UNIT – IV**

8 Draw the Bode plot for the system having:

\[ G(s) = \frac{75(1 + 0.2s)}{s^2 + 16s + 100} \]

From the above plot determine gain margin, phase margin and stability of the closed loop system.

OR

9 The open loop transfer function of a unity feedback system is given by:

\[ G(s) = \frac{1}{s^2(1+s)(1+2s)} \]

Sketch the polar plot and determine the gain margin and phase margin.

**UNIT – V**

10 (a) Write the state variable formulation of the following parallel RLC network. The current through the inductor and voltage across the capacitor are the output variables.

(b) Compute the resolvent matrix and state transition matrix of the state matrix: \( A = \begin{bmatrix} 0 & 1 \\ -1 & -2 \end{bmatrix} \).

**OR**

11 Diagonalize the given matrix \( A = \begin{bmatrix} 0 & 1 & 0 \\ 3 & 0 & 2 \\ -12 & -7 & -6 \end{bmatrix} \).

*....*
1 Answer the following: (10 X 02 = 20 Marks)
(a) Distinguish between open loop and closed loop systems.
(b) State Mason’s gain formula.
(c) List the time domain specifications.
(d) Determine the static error constants for a system given by: \( G(s)H(s) = \frac{10(s+2)(s+3)}{s(s+1)(s+4)(s+5)} \).
(e) State limitations for Routh’s stability.
(f) How do you determine the centroid and angle of asymptotes?
(g) Find the resonant frequency and resonant peak for a unity feedback system with: \( G(s) = \frac{100}{s(s+10)} \).
(h) What is Polar plot?
(i) What are the advantages of state space analysis?
(j) State the properties of state transition matrix.

2 (a) Write differential equations for the mechanical system shown in figure below.
(b) Explain with a neat sketch, the working of Synchro transmitter and Receiver.

OR

3 Determine the overall transfer function C/R for the block diagram shown in figure below by using block diagram reduction rules.
UNIT – II
4 Derive the expression for transient response of a under damped second order system with unit step input and draw the response curve.

OR
5 The block diagram of a unity feedback system is shown in figure below.

\[
\begin{align*}
\begin{array}{c}
R(s) \\
\end{array} \\
\begin{array}{c}
\frac{20}{(s+1)(s+5)} \\
\end{array} \\
\begin{array}{c}
C(s) \\
\end{array}
\end{align*}
\]

Determine the characteristic equation of the system: (i) Natural frequency. (ii) Damping factor. (iii) Damping frequency. (iv) Rise time. (v) Peak time. (vi) Peak overshoot.

UNIT – III
6 Determine the value of ‘a’ and ‘K’ at which a unity feedback control system having an open loop transfer function \( G(s) = \frac{K(s+1)}{s^2+aS^2+2S+1} \), will have sustained oscillations at \( \omega = 2 \) rad/sec.

OR
7 Sketch the root locus plot for a system described by: \( G(s)H(s) = \frac{K}{s(s+3)(s+6)} \). Comment on its stability. Determine the value of K for (i) critical damping (ii) Marginal stability (iii) for damping factor 0.6.

UNIT – IV
8 The open loop transfer function of a system is given by: \( G(s) = \frac{20}{s(s+1)(1+0.01s)} \). Sketch the Bode plot and determine the gain Margin and Phase Margin.

OR
9 The open loop transfer function of a system is given by: \( G(s) = \frac{40}{(s+4)(s^2+2s+1)} \). Sketch the Nyquist plot and comment on the stability of the system.

UNIT – V
10 Determine the state vector \( x(t) \) for the state model 
\[
\begin{bmatrix}
\dot{x}_1 \\
\dot{x}_2
\end{bmatrix} = 
\begin{bmatrix}
-12 & 2/3 \\
-36 & -1
\end{bmatrix}
\begin{bmatrix}
x_1 \\
x_2
\end{bmatrix} +
\begin{bmatrix}
1/3 \\
1
\end{bmatrix}u; \text{ and the initial conditions are } x_1(0) = 2, \ x_2(0) = 1.
\]

OR
11 State whether the system is controllable and observable for the linear time invariant system characterized by the state model:
\[
\begin{bmatrix}
\dot{x}_1 \\
\dot{x}_2
\end{bmatrix} = 
\begin{bmatrix}
0 & 1 \\
2 & -3
\end{bmatrix}
\begin{bmatrix}
x_1 \\
x_2
\end{bmatrix} +
\begin{bmatrix}
0 \\
1
\end{bmatrix}u; \ Y(t) = [1 \ 1] \begin{bmatrix}
x_1 \\
x_2
\end{bmatrix}
\]

****
1. Answer the following: (10 X 02 = 20 Marks)
   (a) List the advantages of negative feedback in control system.
   (b) Write the Mason’s gain formula of signal flow graph.
   (c) How do you find the type of a control system?
   (d) Find the value of position error constant for second order system using ramp input.
   (e) Write the necessary and sufficient condition for stability in Routh’s stability criterion.
   (f) Define BIBO stability.
   (g) Write the expression for resonant peak in frequency response analysis.
   (h) What is meant by lag compensation?
   (i) Define state and state variable.
   (j) What are the properties of state transition matrix?

2. Derive the transfer function of DC servomotor.
   OR
   3. Find the transfer function $\frac{C(S)}{R(S)}$ for the system using block diagram reduction technique.

4. (a) Transfer function of unity feedback control system is $G(s) = \frac{-25}{s(s+5)}$. Obtain the rise time, peak time, maximum overshoot and the settling time when the system is subjected to a unity step input.
   (b) Derive the time response of first order system for step input.

5. The open loop transfer function of a system with unity feedback $G(S) = \frac{10}{s(0.1s + 1)}$. Evaluate the static error constants of the system. Obtain the steady state error of the system, when subjected to an input given by the polynomial $r(t) = a_0 + a_1t + a_2t^2/2$. 

   Contd. in page 2
UNIT – III
6 Draw the root locus plot for the system whose open loop transfer function is given by:
\[ G(S)H(S) = \frac{K}{S(S + 4)(S^2 + 4S + 13)} \]
OR
7 Obtain the Routh array for the system whose characteristic polynomial equation is:
\[ S^6 + 2S^5 + 8S^4 + 12S^3 + 20S^2 + 16S + 16 = 0 \]. Check the stability.

UNIT – IV
8 Explain in detail about lag-lead compensator technique.
OR
9 The open loop transfer function of a unity feedback system is given by:
\[ G(S) = \frac{\frac{1}{S(1+S)(1+2S)}}{1} \]
Sketch polar plot and determine the gain and phase margin.

UNIT – V
10 Consider a system with state model given below:
\[ x = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -1 & -5 & -1 \end{bmatrix} x + \begin{bmatrix} 0 \\ 5 \\ -24 \end{bmatrix} u; \ y = \begin{bmatrix} 1 & 0 & 0 \end{bmatrix} x + [0] u \]
Verify, the system is observable and controllable.
OR
11 (a) Obtain the state model of the system described by the following transfer function:
\[ Y(s)/U(s) = \frac{5}{(s^2 + 6s + 7)}. \]
(b) Explain about diagonalization.
1. Answer the following: (10 X 02 = 20 Marks)
   (a) Compare open loop control system and closed loop control system.
   (b) What is servomechanism?
   (c) What is steady state error?
   (d) Mention two advantages of generalized error constants over static error constants.
   (e) How the roots of characteristic equation are related to stability?
   (f) What is centroid? How the centroid is calculated?
   (g) For a second order system, the damping ratio is 0.5 and natural frequency of oscillation is 8 rad/sec. Calculate resonant peak and resonant frequency.
   (h) What are the advantages of Bode plot?
   (i) What is companion or bush form of state model?
   (j) What are phase variables?

2. (a) Obtain the transfer function of below block diagram.

   ![Block Diagram](image)

   (b) Write the force balance and torque balance equations for basic elements in mechanical systems.

OR

3. (a) Obtain the transfer function of below signal flow graph using Mason’s Gain formula.

   ![Signal Flow Graph](image)

   (b) Obtain the transfer function of a armature controlled DC Servo motor.

Contd. in page 2
UNIT – II

4 (a) Derive an expression for the underdamped response of a second order feedback control system for step input.

(b) For a unity feedback control system, the open loop transfer function is: \( G(s) = \frac{10(s+2)}{s^2(s+1)} \). Find position, velocity and acceleration error constants.

OR

5 (a) For a unity feedback control system, the open loop transfer function is: \( G(s) = \frac{10(s+2)}{s^2(s+1)} \). Find steady state error when the input \( R(s) = \frac{3}{s} - \frac{2}{s^2} + \frac{1}{3s^2} \).

(b) Obtain expressions for rise time and peak time for a second order feedback control system for step input. (under damped case)

UNIT – III

6 (a) The open loop transfer function of a unity feedback control system is given by: \( G(s) = \frac{K}{(s+2)(s+4)(s^2+6s+25)} \). by applying Routh criterion, discuss the stability of the closed loop system as a function of K. Determine the values of K which will cause sustained oscillations in the closed loop system. What are the corresponding oscillation frequencies?

(b) Define the following terms with respect to Root locus technique:
(i) Centroid. (ii) Asymptote. (iii) Break away point.

OR

7 (a) The open loop transfer function of a unity feedback control system is given by: \( G(s) = \frac{K(s+9)}{s(s^2+4s+11)} \). Sketch the root locus of the system.

(b) Using Routh criterion, determine the stability of the system represented by the characteristic equation \( s^2 + 8s^3 + 18s^2 + 16s + 5 = 0 \). Comment on the location of the roots of characteristic equation.

UNIT – IV

8 (a) The open loop transfer function of a system is \( G(s)H(s) = \frac{(1+4s)}{s^2(1+sT_1)(1+sT_2)} \). Sketch the Nyquist plot and determine the stability of the closed loop system. If the closed loop system is not stable then find the number of closed loop poles lying on the right half of s plane.

(b) Sketch the polar plot of:
(i) \( G(s) = \frac{1}{s^2(1+sT_1)(1+sT_2)} \).
(ii) \( G(s) = \frac{1}{(1+sT_1)(1+sT_2)(1+sT_3)} \).
(iii) \( G(s) = \frac{1+sT}{sT} \).

OR

9 The open loop transfer function of a unity feedback control system is given by \( G(s) = \frac{K^e^{-0.2s}}{s(s+2)(s+8)} \). Draw the Bode plot and find K so that the system is stable with, (i) Gain margin is equal to 2db. (ii) Phase margin is equal to 45\(^0\).

UNIT – V

10 (a) Determine the canonical state model of the system whose transfer function is: \( T(s) = \frac{2(s+5)}{(2s)(s+3)(s+4)} \) and draw block diagram representation of the state model.

(b) Write the properties of state transition matrix.

OR

11 (a) Determine the state model of the system whose transfer function is: \( T(s) = \frac{10}{s^2+4s^2+2s+1} \) and draw block diagram representation of the state model.

(b) Define controllability and observability and state the condition for controllability and observability.

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CONTROL SYSTEMS ENGINEERING

Time: 3 hours                                                                                                           Max. Marks: 70

PART – A
(Compulsory Question)

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1 Answer the following: (10 X 02 = 20 Marks)
   (a) What is the effect of positive feedback on stability of the system?
   (b) What is the basic rule used for block diagram reduction technique?
   (c) What are test signals and write their significance?
   (d) Define IAE, ITAE.
   (e) Determine the stability of the system whose characteristic equation is given by:
\[ S^4 + 6S^3 + 23S^2 + 40S + 50 = 0 \] using Routh’s stability criterion.
   (f) Draw the Root-Locus plot of \[ G(S) H(S) = \frac{K}{S+P}. \]
   (g) Define gain margin and phase margin.
   (h) Define state and state variable.
   (i) What are the advantages of state space modeling using physical variables?
   (j) What is similarity transformation?

PART – B
(Answer all five units, 5 X 10 = 50 Marks)

UNIT – I

2 (a) Explain the operation of synchro transmitter and receiver.
(b) Write the block diagram reduction techniques in the analysis of control systems.

OR

3 (a) Write the analogy between mechanical systems and electrical systems.
(b) Determine C/R of the system shown in figure below by block diagram reduction technique.

\[
\begin{align*}
R & \rightarrow \bigoplus \rightarrow G_1 \rightarrow \bigoplus \rightarrow G_2 \rightarrow -H_1 \rightarrow C
\end{align*}
\]

UNIT – II

4 (a) For a unity feed-back system whose open-loop transfer function is \[ G(S) = \frac{100}{(1+0.25)(1+25)}. \] Find the position, velocity and acceleration error constants.
(b) What will be the nature of response of a second order system with different types of damping?

OR

5 (a) Derive the expression for 2nd order system under damped system with unit step as input.
(b) The open loop, transfer function of a unity feedback system is \[ G(S) = \frac{1}{1+S}. \] Using generalized error series determine the steady state error when the system is excited by \[ R(t) = 1 + t + t^2. \]

Contd. in page 2
6 (a) The open loop transfer function of a unity feedback system is given by \( G(S) = \frac{K}{S(S + 3)(S^2 + S + 1)} \). Determine the values of 'K' that will cause sustained oscillations in the closed loop system. Also find the oscillation frequency.

(b) What is centroid and how it is calculated?

OR

7 Sketch the root locus for the open loop transfer function of unity feedback control system given by \( G(S) H(S) = \frac{K}{S(S + 1)(S + 2)} \). Also find K of breakaway point.

UNIT – IV

8 (a) Sketch polar plot of \( G(S) = \frac{1}{(1 + ST_1)(1 + ST_2)} \).

(b) The open-loop transfer function of closed loop system is \( G(S) H(S) = \frac{1 + 4S}{S^2(S + 1)(2S + 1)} \). Determine the stability using Nyquist criterion.

OR

9 Sketch the bode plot for the transfer function \( G(S) = \frac{KS^2}{(1 + 0.2S)(1 + 0.25)} \). Determine the system gain ‘K’ for the gain cross-over frequency to be 5 rad/sec.

UNIT – V

10 (a) Explain various methods of evaluation of state transition matrix.

(b) Given \( \dot{x}(t) = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} x(t) = A.x(t) \). Find Eigen values, vectors and response when X(0) = \( \begin{bmatrix} 1 \\ 1 \end{bmatrix} \).

OR

11 (a) Discuss the merits and demerits of representing a state model into: (i) Phase variable form. (ii) Canonical form.

(b) Find the state transition matrix for \( \dot{X} = \begin{bmatrix} -2 & 1 & 0 \\ 0 & -2 & 1 \\ 0 & 0 & -2 \end{bmatrix} x \).
PART – A
(Compulsory Question)
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1. Answer the following: (10 x 02 = 20 Marks)
   (a) If a forward path touched all closed loops, what would be the value of $\Delta_k$?
   (b) Write the analogous electrical elements in force voltage analogy for the elements of mechanical translational system.
   (c) Define impulse signal with its waveform.
   (d) How the system was classified depending on the value of the damping?
   (e) Why marginally stable systems are considered unstable under the BIBO definition of stability?
   (f) What kind of compensation improves the steady-state error?
   (g) Write a short note on the correlation between the time and frequency response.
   (h) How closed loop frequency response is determined from open loop frequency response using M and N circles?
   (i) How can the poles of a system be found from the state equations?
   (j) Write the general form of the state-transition matrix. How many constants would have to be found?

PART – B
(Answer all five units, 5 x 10 = 50 Marks)

UNIT – I

2. Using Mason’s rule, find the transfer function, $G(s) = \frac{C(s)}{R(s)}$, for the system represented by figure below.

OR

3. A motor and generator are set up to drive a load as shown in figure below. If the generator output voltage is $e_g = K_f i_f(t)$, where $i_f(t)$ is the generator’s field current, find the transfer function $G(s) = \frac{\theta(s)}{E_i(s)}$. For the generator, $K_f = 2 \Omega$. For the motor, $K_t = 1 - m/A$, and $K_b = 1 V/s/rad$. 

Contd. in page 2
UNIT – II

4 For the system of figure below, find the values of \( K_1 \) and \( K_2 \) to yield a peak time of 1.5 second and a settling time of 3.2 seconds for the closed-loop system’s step response.

![System Diagram]

**OR**

5 (a) What pole locations characterize: (i) The under damped system. (ii) The over damped system. (iii) The critically damped system.
(b) A system has a damping ratio of 0.5, a natural frequency of 100 rad/s and a DC gain of 1. Find the response of the system to a unit step input.

UNIT – III

6 Consider the unity feedback system shown with transfer function \( G(s) = \frac{K}{s(s+4)(s+6)} \). Draw the root locus and identify the stability.

**OR**

7 Using the Routh-Hurwitz criterion and the unity feedback system with \( G(s) = \frac{K}{s(s+1)(s+2)(s+3)} \).
(i) Find the range of K for stability. (ii) Find the value of K for marginal stability. (iii) Find the actual location of the closed-loop poles when the system is marginally stable.

UNIT – IV

8 Make a polar plot of the frequency response for the transfer function given by: \( G(s) = \frac{(s+5)}{s(s+2)(s+4)} \)

**OR**

9 Given a unity feedback system with the forward-path transfer function \( G(s) = \frac{K}{s(s+1)(s+3)(s+6)} \) and a delay of 0.5 second, find the range of gain, K, to yield stability. Use Bode plots.

UNIT – V

10 Give the following state-space representation of a system, find Y(s):

\[
\begin{bmatrix}
0 & 1 & 0 \\
-2 & -4 & 1 \\
0 & 0 & -6
\end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} e^{-t}
\]

\[
Y = \begin{bmatrix} 0 & 0 & 1 \end{bmatrix} X; \quad X(0) = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}
\]

**OR**

11 Solve for y(t) for the following system represented in state space, where u(t) is the unit step. Use the Laplace transform approach to solve the state equation.

\[
\begin{bmatrix}
-3 & 1 & 0 \\
0 & -6 & 1 \\
0 & 0 & -5
\end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u(t)
\]

\[
Y = \begin{bmatrix} 0 & 1 & 1 \end{bmatrix} X; \quad X(0) = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}
\]

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Part – A
(Compulsory Question)

1. Answer the following: (10 x 02 = 20 Marks)
   (a) Why is negative feedback preferred as compared to positive feedback in a closed loop system?
   (b) Write any three basic properties of signal flow graph.
   (c) Mention any two advantages of generalized error coefficients.
   (d) A unity feedback system has a open loop transfer function of \( \frac{10}{(s+1)(s+2)} \). Determine steady state error for unit step input.
   (e) State the rule for finding the value of gain \( K \) at any point \( s_0 \) on the root locus diagram.
   (f) In Routh array what conclusion you can make when there is a row of all zeros?
   (g) Mention any two advantages and any two disadvantages of frequency response analysis.
   (h) Which characteristic feature of the lag network is utilized for compensation?
   (i) Give the expression to obtain the transfer function of a system from the given state model:
      \[ X = AX + BU \]
      \[ Y = CX + DU \]
   (j) Is the state-model of a system unique?

Part – B
(Answer all five units, 5 x 10 = 50 Marks)

2. (a) Compare the merits and demerits of open loop and closed loop systems with examples
   (b) Obtain the transfer function for the signal flow graph given in figure below, using Mason’s gain formula.

OR

3. Write the torque equations of the rotational system shown in figure below. Draw the analogous electrical networks based on: (i) Torque-current. (ii) Torque-voltage analogies.
UNIT – II

4 (a) Define the following time domain specifications: (i) Rise time. (ii) Delay time. (iii) Peak time. (iv) Peak overshoot. (v) Settling time.

(b) A Unity feedback control system is characterized by the following open-loop transfer function
\[ G(s) = \frac{0.4(s+1)}{s(s+0.6)} \]. Determine its transient response for a unit-step input. Evaluate the maximum overshoot and the corresponding peak time.

OR

5 (a) Write the merits and demerits of: (i) Proportional only controller. (ii) Integral controller.

(b) Determine the values of \( K \) and \( P \) of the closed-loop system shown in figure below, so that the maximum overshoot in the unit-step response is 25% and the peak time is 2 seconds. Assume that \( J = 1 \text{ kg-m}^2 \).

\[ \text{Figure: Control System Diagram} \]

UNIT – III

6 (a) What are the difficulties in the formulation of the Routh table? Explain how they can be overcome.

(b) The characteristic polynomial of a system is:
\[ s^7 + 9s^6 + 24s^5 + 24s^4 + 24s^3 + 23s^2 + 15s = 0 \]. Determine the location of roots on s-plane and hence the stability of the system.

OR

7 Draw the complete root locus for \( G(s)H(s) = \frac{K}{s(s+2)(s+4)} \). From the root locus plot, find the range of values of \( K \) for which the system will have damped oscillatory response. Also determine the value of \( K \) for a damping ratio of 0.5. With this value of \( K \), find the closed-loop transfer function.

UNIT – IV

8 Sketch the Bode plot for the following transfer function and determine the system gain \( K \) for the gain cross over frequency to be 5 rad/sec.
\[ G(s) = \frac{Ks^2}{(1+0.2s)(1+0.02s)} \]

OR

9 (a) Sketch the Nyquist plot and comment on the stability of the closed loop system whose open loop transfer function is \( G(s)H(s) = \frac{K(s-4)}{(s+1)^2} \).

(b) Write the procedure for design of lead compensator using Bode plot.

UNIT – V

10 (a) Distinguish between transfer function approach and state variable approach.

(b) Obtain the state model for the transfer function of a control system given by:
\[ \frac{Y(s)}{U(s)} = \frac{s^2 + 3s + 4}{s^3 + 2s^2 + 3s + 2} \]

OR

11 (a) Write the properties of state transition matrix.

(b) Diagonalize the system matrix given below:
\[ A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -6 & -11 & -6 \end{bmatrix} \]

*****
PART – A

(Compulsory Question)

*****

1. Answer the following: (10 X 02 = 20 Marks)
   (a) Prove that the closed loop transfer function of a unity negative feedback control system having the forward path transfer function \( G(s) \) is given by \( \frac{G(s)}{1+G(s)} \).
   (b) In an electrical circuit \( i = C \frac{dv}{dt} \) where \( i \) is current, \( C \) is Capacitance and \( V \) is Voltage. Write the analogous equations for: (i) Mechanical (translational) system. (ii) Mechanical (rotational) system. Use force-current analogy.
   (c) Define ‘TYPE’ and ‘ORDER’ of a system. What are the TYPE and ORDER of \( \frac{G(s)}{s(1+s)} \)?
   (d) What is the effect of adding integral action to a proportional controller on: (i) Steady state error? (ii) Relative stability?
   (e) What is the location of breakaway point in the root locus for the open loop transfer function: \( G(s)H(s) = \frac{K}{(s+2)(s+4)} \).
   (f) When is a system said to be Bounded Input-Bounded Output (BIBO) stable? What is the condition on impulse response for BIBO stability?
   (g) A unity feedback system has \( G(s) = \frac{100}{s(s+10)} \). What is the resonant frequency of the system?
   (h) What is the importance of cut-off frequency and cut-off rate in control systems?
   (i) Define ‘State’ and ‘State variables’.
   (j) What is the characteristic equation of a system having the State Matrix?

\[
A = \begin{bmatrix}
0 & 2 & 0 \\
4 & 0 & 1 \\
-48 & -34 & -9
\end{bmatrix}
\]

PART – B

(Answer all five units, 5 X 10 = 50 Marks)

UNIT – I

2. Find the overall transfer function, from \( R(s) \) to \( C(s) \), of the system shown below.

3. With the help of necessary diagrams, describe the constructional and operational features of A.C Servo Motors. Derive the transfer function between the rotor position and error signal of an A.C Servo motor.

Contd. in page 2
UNIT – II

4 (a) A system has the closed loop transfer function \( \frac{\omega_n^2}{s^2 + 2\zeta\omega_n s + \omega_n^2} \). It is required that the unit step response of the system should have a settling time of 2 sec according to 2% criterion; and the overshoot should be approximately 5%. What should be the closed loop pole locations?

(b) A unity feedback control system has the closed loop transfer function \( \frac{k s + b}{s^2 + a s + b} \). Determine the steady state error in the unit ramp response, in terms of \( k, a, \) and \( b \).

OR

5 Derive the expressions for: (i) Rise time. (ii) Peak time. (iii) Maximum overshoot. (iv) Settling time of the unit-step response of an under damped prototype second order system. Hence determine the quantities for a system having the closed loop transfer function \( \frac{16}{s^2 + 2s + 16} \).

UNIT – III

6 (a) How many roots of the characteristic polynomial of a system \( s^3 - s^2 - 2s + 2 \) have positive real parts?

(b) Determine the value of \( K \) for which the characteristic polynomial of a system \( s^4 + 8s^3 + 24s^2 + 32s + K \) has roots with zero real part.

OR

7 A unity feedback system has the open loop transfer function \( G(s) = \frac{K}{s(s+2)(s^2+4s+25)} \).

(a) Sketch the root locus for \( 0 \leq K \leq \infty \).

(b) At what value of \( K \) does the system become unstable?

(c) What is frequency of sustained oscillations of the system when it just loses stability?

UNIT – IV

8 (a) Draw the Bode plot and determine the Gain Margin and Phase Margin for \( G(s)H(s) = \frac{e^{-0.2s}}{s(s+1)} \).

(b) A Unity feedback control system has the Open Loop Transfer Function \( G(s) = \frac{as + 1}{s^2} \). What should be the value of \( a \) for the system to have Phase Margin of \( 45^0 \).

OR

9 (a) Draw a network of lag-lead compensator consisting of resistors and capacitors and derive its transfer function.

(b) Draw the Nyquist plot for the open loop transfer function \( G(s)H(s) = \frac{(s+2)}{(s+1)(s-1)} \). Applying Nyquist stability criterion, determine whether the closed loop system is stable or not.

UNIT – V

10 Obtain the state model for the system represented by:

\[
\frac{d^3y}{dt^3} + 6 \frac{d^2y}{dt^2} + 11 \frac{dy}{dt} + 10y = 3u(t).
\]

OR

11 The state space representation of a system has the characteristic matrix \( A = \begin{bmatrix} 0 & 1 \\ -2 & 0 \end{bmatrix} \) and output matrix \( C = \begin{bmatrix} 1 & -1 \end{bmatrix} \). Find the zero excitation response of the system for \( X(0) = \begin{bmatrix} 1 \\ 1 \end{bmatrix} \).

*****
PART – A
(Compulsory Question)

1. Answer the following: (10 X 02 = 20 Marks)
   (a) What is the effect of positive feedback on stability?
   (b) What are the differences between Synchro transmitter and control transformer?
   (c) The closed loop transfer function of a second order system is \( \frac{C(s)}{R(s)} = \frac{10}{s^2 + 6s + 10} \). What is the type of damping in the system?
   (d) Why derivative controller is not used alone in control systems?
   (e) What is the necessary and sufficient condition for stability in Routh’s stability criterion?
   (f) What is meant by damping pole in Root locus diagram?
   (g) Define Gain margin and Phase margin.
   (h) In minimum phase system, how the start and end of polar plot are identified?
   (i) State various properties of state transition matrix.
   (j) What are the advantages of state space analysis over transfer function analysis?

PART – B
(Answer all five units, 5 X 10 = 50 Marks)

UNIT – I

2. (a) What is meant by open loop and closed loop control systems? Differentiate them.
    (b) Find the closed loop transfer function of the following block diagram using reduction technique.

OR

3. (a) Define transfer function and also derive transfer function for AC Servo motor.
    (b) With the help of Mason’s gain formula find the overall transfer function of the following signal flow graph.
UNIT – II

4 (a) Obtain the response of a first order system \( \frac{C(s)}{R(s)} = \frac{1}{1+7s} \) for unit step input.

(b) A closed loop servo is represented by the differential equation: \( \frac{dc}{dt} + 8 \frac{dc}{dt} = 64e \). Where ‘c’ is the displacement of the output shaft, ‘r’ is the displacement of the input shaft and \( e = r - c \). Determine undamped natural frequency, damping ratio and percentage maximum overshoot for unit step input.

5 (a) What is meant by transient response and steady state response? Explain in detail about various time domain specifications.

(b) Find the various static error constants for a unity feedback control system whose open loop transfer function is: \( G(s) = \frac{10(s+2)}{s^2(s+1)} \).

UNIT – III

6 With the help of Routh’s stability criterion find the stability of the following systems represented by the characteristic equations:

(i) \( s^4 + 8s^3 + 18s^2 + 16s + 5 = 0 \).

(ii) \( s^6 + 2s^5 + 8s^4 + 12s^3 + 20s^2 + 16s + 16 = 0 \).

(iii) \( s^5 + s^4 + 2s^3 + 2s^2 + 3s + 5 = 0 \).

OR

7 A negative feedback control system has the forward path transfer function: \( G(s) = \frac{K(s+1)}{s(s-1)(s^2 + 6s + 25)} \). Draw the root locus for \( 0 \leq K \leq \infty \).

UNIT – IV

8 Sketch the bode plot for the following transfer function and determine phase margin and gain margin:

\( G(s) = \frac{75(1+0.2s)}{s(s^2 + 16s + 100)} \).

OR

9 The open loop transfer function of a unity feedback system is given by: \( G(s) = \frac{1}{s^2 (1+s)(1+2s)} \). Sketch the polar plot and determine the gain margin and phase margin.

UNIT – V

10 (a) Write the state variable formulation of the following parallel RLC network. The current through the inductor and voltage across the capacitor are the output variables.

![Parallel RLC network diagram]

(b) Compute the resolvent matrix and state transition matrix of the state matrix: \( A = \begin{bmatrix} 0 & 1 \\ -1 & -2 \end{bmatrix} \).

OR

11 (a) Obtain the state model of the transfer function:

\[ \frac{Y(s)}{U(s)} = \frac{s^2 + 3s + 4}{s^3 + 2s^2 + 3s + 2} \]

(b) Diagonalize the system matrix, \( A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -6 & -11 & -6 \end{bmatrix} \).

*****
PART – A
(Compulsory Question)

1. Answer the following: (10 × 02 = 20 Marks)
   (a) Name three basic forms for interconnecting subsystems.
   (b) What is sink and source?
   (c) What is proportional controller and what are its advantages?
   (d) State the importance of test signals.
   (e) What would happen to a physical system that becomes unstable?
   (f) When the maximum phase lead occurs in lead compensator?
   (g) What are the frequency domain specifications?
   (h) What are advantages of frequency response analysis?
   (i) Write short notes on BIBO stability.
   (j) Briefly describe the design procedure for a controller.

PART – B
(Answer all five units, 5 × 10 = 50 Marks)

UNIT – I

2. Reduce the block diagram using reduction technique, shown in figure below to a single block, \( T(s) = \frac{C(s)}{R(s)} \).

OR

3. Consider the rotational mechanical system shown below represent the system as a signal-flow graph. And calculate the transfer function of the system if the output is \( \theta_2(t) \).

Contd. in page 2
UNIT – II

4 For the system shown in figure below, find the following: (i) The damping ratio. (ii) Natural frequency. (iii) % overshoot. (iv) Settling time. (v) Peak time. (vi) Rise time. (vii) Damped frequency of oscillation.

OR

5 (a) Sketch the time response of the second order system and explain each component briefly.
(b) For the system shown in figure below, find K and \( \alpha \) to yield a settling time of 0.15 second and a 30% overshoot.

UNIT – III

6 Determine the stability of the closed-loop transfer function using R-H criteria.

\[
G(s) = \frac{K}{s^3 + 2s^2 + 3s^2 + 6s + 5 + 3}
\]

OR

7 Consider the unity feedback system shown with transfer function: 

\[
G(s) = \frac{K}{s(s+3)(s+5)(s+7)}
\]

Draw the root locus and identify the stability.

UNIT – IV

8 For the given transfer function: 

\[
G(s) = \frac{1}{s(s+2)(s+4)}
\]

sketch the Bode asymptotic magnitude and asymptotic phase plots.

OR

9 Consider the unity feedback system shown with the transfer function: 

\[
G(s) = \frac{8000}{(s+6)(s+20)(s+35)}
\]

Find the:

UNIT – V

10 (a) What are the properties of state transition matrix?
(b) Given the system represented in state space by:

\[
\begin{align*}
\dot{X} &= \begin{bmatrix} 0 & 2 \\ -2 & -5 \end{bmatrix} X + \begin{bmatrix} 0 \\ 1 \end{bmatrix} e^{-2t} \\
Y &= \begin{bmatrix} 2 & 1 \end{bmatrix} X \\
X(0) &= \begin{bmatrix} 1 \\ 2 \end{bmatrix}
\end{align*}
\]

Solve for the state transition matrix.

OR

11 A system is represented by the state and output equations that follow.

Find: (i) The characteristic equation. (ii) The poles of the system.

\[
\begin{align*}
\dot{X} &= \begin{bmatrix} 0 & 2 & 3 \\ 0 & 6 & 5 \\ 1 & 4 & 2 \end{bmatrix} X + \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix} u(t) \\
Y &= \begin{bmatrix} 1 & 2 & 0 \end{bmatrix} X
\end{align*}
\]

*****
PART – A
(Compulsory Question)

1. Answer the following: (10 X 02 = 20 Marks)

(a) List all electrical analogs of rotational mechanical systems using force-current analogy.

(b) A closed loop control system has an open loop gain of 100. Its feedback loop has a gain of 0.005. Find its sensitivity for negative feedback.

(c) Write the expressions for the response of first order system to the unit step input signal and unit ramp input signal in time domain.

(d) What is a type 1 system? What is its steady state error for unit ramp input?

(e) Determine the stability of the system with the characteristic equation $s^4 + s^3 + s^2 + 4s + 6 = 0$.

(f) Discuss the effect of addition of open loop poles on the root loci.

(g) Define gain margin.

(h) Define gain cross-over point.

(i) Define the state of a system.

(j) Derive the response of unforced system.

PART – B
(Answer all five units, 5 X 10 = 50 Marks)

UNIT – I

2. Find the transfer function matrix for the two input two output system shown in the figure below.

OR

3. Develop a signal flow graph for the motor shown in figure below with the given constants. Find the transfer function $\frac{\theta_m(s)}{V_a(s)}$ using Mason’s formula.

Contd. in page 2
UNIT – II

4. A unity feedback system has an open loop transfer function \( G(s) = \frac{25}{s(s+8)} \). Determine its damping ratio, peak overshoot and time required to reach the peak output. Now a derivative component having transfer function of \( \frac{1}{s^2} \) is introduced in the system. Discuss its effect on the values obtained.

OR

5. A unity feedback system having open loop transfer function as \( G(s) = \frac{k(s+2)}{s(s^2+7s^2+12s)} \), determine: (i) Type of system. (ii) \( k_p \), \( k_i \) and \( k_a \). (iii) Steady state error for parabolic input.

UNIT – III

6. Sketch the root locus for a unity feedback system having \( G(s) = \frac{k(s+1)}{s^2(s+5)} \).

OR

7. The open loop transfer function of a unity feedback system is given by \( G(s) = \frac{k}{s(s+2)(s^2+6s+25)} \). Sketch the root locus for \( 0 \leq k \leq \infty \).

UNIT – IV

8. Consider the transfer function \( GH(s) = \frac{60}{(s+1)(s+2)(s+5)} \). Comment on stability of the system using the sketch of its Nyquist plot.

OR


UNIT – V

10. Consider the electric circuit shown in the figure below, where \( e_1 \) and \( e_2 \) are the inputs and \( v_1, v_2, v_3 \) are outputs. Choosing \( i_1, i_2 \) and \( i_3 \) as the state variables, determine the system equations and write the state model.

11. Consider the system \( \dot{X} = AX \) with \( X_0 = X(0) \) where \( A = \begin{bmatrix} -2 & -4 \\ 1 & -2 \end{bmatrix} \). Find \( \phi(t) \) and the solution for \( X_0 = [1 \ 1]^T \).

****
1. Answer the following: (10 X 02 = 20 Marks)
   (a) What is the feedback? What are the characteristics of negative feedback?
   (b) Define transfer function. Write the Mason’s gain formula to find transfer function and explain each term in it.
   (c) The open loop transfer function of a unity feedback system is $G(s) = 20/(s(s + 10))$. What is the nature of response of closed loop system for unit step input?
   (d) Give the relation between generalized and static error coefficients.
   (e) What are asymptotes? How will you find the angle of asymptotes?
   (f) In Routh array what conclusions you can make when there is a row of all zeros.
   (g) Draw the polar plot of $G(s) = 1/(1 + ST)$.
   (h) Mention the advantages of Bode plot.
   (i) What is meant by state, state variable and state model?
   (j) Define state transition matrix and explain its significance on stability of the system.

2. (a) What are the various types of control systems? Give an example of each. What are the advantages and disadvantages of open loop and closed loop systems?
   (b) Find the transfer function $\frac{\theta(s)}{r(s)}$ for the figure given below.

   \[ \text{Diagram:} \]

   OR

3. (a) Derive the transfer function of AC servomotor.
   (b) Using block diagram reduction technique, obtain closed loop transfer function of the figure give below.

   \[ \text{Diagram:} \]
UNIT – II

4  (a) Obtain the time response of undamped second order system for unit step input.
    (b) A unity feedback system has the forward transfer function: \( G(s) = \frac{K_{1}(2s+1)}{s(s+1)(1+s)^2} \). The input \( r(t) = 1 + 6t \) is applied to the system. Determine the value of \( K_{1} \) if the steady error is to be less than 0.1.

OR

5  (a) A unity feedback control system has an open loop transfer function: \( G(s) = \frac{10}{S(S+2)} \). Find the time domain specifications for a step input of 12 units.
    (b) Explain the effect of PI and PD controllers on transient response of the system.

UNIT – III

6  (a) The open loop transfer function of a unity feedback system is given by \( G(s) = \frac{K_{2}(s+1)}{s^3+as^2+bs+1} \). Determine the value of \( K \) and so that the system oscillates at a frequency of 2 rad/sec.
    (b) Explain the effect of adding poles and zeros to characteristic equation on stability of the root loci.

OR

7  Sketch the root locus of the system whose open loop transfer function is \( G(S) = \frac{K}{S(S+2)(4+S)} \). Find the value of \( K \) so that the damping ratio of the closed loop system is 0.5.

UNIT – IV

8  (a) Explain the frequency response specifications.
    (b) The transfer function of a phase-lead controller is given as \( G(s) = \frac{1+asT}{1+aTs} \), \( a > 1 \) and \( T \) is constant depending on the circuit parameters. Determine the maximum value of the phase load which can be obtained from this controller.

OR

9  Sketch the bode plot and find gain margin & phase margin of the systems represented by:
    \( G(s)H(s) = \frac{75(0.25+1)}{S(S^2+16S+100)} \).

UNIT – V

10 (a) Discuss about the properties of state transition matrix.
     (b) The state equation of a linear-time invariant system is given:
         \[
         \begin{bmatrix}
         \dot{X}_1 \\
         \dot{X}_2 
         \end{bmatrix}
         = \begin{bmatrix}
         0 & 5 \\
         -1 & -2 
         \end{bmatrix}
         \begin{bmatrix}
         X_1 \\
         X_2 
         \end{bmatrix}
         + \begin{bmatrix}
         1 \\
         1 
         \end{bmatrix}u 
         \text{ and } Y = \begin{bmatrix}
         1 \\
         1 
         \end{bmatrix}X 
         
         \text{Determine state transition matrix.}

OR

11 (a) Determine the transfer function for following system given below:
      \[
      [X] = \begin{bmatrix}
      0 & 3 \\
      -2 & -5 
      \end{bmatrix}[X] + \begin{bmatrix}
      1 \\
      1 
      \end{bmatrix}[U] \text{ and } Y = \begin{bmatrix}
      2 & 1 \\
      1 & 0 
      \end{bmatrix}X 
      \]
      (b) A state model of a system is given as:
      \[
      \dot{X} = \begin{bmatrix}
      0 & 1 & 0 \\
      0 & 0 & 1 \\
      -1 & -3 & -3 
      \end{bmatrix}[X] + \begin{bmatrix}
      0 \\
      0 \\
      0 
      \end{bmatrix}U \text{ and } Y = \begin{bmatrix}
      1 & 0 \\
      0 & 0 
      \end{bmatrix}X 
      \]
      \text{Determine: (i) The Eigen values. (ii) The state transition matrix.}

*****